A causality-based method for multi-model comparison: Application to relationships between atmospheric, oceanic and marine biogeochemical variables

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Abstract. We introduce ~~an novel~~ a novel causality-based approach to compare Earth System Model ~~output using a causality-based approach~~outputs. The method is based on the PCMCI+ algorithm, which identifies causal relationships between multiple variables. We aim to investigate the causal relationships between atmospheric (North Atlantic Oscillation - NAO), oceanic (gyre strength, stratification, circulation), and biogeochemical variables (nitrate, iron, silicate, phosphate and net primary production) in the North Atlantic subpolar gyre~~,~~. It is a critical region for the global climate system with a well characterised multi-year variability in physical and biogeochemical properties in response to the North Atlantic Oscillation. We test a specific multivariate conceptual scheme, involving causal links between these variables. Applying the PCMCI+ method allows us to differentiate between the influence of vertical mixing and horizontal advection on nutrient concentrations, spring bloom intensity, as well as to highlight model-specific dynamics. The analysis of the causal links suggests a dominant contribution of winter vertical mixing to ~~peak spring bloom intensity~~ nutrient concentration compared to transport. The strength of the links is variable among models. Stratification is identified as an important factor controlling spring bloom NPP in some, but not all, models. Horizontal transport also significantly influences ~~biogeochemistry~~nutrient concentration. However, horizontal transport generally exhibits lower contributions than vertical mixing ~~. Most of the links found are model-specific, hence likely contributing to inter-model spread~~to nutrient variability. The limitations of the method are discussed and directions for future research are suggested.

1 Introduction

Earth System models (ESMs) are essential tools in climate science. They are designed to unravel the intricate workings of the planet's climate system. The simulation of historical and present dynamics have proven to be skillful in many aspects, including the representation of ocean physics and marine biogeochemistry (Flato et al., 2014; Séférian et al., 2020; Vautard et al., 2021; Tsujino et al., 2020). Despite advances in complexity, ESMs simplify the real world and this is a source of errors and uncertainties. These models create their own climate system shaped by specific spatial resolutions and parameterizations of various physical, chemical or biogeochemical processes. Multiple reasons explain the differences in architecture between models (Bonan and Doney, 2018): the constraint of computational efficiency which calls for the parameterization of small-scale processes unresolved by the large-scale variables in the model, but also the selection of which processes to include. Given the

inherent complexity of the climate system, encompassing myriad of processes currently impossible to be represented in a

25 model, these disparities can lead to differences in future climate states and dynamics ~~leading to projections with still scattered outcomes~~ with scattered projections (e.g., Kwiatkowski et al., 2020; Tebaldi and Knutti, 2007; Flato et al., 2014; Zelinka et al., 2020).

Intercomparing model output is essential to characterize inter-model differences and to identify the uncertainty around projected values. Most model intercomparison studies still rely on the analysis of the spatial and temporal distribution of selected

30 model outputs presented as maps of mean values, their range, along with the computation of statistics (e.g. extremes, variability) (e.g., Wang et al., 2020; Flato, 2011; Jacob et al., 2007; Chen and Knutson, 2008). For intercomparisons targeting the historical period, observations or reanalyses are commonly used as references. Model performance is evaluated against real-world data or derived products and bias maps are used to locate model differences (e.g., Séférian et al., 2020; Yool et al., 2021; Chen and Knutson, 2008; Schaller et al., 2011). ~~Yet~~However, none of these methods characterises the interactions be-

35 tween ~~the~~ variables or quantifies their ~~inter-model differences . Hence,~~ differences between models. Two recent approaches try to address these limitations. First, the emergent constraint framework is increasingly applied to biogeochemical variables to reduce projection spread (Goris et al., 2023; Kwiatkowski et al., 2017; Fu et al., 2016). This approach identifies relationships between observable present-day variables and specific behaviours in future projections across models, helping to constrain uncertainties in climate predictions. Second, correlation-based approaches have been developed to ~~try to overcome these~~

40 ~~limitations~~ intercompare models and analyse the interactions between variables(e.g., Charakopoulos et al., 2018; Anagnostopoulos et al., 2010; Gleckler et al., 2008). However, ~~if correlation allows the identification of co-variation between variables or phenomena, it fails~~ while both these methods provide valuable insights, they fail to identify causal ~~relationships.~~ links between variables

To overcome the limitations of correlation-based ~~approaches~~methods, Krich et al. (2020) and Nowack et al. (2020) employed

45 a causality approach to analyse or evaluate model output. Here, we extend these earlier studies to the analysis and comparison of multi-model output~~by adopting a causality framework . This approach~~. The causality framework allows to describe model differences in a novel way, potentially revealing model-specific dynamics, quantifying the strength of interactions and its range across Earth System Models.

Our study focuses on the subpolar North Atlantic, a critical region for the global climate system with a well characterised

50 multi-year variability in physical and biogeochemical properties in response to the North Atlantic Oscillation, the dominant mode of regional climate variability (Yamamoto et al., 2020; Feucher et al., 2022; Keller et al., 2012; Tjiputra et al., 2012). At the seasonal time scale, deep winter mixing replenishes the sunlit surface ocean in nutrients and sustains an intense spring bloom. The subpolar North Atlantic is also a region undergoing rapid changes including freshening and cooling (Tesdal et al., 2018; Holliday et al., 2020), with potential impacts on large-scale circulation (Fox-Kemper et al., 2021; Hakkinen and Rhines,

55 2004). Along with these physical changes, an important variability in surface ocean nutrient levels has been documented (Johnson et al., 2013; Hátún et al., 2017) potentially foreshadowing future changes in primary productivity under climate change.

The impact of climate change on net primary production (NPP) in the North Atlantic region remains highly uncertain with a larger spread between model projections compared to other regions (Tagliabue et al., 2021; Fu et al., 2022). While vertical mixing is crucial for injecting nutrients to the productive surface ocean and fuelling primary production (D'Asaro, 2008; Williams et al., 2006), recent studies highlighted the contribution of horizontal transport to observed and projected variability of nutrients and primary production (Whitt and Jansen, 2020; Kwiatkowski et al., 2020; Hátún et al., 2017). The eastern part of the subpolar North Atlantic was proposed by Hátún et al. (2017) as a key area for the mixing of nutrient-poor subtropical waters into the subpolar North Atlantic gyre. The variability of the gyre circulation would be one mechanism controlling the advection and mixing of nutrients and ultimately NPP at regional scale. Moreover, ~~(Pelegrí et al., 1996; Williams et al., 2011)~~ Pelegrí et al. (1996) and Williams et al. (2011) highlight the contribution of subsurface nutrient-rich waters of subtropical origin (the nutrient streams) as a source of nutrients to the subpolar Atlantic through vertical mixing.

This study targets the eastern subpolar North Atlantic and seeks to differentiate between the variability of vertical mixing and horizontal advection of nutrients as controls of fluctuations of NPP. It draws on an ensemble of Earth System Model simulations to explore causal links from atmospheric processes to marine biogeochemistry. We rely on the "PCMCI+" method (Runge et al., 2019) for the analysis of causal interactions represented as causal graphs. In these graphs, nodes represent variables and edges indicate potential causal links with associated strengths. Our objective is twofold: (1) to propose a novel approach for model intercomparison, (2) to understand model-specific causal links between variability in atmospheric processes, advection and vertical mixing of nutrients to the surface ocean and NPP~~, as well as the consequences on inter-model spread~~.

This article is structured as follows: The ~~next~~ section 2 describes the causality discovery algorithm we use as well as the conceptual scheme that guides our study. Section 3 details the data used and the pre-processing steps applied to each variable. Section 4 presents the results obtained, highlighting specific key links and their similarities and differences between models. Section 5 discusses the limitations of the method employed, providing details on its strengths and weaknesses. Results are discussed in section 6 and section 7 concludes this article as well as proposing future perspectives.

2 Methodology

2.1 Causality approach: PCMCI+

To investigate the causal links ~~among~~ between the variables in our study, we use the PCMCI+ method (Runge et al., 2019; Runge, 2020). ~~PC stands for "Peter & Clark", the first step of PCMCI+ (Spirtes and Glymour, 1991), and MCI stands for "Momentary Conditional Independence", the other step of PCMCI+. This method~~ This approach is based on ~~Granger-Causality (Granger, 1969). Granger Causality~~ Granger Causality (Granger, 1969), which examines whether past values of variable ~~A enhances~~ A enhance the prediction of ~~B more than using B's own past values . In such a case, it is said that A Granger-causes B.~~ B beyond what B's previous values can predict by themselves. PCMCI+ ~~relies on Granger causality to create~~ generates a causal graph ~~by detecting contemporaneous or lagged relationships between the (physical or biogeochemical) variables , noted X^i from now on. These variables, within the PCMCI+ framework, become the nodes in the causal graph. The edges of the graph correspond to the~~ where physical and biogeochemical variables form the nodes, while edges represent contemporaneous

or lagged ~~links. A causal link between two nodes has a~~ relationships between these variables (A conceptual example of causal graph is given in Figure S1). Each causal link is characterized by a time lag (0 ~~if contemporaneous~~ for contemporaneous relationships) and a strength ranging from -1 to ~~1. The strength is the result of a correlation so if A causes B with a certain strength,~~ 1, with the sign indicating whether the ~~sign indicates if the~~ relationship is positive or negative, and the value ~~indicates~~ indicating the intensity of the ~~correlation. The graphs provided by PCMCI+ for the different climate models will be compared to the conceptual scheme discussed in Section 2.3 and intercompared to each other.~~

~~To investigate lagged interactions, we set a maximum lag value T. This means that all causal links established will have a lag within $[\![0,T]\!]$. To consider the lagged interactions, each variable X^i is considered T times. For each timestep $t \in [\![0,T]\!]$, a new set of variables X_t^i is obtained, by considering the variable X^i shifted by t timesteps. Then, for each X_0^i a first selection of possible candidate explanatory variables is done based on correlation tests. The variables in the selection are ranked in terms of decreasing correlation order. These explanatory variables able to "cause" X_0^i are called the parents of X_0^i.~~

~~Before explaining the PCMCI+ algorithm in details, it is important to remind the~~ relationship. To detect these causal relationships, the method relies on the concept of conditional independence~~of A and B given C (Dawid, 1979), defined by Equation (1). It describes the irrelevance of the event B to explain the event A when conditioned by C:~~. Two variables A and B are conditionally independent given a variable C if knowledge of B provides no additional information about A when C is already known. In other words:

$$A \perp\!\!\!\perp B|C \iff P(A|B,C) = P(A|C) \quad \text{with } A, B, C \text{ being events.} \tag{1}$$

~~The first step of PCMCI+, PC, consists in an iterative process where the conditional independence of two variables given a third one is tested (Spirtes and Glymour, 1991). More concretely, let X, Y and Z be three variables and $t_i, t_j \in [\![0,T]\!]$. We want to test if variable $X_{\tau=0}$ is still related to $Y_{\tau=t_i}$~~ In our analysis, this concept is applied through partial correlation tests which evaluate whether the relationship between two variables persists when the influence of ~~the most significant variable (according to the ranking previously made) to $X_{\tau=0}$ (e.g., $Z_{\tau=t_j}$)~~ one or more conditioning variables is removed. ~~This is achieved through Partial Correlation (noted $ParCorr$ in equation (??)), to test the conditional independence of $X_{\tau=0}$~~ The partial correlation is computed by first performing regressions of both variables on the conditioning set, then calculating the correlation between their residuals. The algorithm proceeds in two main steps: PC ("Peter and Clark") and ~~$Y_{\tau=t_i}$ given $Z_{\tau=t_j}$, by conducting a regression on each variable:~~

$$ParCorr(X_{\tau=0}, Y_{\tau=t_i}|Z_{\tau=t_j}) = Corr(\epsilon_{X_{\tau=0}|Z_{\tau=t_j}}, \epsilon_{Y_{\tau=t_i}|Z_{\tau=t_j}})$$

~~with~~

$$\begin{cases} X_{\tau=0} = \alpha_{X_{\tau=0}} * Z_{\tau=t_j} + \epsilon_{X_{\tau=0}|Z_{\tau=t_j}} \\ Y_{\tau=t_i} = \alpha_{Y_{\tau=t_i}} * Z_{\tau=t_j} + \epsilon_{Y_{\tau=t_i}|Z_{\tau=t_j}} \end{cases}$$

~~and $Corr()$ being the Pearson correlation . Applied to our field of interest, let's consider an example where we have nitrate (X) related to the gyre strength (Y) and Mixed Layer depth (Z~~ MCI ("Momentary Conditional Independence"). The ~~algorithm's~~

~~purpose is to determine if nitrate and the gyre strength remain correlated when the influence of mixed layer depth is removed. The first iteration of the PC steptests, for each variable, the conditional independence with all the possible parents (explanatory variables) given the most significant parent . The subsequent iterations of PC test the conditional independence of each parent according to~~ PC step first identifies potential relationships between variables through a series of conditional independence tests. The most significant relationships are then validated during the MCI step, which examines indirect influences between variables. For example, let's assume that NAO is identified as a parent (explanatory variable) of MLD and that transport and MLD are parents of nutrients. Then, when testing the link between nutrient and transport we will not condition by MLD but by NAO, the parent of MLD. For a detailed description of ~~the k most significant variables (according to a new ranking made at the end of the previous iteration). Regressions are made with k variables. False Discovery Rates (hereafter FDR, Benjamini and Hochberg, 199? are then used to find the equivalent of a p-value that will be the threshold to keep only the most significant links~~PCMCI+ method, we refer to Runge (2020). The variables of the conceptual scheme discussed in Section 2.3 will be given to PCMCI+ and the resulting causal graphs for different climate models will be compared to each other.

~~At the end of PC, each variable has a set of parents, corresponding to the possible explanatory variables. The concluding step MCI ("Momentary Conditional Independence") can then start, testing if the "grand-parents" influence the variable. For each variable, the conditioning variables are not taken among the parents but among the parents of the parents. Testing the grand-parents influence allows to investigate more deeply the causal relationships and to see if more distant variables have an influence~~It is important to note that the absence of a statistically significant causal link in our analysis should not be interpreted as definitive evidence for the absence of any relationship between variables. Rather, it indicates that any potential relationship is not strong enough to be significant through this analysis.

2.2 Quantification of causal graph: Dissimilarity measure

The output of PCMCI+ is a causal graph with a set of nodes (the variables given to PCMCI+) and potential edges (i.e., causal relationships) between those nodes. We can look at the PCMCI+ results via the adjacency matrix M representing the presence and strength of links between nodes. To compare the graphs (i.e., the relationships within models), it is then possible to compute dissimilarity metrics between adjacency matrices. However, many of these measures have limitations that make them inappropriate in our case. Firstly, the methods often assume edge's weight to be positive (e.g., Wicker et al., 2013; Koutra et al., 2013), which is not suitable in our case, as our edges can be positive or negative. The second problem is that the lag associated to the link also has to be taken into account. Even if different, when the lags are close, the distance should be small. In the other hand, once we exceed a certain difference in terms of lags, we can consider the link already too different that an even bigger difference in terms of lags will not give a bigger distance. To address these limitations, we propose an alternative approach that allows for negative weights and lags.

An Euclidean distance (as dissimilarity) allows us to deal with the weights of positive and negative edges noted w_{ij} where $i, j \in [\![0, N]\!]$. To account for the lags, we extend the matrices M from size $N \times N$ to size $N \times N \times T$ by adding a third dimension, indicating the lag at which the link occurs:

$$M[i,j,t] = \begin{cases} w_{ij}, & \text{if there is a link from } i \text{ to } j \text{ with a lag } t \\ 0, & \text{otherwise.} \end{cases}$$

Next, each vector $M[i,j]$ is blurred with a Gaussian filter convolution. The kernel K is a gaussian blur 3x1 ($\left[\frac{1}{4}, \frac{1}{2}, \frac{1}{4}\right]$). For the convolution operation, we use full padding, which extends the input vector by a total of 2 elements (size of kernel minus one), adding one element at each end. We note M' the matrix after the application of the Gaussian filter convolution. This approach helps to consider the lag difference by blurring the links in the third dimension, similar to how a blur would make two red squares on blank images share some red pixels if they are close enough. If we consider an example where $M[i,j] = [w_{ij}, 0, 0, 0]$ (i.e., a relationship from i to j only at $t = 0$), the transformed vector $M'[i,j]$ is thus given by:

$$M'[i,j] = M[i,j] * \left[\tfrac{1}{4}, \tfrac{1}{2}, \tfrac{1}{4}\right] = [w_{ij}, 0, 0, 0] * \left[\tfrac{1}{4}, \tfrac{1}{2}, \tfrac{1}{4}\right] = \left[\tfrac{w_{ij}}{4}, \tfrac{w_{ij}}{2}, \tfrac{w_{ij}}{4}, 0, 0, 0\right].$$

The Euclidean distance can then be applied to the blurred vectors/matrices, considering both the variations in lags and strengths. Our new dissimilarity measure DIS between two (blurred) adjacency matrices M_1 and M_2 can thus be written as:

$$DIS(M_1, M_2) = \sqrt{\sum_{(i,j,k)} (M'_1[i,j,k] - M'_2[i,j,k])^2}. \tag{2}$$

With this dissimilarity, we take into account how different the lags are for the same link while also taking into account the difference in intensity (strength of interaction). As an example, consider three causal graphs that are identical except for a single causal link with different time lags $k_1, k_2,$ and k_3, where $k_1 < k_2 < k_3$. The convolution ensures that the dissimilarity measure reflects the temporal proximity of these lags, such that $Dis(M_1, M_2) < Dis(M_1, M_3)$. However, when an expert considers that two time lags k_1 and k_2 are sufficiently distant from each other, they can adjust the convolution kernel size (set to 3 in our study) to reflect this assessment. Specifically, by choosing a kernel size smaller than the difference between k_2 and k_1, the dissimilarity between models M_1 and M_2 becomes maximal. In this case, the expert effectively indicates that the temporal distance between these lags is so significant that both M_2 and M_3 should be considered equally dissimilar from M_1, resulting in $Dis(M_1, M_2) = Dis(M_1, M_3)$. Here we selected a width of 3 years because we consider that lag differences beyond three years reach maximum dissimilarity. The width of the kernel is a user-defined parameter that can be changed for specific studies.

2.3 Conceptual scheme

We selected the Eastern subpolar North Atlantic (Figure 1) as a test case for this study focusing on the comparison of physical-chemical drivers of spring bloom dynamics in an ensemble of ESMs through a causality approach. The region is known for its large variability in contemporary nutrient concentrations (Johnson et al., 2013; Hátún et al., 2017). The latter has been linked to the strength of the subpolar gyre circulation through its control on the inflow of nutrient poor subtropical waters (Hátún et al., 2017). Fluctuations in gyre circulation, in turn, are driven by regional atmospheric forcing, leading to a causal chain from atmospheric processes to ocean dynamics and finally biogeochemistry.

This region is also prone to great sensitivity to climate change with a high spread of projected values of primary production. However, the mechanisms behind the projected impacts of climate change on NPP are not well understood(Kwiatkowski et al., 2019; Tagliabue et al., 2021). While vertical mixing is crucial for injecting nutrients to the productive surface layers and fueling NPP (e.g. deepening of the mixed layer during winter for nutrient supply and spring stratification for the initiation of the bloom), changes in subsurface nutrients brought by horizontal transport are also important and are likely to contribute to the between-model spread of projected NPP ~~. (Whitt and Jansen, 2020; Kwiatkowski et al., 2020) (Johnson et al., 2013)~~ ~~.~~ (Whitt and Jansen, 2020; Kwiatkowski et al., 2020; Johnson et al., 2013). Our conceptual scheme aims to highlight model-specific representations of the chain of causality running from atmospheric forcing to NPP. It attempts to disentangle the respective contributions of variability in vertical mixing and horizontal transport to modelled fluctuations of nutrient levels and NPP in the Eastern North Atlantic basin (Fig. 1).
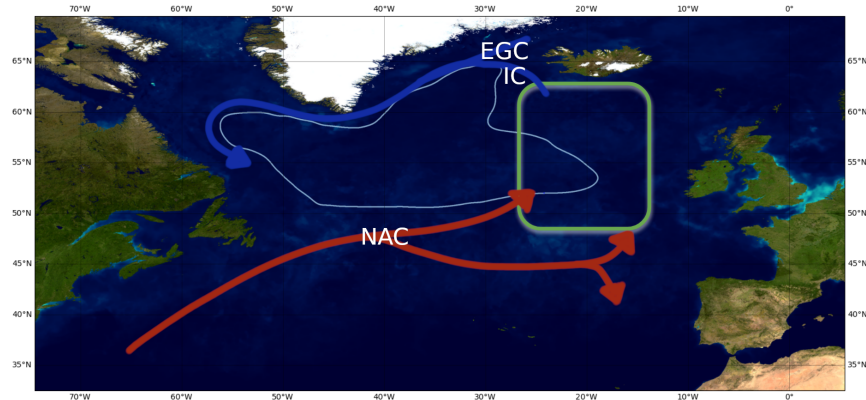
Figure 1. Study area "Eastern North Atlantic Subpolar Gyre" (green square). The main surface circulation patterns are indicated by the arrows (inspired by Daniault et al. (2016)). IC stands for Irminger Current, EGC for Eastern Greenland Current and NAC for North Atlantic Current. The gyre corresponds to the zone in light blue.

The anticipated chain of causality is represented as a conceptual scheme in Fig. 2. The target variable is the NPP of the spring bloom. Predictors of its variability include atmospheric and ocean physical processes, but also nutrient concentrations (nitrate, silicate and dissolved iron). Atmospheric processes are represented by the North Atlantic Oscillation (NAO), a prominent mode of regional climate variability and an important driver of variability of ocean physical and biogeochemical dynamics (Yamamoto et al., 2020; Feucher et al., 2022; Keller et al., 2012; Oschlies, 2001; Herceg-Bulić and Kucharski, 2014; Delworth and Zeng, 2016). Physical processes included are vertical and horizontal transports. Winter-time deepening of the mixed layer injects nutrients to the surface ocean, replenishing the pre-bloom surface nutrient stock.(Williams et al., 2006). Stratification during spring and the shoaling of the mixed layer contribute to initiate the spring bloom. Mixed Layer Depth (MLD) and stratification are thus chosen as predictors of vertical transport. For the advection of nutrients we will focus on the net transport into the area of study, as well as consider the strength of the North Atlantic subpolar gyre. Lastly, ~~three~~ four nutrients are considered: nitrate, phosphate, silicate and dissolved iron.
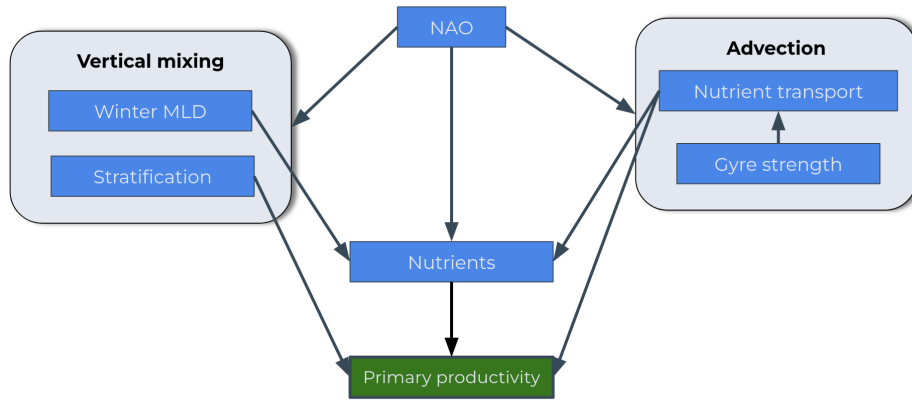
Figure 2. Suggested conceptual scheme. The target variable is in green, the explanatory variables are in blue.

We anticipate numerous interconnections across the scheme. The NAO is known to exert influence over multiple processes in the North Atlantic affecting physical variables such as gyre strength, water transport and MLD (Yamamoto et al., 2020; Feucher et al., 2022), but also nutrient concentrations. Diving into the oceanic variables, the gyre strength, relevant for physical variables such as MLD (Swingedouw et al., 2021), could as well be explanatory for nutrient concentrations (Hátún et al., 2017; Johnson et al., 2013) through its impact on nutrient transport. For the vertical mixing component of the scheme, a link from MLD to nutrient concentrations is anticipated, because winter MLD deepening is crucial for replenishing the nutrient stock (Williams et al., 2006). We also expect a relationship between stratification and NPP because high stratification during the productive period will inhibit the upward mixing of nutrients and thus NPP (Lozier et al., 2011; Tagliabue et al., 2021). The scheme will be explored for each nutrient (nitrate, dissolved iron and silicate) and we anticipate differences in the intensity of the relationships for each nutrient, especially for the relationship between nutrient and productivity.

3 Experimental setup

3.1 Selection of Earth System Models and simulations

We selected a set of Earth system models with biogeochemical models of similar complexity to explore the variability of causal links connecting atmospheric processes to NPP. These biogeochemical models include ~~4 plankton~~ at least 2 phytoplankton functional types (PFT) ~~(2 phyto- and 2 zoo-plankton groups)~~ with model-specific parameterisations of interactions between PFTs, as ~~wall~~ well as nutrient limitation of phytoplankton growth. We made sure not to repeat the coupling of ocean and biogeochemical models twice. This led to the selection of ~~5~~ 6 Earth System Models presented in table 1. There is nevertheless some redundancy in our selection with 4 ESMs sharing the same ocean model (3 with the same version). Additional information on the biogeochemical models is available in the supplementary.

Table 1. Models used in the study.

ESM model	Oceanic model	Oceanic grid	Atmospheric model	Atmospheric grid	Biogeochemical model	ESM reference
IPSL-CM6A-LR	NEMO-OPA 3.6	1° x 1° with 75 levels	LMDZ	1.3° x 2.5° with 79 levels	PISCES-v2	Boucher et al. (2020)
CESM2	POP2	1°x1.125° with 60 levels	CAM6	0.9°x 1.25° with 32 levels	MARBL	Danabasoglu et al. (2020)
CMCC-ESM2	NEMO-OPA 3.6	1° x 1° with 50 levels	CAM5.3	0.9° × 1.25° with 30 levels	BFM5.1	Lovato et al. (2022)
CanESM5-CanOE	CanNEMO 3.4.1	1° x 1° with 45 levels	CanAM5	isotropic triangular 2.8° grid with 49 level	CanOE	Swart et al. (2019); Christian et al. (2021)
UKESM1-0-LL	NEMO-OPA 3.6	1° x 1° with 75 levels	MetUM-HadGEM3-GA7.1	1.25° x 1.88° gridpoints with 85 levels	~~MEDUSA2~~ MEDUSA-2.0	Sellar et al. (2019); Yool et al. (2021)
MIROC-ES2L	COCO	1° x 0.7° with 62 levels	CCSR-NIES	T42 spectral truncation (2.8°) with 40 levels	OECO2	Hajima et al. (2020)

We selected pre-industrial control simulations (piControl) from the 6th Coupled Model Intercomparison Project (CMIP6)
225 (Eyring et al., 2016). These simulations were run for 500 years with constant natural external forcings (e.g. volcanoes, solar radiation, greenhouse gases) fixed at pre-industrial level. It allows access to an ~~extented~~ extended period for assessing model specificites through causal graphs. Due to the absence of variability and trend in external forcings, climate variability is restricted to its unforced internal component. ~~Interactions between variables should not evolve during the 500 years of simulation~~ The primary mechanisms driving interactions between spring productivity and its controlling factors are expected to maintain
230 consistent relationships over the 500-year simulation period, though their relative strength may show some temporal variations.

3.2 Definition and preprocessing of variables for PCMCI+

We compute time series of annual means from monthly output fields for each model variable. From these time series variables for PCMCI+ are computed as described below. Each processed variable is ~~normalized~~ centered (mean at 0) and reduced (standard deviation at 1) prior to running PCMCI+. Variables selected for PCMCI+ and their definition are presented in table
235 2. The following paragraphs add details to the preprocessing. With the exception of transport of nutrients and the subpolar gyre index which are computed on the original model grid, all other variables are interpolated on a regular 1°x1° grid prior to preprocessing.

Table 2. Variables and their formulation. The variables used in PCMCI+ are in bold.

Full name	Abbreviation	Formulation	Period	Grid
Net Primary Productivity	**intpp**	$Max(\int_{depth} pp)$	Peak of the bloom	Regular Grid
Nutrients	**no3, dfe, si**	$Max([nutrients]_{0m-100m})$	Peak reached before the bloom	Regular Grid
Mixed Layer Depth	**mlotstmax**	$Max(mlotst)$	Peak reached before the bloom	Regular Grid
North Atlantic Oscillation	**NAO**	$slp_\alpha - slp_\beta$	From the start of the bloom to the peak of the bloom	Regular Grid
Sea Level Pressure of the high pressure zone	slp_α	$\alpha = \{(i,j) \mid \mid\{t \mid slp(i,j,t) > P_{90}(t)\}\mid > 0.9*T\}$ with (i,j) indicating a grid point, and $P_{90}(t)$ the 90th percentile of slp at time t, and T the number of timesteps		Regular Grid
Sea Level Pressure of the low pressure zone	slp_β	$\beta = \{(i,j) \mid \mid\{t \mid slp(i,j,t) < P_{10}(t)\}\mid > 0.9*T\}$ with (i,j) indicating a grid point, and $P_{10}(t)$ the 10th percentile of slp at time t, and T the number of timesteps		Regular Grid
Strength of the gyre	**Gyre**	$Mean(\psi_{7.5})$ where $\psi_{7.5} = \{\psi > 7.5\ Sverdrup\}$ with ψ the barotropic streamfunction	From the start of the bloom to the peak of the bloom	Original Grid
Barotropic Streamfunction	ψ	$\int_{West}^{East} \int_{-2000m}^{0m} v dx dz$ with v the meridional component of the velocity		Original Grid
Stratification	**Strati**	$\rho_{100} - \rho_0$ with ρ_z the density at depth z	From the start of the bloom to the peak of the bloom	Regular Grid
Transport	**Trsp**	$\sum_{(i,j)\in B} Max(\int_{MLD}^{0m} vel[nutrient]dz, 0)$ with B the group of bordering points of the study area and vel the velocity, meridional or zonal component according to the orientation of the border)	From the start of the bloom to the peak of the bloom	Original Grid

3.2.1 Bloom and productivity

We focus on the variability of maximum of NPP reached during the year. This corresponds to the maximum reached during the spring months, the spring bloom. For several other variables (e.g. atmospheric forcing, nutrient transport, gyre circulation) it is important to time the start of the bloom as their variability during the bloom might impact bloom dynamics. Following the threshold method in ~~(Brody et al., 2013)~~ Brody et al. (2013) we consider the bloom has started once a certain threshold has been exceeded. This threshold value corresponds to the median NPP plus 5%. The starting date for the bloom is the first month m verifying Eq. (3):

$$intpp(m) > 1.05 \times median(intpp). \tag{3}$$

3.2.2 Nutrients

The study focuses on nitrate, phosphate, silicate, and dissolved iron before the beginning of the bloom to qualify the biogeochemical context of the spring bloom. Specifically, we will consider the average concentration in the upper 100 meters of the water column. When the bloom starts, nutrient concentrations of the pre-bloom period begin to decline. The timing of the spring bloom varies across different regions and models, as does the timing of the maximum nutrient concentration. Therefore, we will define our annual signal as the peak (i.e., maximum) concentration reached during the winter-spring season. This approach will allow us to capture the yearly variability in nutrient concentrations associated with the intensity of the spring bloom.

3.2.3 North Atlantic Oscillation

The NAO (North Atlantic Oscillation) index quantifies the difference between the high and low-pressure zones in the North Atlantic region. However, the location of the high and low-pressure centers varies among different climate models, making it necessary to use a model-independent method for its computation. Historically the NAO was computed as the difference of Sea Level Pressure (slp) between two specific stations (Lisbon, Portugal and Stykkisholmur, Iceland) (Hurrell et al., 2003). Nowadays, the use of EOF over a large geographic area has become common (Hurrell et al., 2003; Hurrell and Deser, 2010). We preferred using the method consisting in computing the difference of slp on two selected zones (Hurrell, 1995; Hurrell et al., 2003) but the selection of the zone needs to be model independent.

Our proposed solution to select the zones here uses a counting approach. At each time step, the points belonging to the higher and lower 10_{th} percentiles of sea level pressure are identified. For each of these points, the counting index for the high and low pressure is incremented accordingly. As a result, each point is associated with two numbers α and β indicating how many times it belonged to the high (α) or low-pressure zone (β). To compute the NAO index, we consider 10_{th} percentile for respectively α and β as the high and low-pressure areas to compute the sea level pressure difference. In the end, we consider the zones that were most of the time high or low pressure as the high and low pressure poles. We display the poles selected for each model in the supplementary material Figure ~~S1~~S3. The selected period for computing the index was from the start to the

peak of the bloom. Choosing this period ensures coherence with the other variables considered during this period (e.g. gyre circulation, nutrient transport)

3.2.4 Gyre index

The gyre circulation is characterized by the gyre index which is computed on the months between the start and the peak of the bloom as it is linked to the NAO (Hurrell and Deser, 2010; Koul et al., 2020). The stream function is computed over 2000 m depth on the original grid and integrated from east to west. Once obtained, a threshold of 7.5 Sverdrup is applied on each grid point as in Biri and Klein (2019). From this method we extract the strength i.e the mean of the stream function at the selected point). The shape of each model gyre and its geographical variability is displayed in the supplementary material in Figure S2.

3.2.5 Vertical mixing

The MLD depth in winter will determine the stock of nutrients available (Williams et al., 2006) for the spring bloom. Here we want to capture the variability of MLD intensity. Therefore, we focus on the maximum depth reached between November and April. The impact of stratification on NPP is an important aspect of our study, and we will quantify this relationship using the difference in density as an indicator (Lozier et al., 2011; Van De Poll et al., 2013). We focus on the difference of density between 100m and the surface $\rho_{100} - \rho_0$. To assess the impact of stratification on productivity, we will calculate the mean value of $\rho_{100} - \rho_0$ from the beginning to the peak of the bloom. This approach will allow us to examine the relationship between stratification and NPP during the most active period of phytoplankton growth.

3.2.6 Nutrient transport

The inflow of nutrients via horizontal advection is also an important factor to consider for the nutrient concentration at the start of the bloom and the resulting NPP. We integrate the transport of nutrients from the ocean surface to the mixed layer depth (MLD) for each model. For each depth level and each month considered (between the ~~beggining~~ beginning of the bloom and the peak of the bloom), the nutrient concentration is multiplied by the transport. The transport is computed from the meridional and zonal velocity variable. For our analysis, we will focus only on the inflow of nutrients into our study region. As for the period selected for the signal we will take the transport of nutrients from the beginning of the bloom to the peak of the bloom.

4 Results

We obtain one distinct causal graph for each nutrient : nitrate, dissolved iron and silicate. With the exception of CanESM5-CanOE for which silicate was not available, all 3 nutrients are considered for the remaining models. Causal links differ slightly between nutrients. For example, for a given link between two variables, the nutrient may not be directly involved but indirectly influence the relationships through changes in conditioning variables, resulting in slight variations in the calculated strength. Nutrients are identified in the following by adding "_no3" (nitrate), "_dfe" (dissolved iron) or "_si" (silicate).

4.1 Similar models

The similarity between models is evaluated based on the dissimilarity introduced earlier. Looking at the dissimilarity of the entire causal graph could mask important local differences. Focusing on sub-matrices provides insight into differences between models with respect to specific ~~causal~~ relationships. For instance, ~~computing the dissimilarity on the sub-matrix corresponding to the drivers of one variable allows to explore specific dynamics shared by two models(similar impacts, similar lags)~~when analyzing dynamics around a specific variable (the ith one), we can extract its corresponding column (the ith column) from the complete PCMCI+ matrix. This column represents all causal influences from the ith variable on the other variables in the system. By applying our dissimilarity measure to these extracted columns from different models, we can systematically compare how various models represent the causal influences linked to this specific variable. Figure 3 represents the dissimilarity between models for links with dfe. UKESM1-0-LL has the largest dissimilarity with other models. These high values of dissimilarity have two possible explanations (interactions between nutrients and lagged links) which will be discussed in section 4.2.
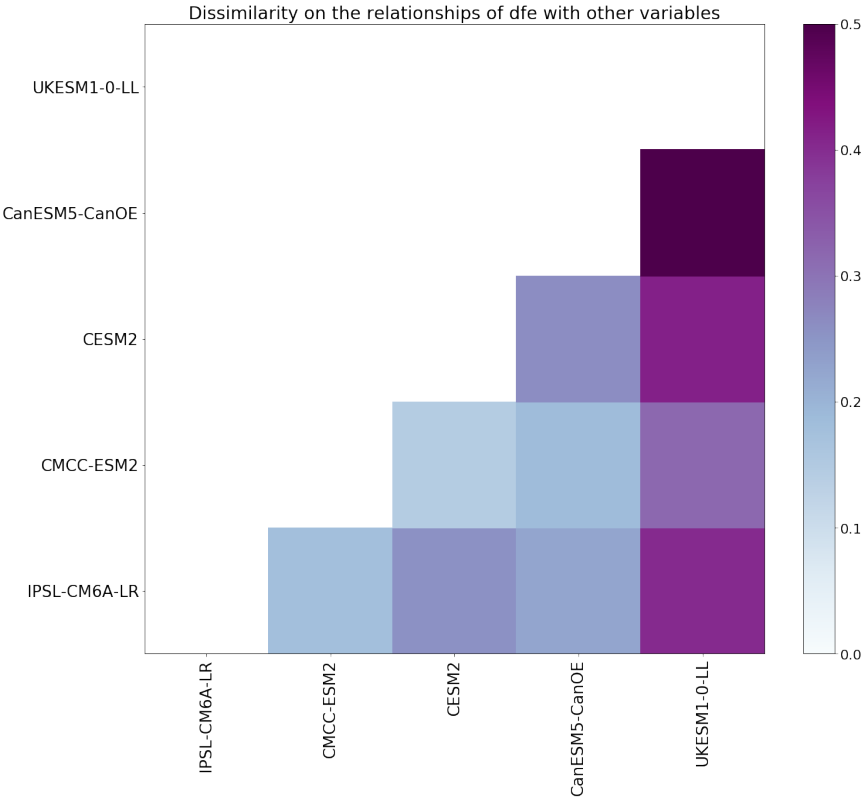
Figure 3. Dissimilarity between each model for iron links only. The darker the colour the more different the models.

310 To further quantify the similarity or dissimilarity between models and to identify the corresponding variables, we count how many times two models are the closest to each other or the most different. The results are synthesised in Figure 4 for IPSL-CM6A-LR with the most ~~and least~~ similar links displayed ~~on 4(a) and the most different on 4(b)~~ in Fig.4. The results for the other models are given as supplementary material from Figure ~~S2 to S5~~S4 to S8. From Figure 4, it appears that CMCC-ESM2 is the closest model, particularly for impacts from NAO, gyre, and transport. It has to be noted that the converse is not

315 necessarily true. To understand this, ~~we can look at~~ let's consider the most different model on the right of Figure 4. CESM2 is the most different model from ~~IPSL~~ IPSL-CM6A-LR with differences located mainly on Gyre and Transport but UKESM1-0-LL also appears to be rather different from IPSL-CM6A-LR. UKESM1-0-LL is also the most different model for all the other models (Figure ~~S1-S4~~S3-S6). However, UKESM1-0-LL obviously also has a most similar model, which is CMCC-ESM2, but this similarity is not reciprocal, as UKESM1-0-LL seems to have the most distinct behaviour. CanESM5-CanOE frequently

320 appears as the most different model from UKESM1-0-LL concerning nutrients, gyre, NAO, and stratification. Therefore, these two models are the most dissimilar. Grouping models according to their similarity or dissimilarity raises the question of which specific links differ between the models and for which links the models agree. To answer this question, specific ~~key links are analysed next starting with contemporaneous links~~ contemporaneous links are analyzed next (at lag 0).

4.2 Control of nutrients

325 In the following subsections, we focus exclusively on contemporaneous lags (lag-0 relationships). While lagged relationships were also identified in our analysis, they were less abundant and much weaker and therefore not robust enough to be considered.

On Figure 5, we have selected a subset of links that directly control pre-bloom nutrient concentrations. The first panel shows the model agreement for the control of MLD on nitrate and silicate (highlighted in green). As expected, the maximum winter

330 MLD has a strong impact on pre-bloom nutrient concentrations with a consensus between models (mean strength of link: ~~0.61 for silicate~~0.60 for silicate, 0.67 for nitrate and ~~0.65 for nitrate~~ 0.60 for phosphate). This agreement brings coherence among models, although links for nitrate and phosphate (standard deviation of ~~0.15) are slightly~~ respectively 0.13 and 0.17) are more scattered compared to silicate (standard deviation of ~~0.08~~0.04). Regarding iron concentration, UKESM1-0-LL stands out with a non-significant link from MLD to iron concentration. For the other models the strength of the link is of the same order of

335 magnitude as for nitrate and phosphate. This reflects the variability in underlying parameterisations of iron biogeochemistry across Earth System Models (Tagliabue et al., 2016). The median strength is about the same for the ~~three~~ four nutrients.

The models also agree in the lack of direct impact of NAO on nutrient concentrations. However, it is possible that the NAO indirectly affects nutrient concentrations by impacting a physical variable which in turn influences nutrient concentrations. As discussed in ~~(Patara et al., 2011)~~Patara et al. (2011), this intermediary variable could be the advection of nutrients, which

340 is considered here via the transport of nutrients. The intermediary variable could also be the MLD, partially driven by the NAO (Yamamoto et al., 2020), also considered in our scheme. These indirect links will be discussed in Section 4.4. Lastly, the influence of nutrient transport on pre-bloom nutrient concentrations is scattered. Models CMCC-ESM2 and IPSL-CM6A-LR agree on a positive impact for nitrate~~and silicate , (CMCC-ESM2: 0.18, IPSL-CM6A-LR:0.27 for nitrate and~~, silicate and
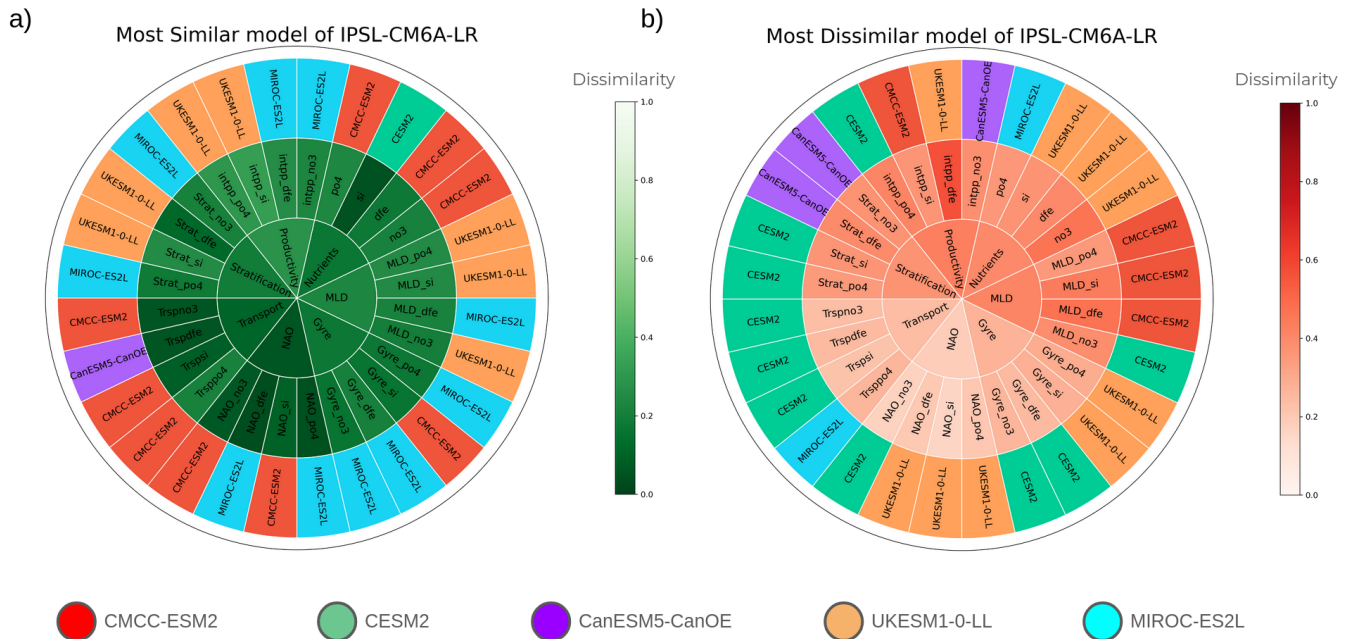
Figure 4. Most similar (a) and ~~most different~~ dissimilar (b) models compared to ~~/from~~ IPSL-CM6A-LR ~~according to~~ based on the dissimilarity ~~introduced~~ metric in Eq. 2. The ~~interior~~ inner circle ~~is~~ indicates the variable~~studied. Each variable is presented for each nutrient in~~, the middle circle shows each variable's variant depending on which nutrient is considered("_no3" for nitrate,"_dfe" for dissolved iron, "_si" for silicate and "_po4" for phosphate). The ~~exterior~~ outer circle indicates ~~which model is~~ the ~~closest/~~most ~~different for this specific variable~~similar or dissimilar model. The color scale in the inner and middle circles represents the dissimilarity intensity, while the outer circle's color identifies the most similar or dissimilar model

phosphate, (respectively: for CMCC-ESM2:~~0.3~~0.19, 0.3 and 0.19, for IPSL-CM6A-LR:0.28, 0.19 ~~for silicate~~and 0.47) but
345 neither shows a significant impact on iron. CESM2 also shows a positive impact on silicate (~~0.24) and~~0.23) and phosphate (0.22) and is the only one to have a moderate impact on iron (0.28). The only other model having an impact on iron ~~(0.27).~~ is MIROC-ES2L with a low intensity (0.15). Concerning this model, nitrate is also affected by transport but also with a low intensity (0.16). CanESM5-CanOE shares some of the behaviour of CMCC-ESM2 and IPSL-CM6A-LR, with a positive impact for nitrate (0.36~~, the strongest link for transport~~) and no impact for iron. UKESM1-0-LL is the only one to have no influence
350 from advection ~~for any nutrient~~except for phosphate (0.24). In CESM2, nitrate is not influenced by advection but is strongly influenced by MLD. In contrast, for ~~iron and silicate~~other nutrients, MLD has a less strong influence, and a positive impact from transport is observed. This suggests that for nitrate, the strong influence of MLD leaves no opportunity for advection to affect nutrient variability.
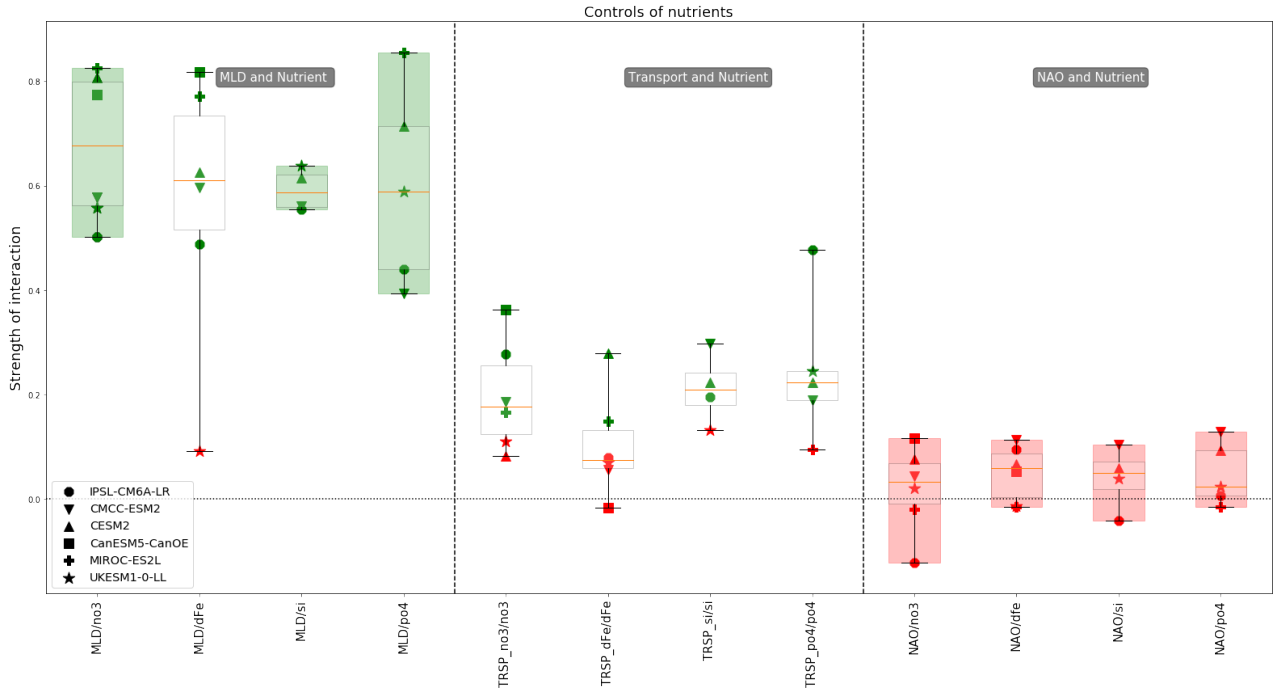
Figure 5. Controls of pre-bloom nutrients concentrations: Strength of links for each model with median and quartile values (boxplot). Each ~~model is represented with~~ marker represents a different ~~marker and~~ model, with the marker color ~~of~~ indicating the ~~marker shows the~~ statistical significance of the causal link ~~according to~~ as determined by PCMCI+ (green for significant ~~and~~ links, $p < \alpha$; red for ~~not significant~~ non-significant links, $p > \alpha$). ~~Boxplots~~ We define model agreement in two ways: when all models consistently identify a link as significant (boxplot highlighted in green), or when all models consistently identify a link as non-significant (boxplot highlighted in red)~~indicate model agreement (disagreement)~~.

A general conclusion of those results is the major importance of vertical mixing for nutrients. While there is a consensus on the importance of MLD for nitrate~~and silicate~~, silicate and phosphate concentrations, inter-model differences still exist, particularly for iron cycling and nutrient transport.

4.3 Productivity drivers

On Figure 6 we isolated a subset of links between variables known to control NPP and the peak intensity of the spring bloom. The left panel reveals two consistent links among the models: nitrate and NPP, silicate and NPP. However, while the models agree on the significance of these interactions, they disagree on their strength, with a wide range of values (nitrate: mean of ~~0.39~~ 0.4 and standard deviation of ~~0.23~~ 0.21; silicate: mean of 0.37 and standard deviation of 0.23). We also observe that for phosphate and NPP models are also close to a consensus with a mean at 0.42 and a standard deviation of 0.19. The UKESM1-0-LL model exhibits the strongest links for ~~both nitrate (~~ three nutrients (nitrate : 0.79~~) and silicate(~~, silicate: 0.72 and phosphate: 0.72), while the CESM2 and IPSL-CM6A-LR models show the weakest, with all values ~~below 0.19 for both~~ around 0.16 for
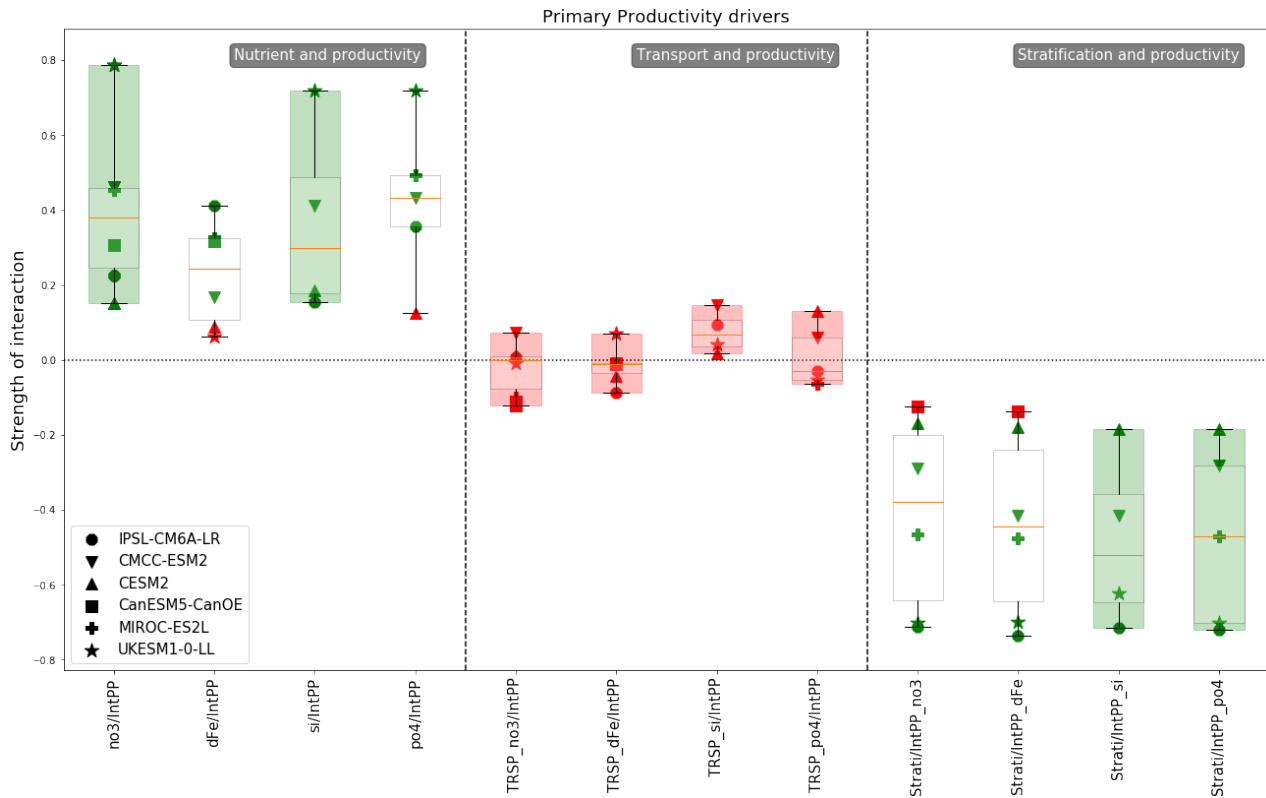
Figure 6. Same as 5 but for controls of net primary productivity.

the same three nutrients. The variability of nitrate~~and silicate~~, silicate and phosphate concentrations before the bloom has a variable impact on NPP across the selected models. For iron the range of interaction strengths is narrower, with both the CESM2 and UKESM1-0-LL models showing non-significant results. The maximum strength value is 0.41, observed for IPSL-CM6A-LR model. Notably, the impact of iron variability on NPP in the IPSL-CM6A-LR model is twice as strong as that of silicate or nitrate. Conversely, the CMCC-ESM2 and UKESM1-0-LL models show the opposite trend. For ~~CMCC-ESM2~~the other models, the strength ~~decreases from approximately 0.44 for both nitrate and silicate to~~ of this link is lower for iron. The strength slightly decreases for MIROC-ES2L going from approximately 0.46 for nitrate and phosphate to 0.35 for iron. For CMCC-ESM2, the strength decreases from approximately 0.44 for the three other nutrients to 0.17 for iron. The difference is even more pronounced in the UKESM1-0-LL model, which exhibits the strongest links for nitrate and silicate, but a non-significant one for iron. In the CESM2 model the strength of those links remains fairly stable, with low strength values for both nitrate and silicate ~~and an iron~~ as well as an iron and phosphate residual value (the last partial correlation value obtained which did not pass the significativity test) that is close to these.

The last panel of Figure 6 presents the relationship between stratification during the productive period (from the start to the peak of the bloom) and NPP. With the exception of CanESM5-CanOE, which shows a non-significant link, the impact

of stratification is negative across all models, as anticipated. However, the range of interaction strengths is quite broad. The UKESM1-0-LL and IPSL-CM6A-LR models exhibit strong negative links (approximately -0.7), while CESM2 shows a weak strength of around -0.2, and CMCC-ESM2 ~~has a moderate strength~~ and MIROC-ES2L have moderate strengths of approximately -0.3 and -0.45. This marked difference in dynamics among the models suggests that they may respond differently to projected climate conditions, as stratification is known to be increasing under global warming (Li et al., 2020). Specifically, if stratification continues to increase and assuming that the relationship will remain unchanged in the future, the intensity of the bloom in the eastern part of the subpolar gyre may decrease more significantly in the UKESM1-0-LL and IPSL-CM6A-LR models ~~compared to the others.~~

Lastly, the middle panel of Figure 6 indicates that nutrient transport does not have a significant direct impact on NPP in any of the models. However, as discussed in the previous subsection, transport plays a role in determining pre-bloom nutrient concentrations for some models (Figure 5). These nutrient concentrations, in turn, significantly affect NPP, as shown in the first panel of Figure 6. Therefore, transport has an indirect impact on NPP via nutrient concentrations. However, this impact is relatively low, as the influence of transport on nutrient concentrations is moderate, and the effect of nutrient concentrations on NPP can also be moderate or strong depending on the model. As a result, two consecutive moderate impacts lead to a rather low overall impact. For instance, if the variability of transport explains 30% of the variability of nutrient concentrations and the latter explains 30% of NPP variability, then transport explains 9% of NPP variability.

4.4 Physical interactions

Figure 7 presents a subset of physical interactions included in our conceptual scheme. Other interactions are displayed in the supplementary Figure S7. The focus of Figure 7 is on the atmospheric impact on the ocean component, specifically the impact of the North Atlantic Oscillation (NAO) on transport, gyre strength, and stratification. For the CMCC-ESM2 model a significant impact of NAO was found for most variables, except for silicate and phosphate transport, which has a residual of around ~~0.14~~ -0.14 and +0.12. The same holds for CESM2 which only misses an impact on nitrate transport with a residual around 0.03. Comparing only these two models, the strength of relationship between NAO and gyre strength is similar (around ~~-0.2~~ 0.2), but the impact on transport is slightly stronger for CESM2 (~~around 0.3~~ (phosphate at approximately +0.24, while silicate and iron at -0.31 for CESM2 and around ~~0.2~~ -0.2 concerning nitrate and iron for CMCC-ESM2). CESM2 also has a stronger effect of NAO on stratification (around ~~-0.3~~ 0.3 for CESM2 and around ~~-0.2~~ 0.2 for CMCC-ESM2), making it the model with the strongest overall impact from NAO on its oceanic variables.

For the other models many model-specific links were identified, suggesting inter-model differences in dynamics. Starting with UKESM1-0-LL, NAO has a significant impact on the gyre strength (~~-0.33~~ 0.33) but none on the stratification in our zone. The lack of a significant link between NAO and stratification sets this model apart. It does not result from the approach taken to compute NAO as there are no major differences in the placement of high and low-pressure zones between UKESM1-0-LL and the other models. The UKESM1-0-LL model also shows significant links from NAO on iron and silicate transport (with a strength around 0.24 slightly bigger for silicate), but not on nitrate transport (residual around -0.12). The IPSL-CM6A-LR
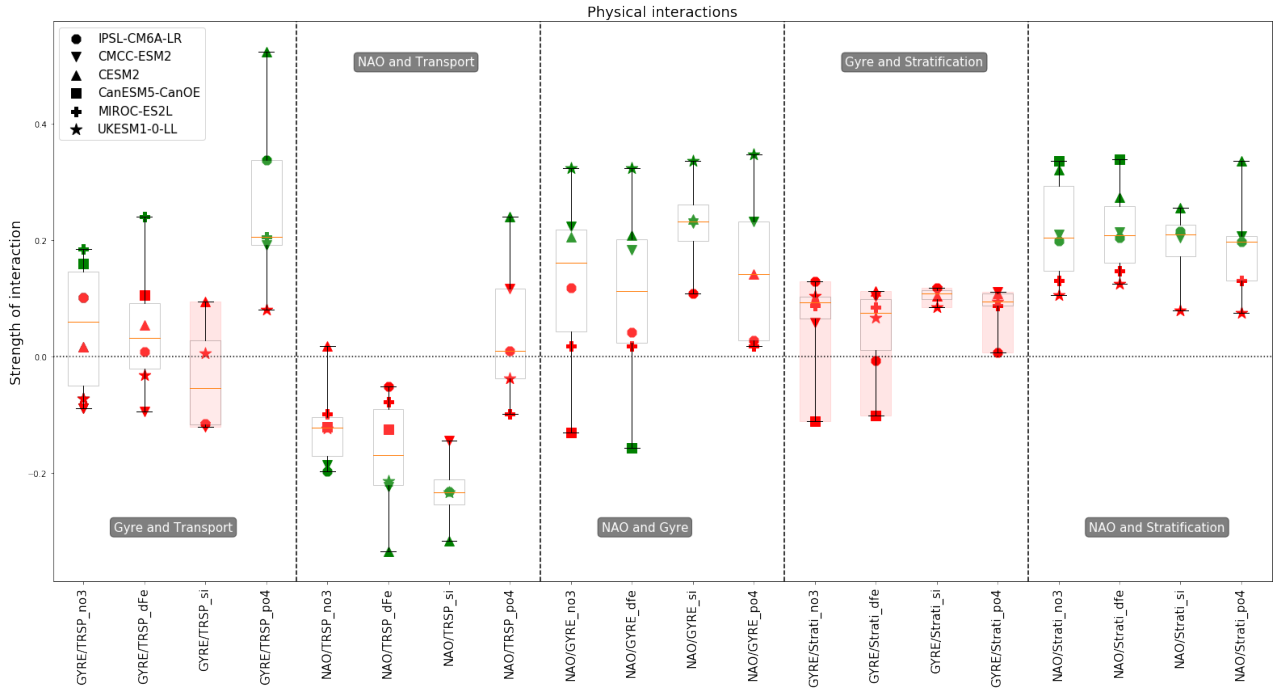
Figure 7. Same as Figure 5 but for selected physical interactions. Other physical interactions are displayed in Supplementary Figure S7

model is the only one with a non-significant impact on gyre strength. However, the NAO significantly impacts stratification (with a strength of about -0.2) and the transport of nitrate and silicate (around -0.22, slightly bigger for silicate).

Lastly the CanESM5-CanOE model, it is the only one with a negative impact of NAO on the gyre opposed to a positive one

415 observed in the other models (or at least a positive residual when not significant). However, we see on the third panel Figure 7 that on the first boxplot it is not significant and on the second one it is. This relationship is on the verge of significance (with a strength of -0.14 when significant). This suggests a potential unique behaviour in this model with respect to the relationship between the NAO and gyre strength. The CanESM5-CanOE model also exhibits one of the strongest impacts on stratification (with a strength of about -0.33). Lastly, the transport of nutrients is not significantly impacted by the NAO.

420 In the previous ~~analysis~~results, we identified for all models, except UKESM1-0-LL, the transport of at least one nutrient impacting the variability of nutrient concentrations. Therefore, it is possible for NAO to indirectly influence nutrient concentrations through its impact on transport. This indirect link between NAO and nutrient concentrations is present in IPSL-CM6A-LR, CESM2~~and~~, CMCC-ESM2 and MIROC-ES2L. In the case of IPSL-CM6A-LR and MIROC-ES2L nitrate and silicate transport significantly impact their respective nutrient concentrations. Likewise, for the CESM2 model, iron and silicate trans-

425 port significantly affect their corresponding nutrient levels. The CMCC-ESM2 model also exhibits this indirect link through nitrate transport, but not for iron transport, as NAO does not impact it. In all these cases the transport variability is partly

driven by the NAO. In summary, the indirect link between NAO and nutrient pre-bloom concentration through transport is model-dependent.

Considering the interaction between gyre strength and ~~nutrient transport and the interaction between gyre strength and~~ stratification, we observe that the models agree on the non-significance of these interactions. However, ~~there is an exception for the link between gyre strength and nitrate transport, where the interaction is significant with a strength of 0.16 for CanESM5-CanOE only~~ with the notable exception of silicate, the gyre strength impacts nutrient transport. MIROC-ES2L has a significant link of about 0.2 for nitrate, iron and phosphate. The other models only have a link for nitrate or phosphate and none is found for UKESM1-0-LL. Some models have an indirect influence of gyre strength on nutrient concentration. For example, the interaction between gyre strength and phosphate transport is strong for CESM2 (0.52). In this model, ~~nitrate~~ phosphate transport significantly impacts pre-bloom ~~nitrate~~ phosphate concentration with a strength of ~~0.36~~ 0.22. Thus, there is an indirect influence of gyre strength on nutrient concentration via nitrate transport. We also observe a marked difference for the dynamics of phosphate transport compared to other nutrients. For three models (IPSL-CM6A-LR, CMCC-ESM2 and CESM2), a significant link is found for phosphate transport without any significant link for other nutrients.

5 PCMCI+ Limitations

Like for many other algorithms, it is crucial to carefully select variables given to PCMCI+, as the selection will significantly affect results. It is important to note that PCMCI+ is not intended to be used as a data mining tool, as stated by Runge et al. (2019). While it is necessary to include all variables containing relevant information, a too high number will decrease the performance of the algorithm. To evaluate the decrease in performance as a function of the number of variables and the time lag, two criteria are commonly used: "precision" and "recall":

- The precision represents the ratio of True Positives among all the positives found by the algorithm (True Positives + False Positives): $precision = \#true\ pos./(\#true\ pos. + \#false\ pos.)$.

- The recall corresponds to the ratio of True Positives among all the positives that the algorithm should have found (True Positives + False Negatives): $recall = \#true\ pos./(\#true\ pos. + \#false\ neg.)$.

To quantify the recall and precision performances of PCMCI+, we applied it to artificially generated random auto-regressive vectors. Auto-regressive vectors are time series built so that they depend on past values of themselves. A set of N vectors $(X_i)_{1 \leq i \leq N}$ is defined according to:

$$X_i(t) = \sum_{0 \leq \tau \leq \tau_{max}} \sum_{1 \leq j \leq N} \alpha_{i,j,\tau} X_j(t - \tau) \tag{4}$$

with $\alpha_{i,j,\tau}$ being randomly chosen dependence coefficient and τ_{max} the maximum lag value. Each non null random dependence between the variables has been constrained to have a value of at least 0.2. To be close to the configuration of this study, vectors are generated on 500 time steps. ~~These~~ The non-null values of αi,j in these auto-regressive vectors ~~are now taken as the~~ serve
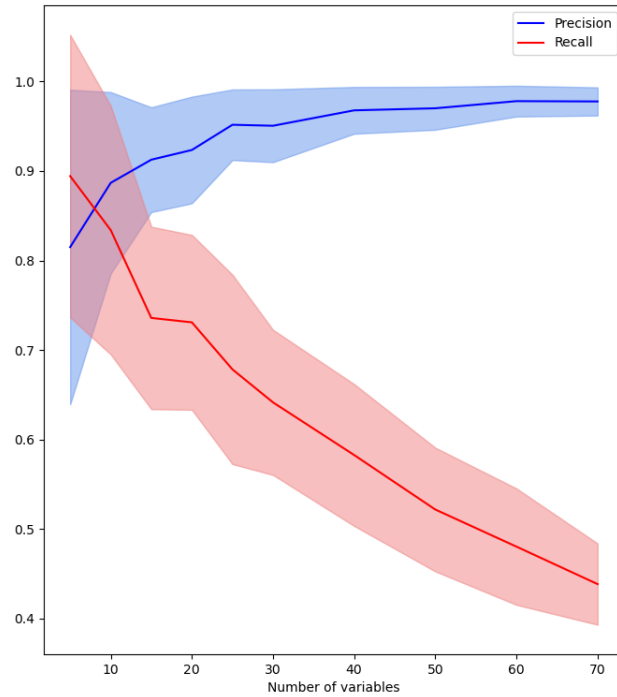
Figure 8. Precision (blue) and recall (red) according to the number of variables with a max time lag fixed at 5.

as our "ground truth" ~~and thus allow~~, allowing us to evaluate the ~~precision and recall performances of the~~ ability of PCMCI+ ~~algorithm~~to correctly identify the presence or absence of causal links.

We tested the performances according to a varying number of variables and 50 times for each number of variables considered.
~~. The result is~~ The results are displayed in Figure 8~~, where the blue curve in Figure 8~~. The blue curve illustrates that precision is not critical, since an increasing number of variables does not lower ~~the~~ it. However, the red curve shows that an increasing number of variable affects the recall. With 60 variables, we retrieve less than half of the expected links (recall criterion). Thus, this experiment clearly illustrates that it is important to give a relatively low number of variables to the algorithm.

Hence, variables need to be selected with great care in order to capture every important feature of the scheme under investigation. In our study, we selected 7 variables to consider key elements for our study and to also have a good compromise with the performance by not having too many variables. If certain key variables are omitted from the set of variables given to PCMCI, there is a risk that some of the causal links found by PCMCI will be incomplete or inaccurate. Forgetting key explanatory variables turns a causality analysis into a correlation analysis.

6 Discussion

470 PCMCI+ has demonstrated its efficiency in identifying model-specific dynamics and highlighting differences between models that may not be immediately apparent on traditional model output intercomparisons. The PCMCI+ method allowed us to explore multiple conceptual schemes through an iterative process of variable selection. By progressively adding or removing variables it is possible to assess the robustness of relationships between variables. Some relationships remain stable despite changes in the variable set, while others emerge or disappear, establishing the relevance of each variable. We were able to

475 separate the role of vertical mixing and advection on controling the variability of NPP. Our analysis suggests that vertical mixing plays a more pronounced role in modulating the intensity of spring bloom NPP in Eastern North Atlantic subpolar gyre than horizontal transport, in line with previous ~~studies~~ study (Ólafsson, 2003). We also observed that stratification during the bloom serves as a significant inhibitor of bloom intensity (Sarmiento et al., 2004), but this relationship is significantly strong in only two of the five models included in this study (IPSL-CM6A-LR, UKESM1-0-LL). As climate change progresses, it is

480 anticipated that NPP in these models will show a greater sensitivity to increasing stratification (Wilson et al., 2022). Moreover, models that currently show no significant impact of stratification on NPP may exhibit a negative effect appearing as global warming intensifies. This could unveil a novel causal relationship emerging under certain climate change scenarios. This inter-model variability of the response of spring bloom NPP to stratification may contribute to the multi-model spread on projected values of NPP.

485 Furthermore, the nutrient transport in this study has been computed along the borders of a large region, with each boundary point of the area (Figure 1) taken into consideration. ~~With the exception of CanESM5-CanOE, this~~ This transport criteria did not allow ~~us~~ to retrieve a consistent link between the gyre strength and the transport ~~.~~ for all the nutrients as discussed in Johnson et al. (2013). In their work, they found an interaction between nitrate and gyre strength and another one, slightly stronger, between phosphate and gyre strength. In our study, we observed more significant relationships for phosphate and

490 fewer for nitrate. However, this criteria allowed to highlight impacts of NAO on nutrient variability via its impact on transport for most of the models. Addressing this indirect link from NAO to nutrient concentration via the transport underscores the importance of a causality based approach and the importance of considering key explanatory variables. If we do not consider transport we may find a spurious link between NAO and nutrient concentration, obscuring a hidden variable. This illustrates results that would have been missed by a correlation-based approach only.

495 The above highlights the complexity of the North Atlantic subpolar gyre and the potential for indirect relationships between variables. Although the NAO does not directly impact nutrient concentrations, it can still influence nutrient availability through indirect pathways. By examining these indirect links, we obtain a more comprehensive understanding of the dynamics of the North Atlantic subpolar gyre and the factors that control nutrient concentrations and NPP. This also emphasises the additional information gained from a causality-based intercomparison approach compared to a correlation-based intercomparison.

500 Despite the redundancy of the oceanic component (NEMO) across selected ESMs, with only CESM2 using a different oceanic model (POP2), we do not observe any unique behaviour specific to CESM2 or a commonality shared by the other four ESMs. It is noteworthy that the two models exhibiting the strongest NAO impact, namely CESM2 and CMCC-ESM2, share

the same atmospheric model CAM6. Simpson et al. (2020) did not identify a distinct behaviour for this atmospheric model compared to others among CMIP models, but did not look at the impact of NAO on specific variables via causality. With our study, it is hard to establish a firm conclusion based on a single member, but applying a causality-based approach to a wider set of simulation using this atmospheric model could offer alternative insights.

The proposed causality-based comparison method also allows to quantify inter-models variations in the strength of variables interactions. While it is expected that winter mixing influences the pre-bloom nutrient stock, variations between the models still exist. All models agree on the significant role of MLD for silicate within a narrow range of strengths. However, the range is somewhat broader for nitrate, phosphate and even more for iron, with CanESM5-CanOE finding MLD not significant. Tagliabue et al. (2016) found a similar result with models having a stronger disagreement for iron~~than for nitrate~~. Also, the unique behaviour we observe in the MEDUSA2 model from UKESM1-0-LL is also discussed in this article with an overestimation of surface iron possibly due to a too long residence time and a too low scavenging rate. We also found a strong auto-correlation for iron (not shown) only for this model which could have the same explanation.

7   Conclusion and perspectives

This study uses a set of Earth System Models to explore the interannual variability of nutrients and NPP in the Eastern North Atlantic Subpolar Gyre. This region is characterized by significant mixing and inter-model uncertainty in nutrient and NPP projections. We established a conceptual scheme to determine which mechanism, vertical mixing or advection, is crucial in explaining multi-model dispersion in nutrient and NPP dynamics in this region.

The method allowed us to extract the causal links from a multivariate conceptual scheme. Our findings indicate that vertical mixing during winter is generally more important for peak spring bloom NPP in this region than horizontal transport. However, the influence of vertical mixing on peak spring bloom NPP still has some variability among the models expressed by the spread of the strength of the link. Combined with model-specific dynamics (e.g. NAO impacting transport, transport impacting nutrient concentration), such differences are likely to contribute to inter-model spread. Stratification is identified as an important factor controlling spring bloom NPP in some, but not all, models. As climate change progresses, it is expected that NPP will suffer from increasing stratification with potentially different reactions to it from one model to another.

Despite its limitations, the causality method used in this study has proven effective in identifying model-specific dynamics and highlighting differences between models that may not be immediately apparent based on usual difference metrics. The proposition of a new dissimilarity measure to be applied on causal graphs has enhanced model comparison by synthesising and quantifying between-model differences.

The method has been verified and can be applied for a variety of purposes such as model evaluation. For example, the comparison of model output and observational data will allow to identify discrepancies in links and associated strengths, suggesting unrealistic model dynamics. The dissimilarity metric proposed could serve as a validation tool. However, it is essential to acknowledge as the recall of PCMCI+ decreases with increasing variables, an important part of the ground truth (True Links existing in the data) can be missed and will add a bias for the validation. While this application is promising, its

implementation would require an in-depth investigation of methodological aspects specific to observational data, particularly regarding the handling of false negatives and the phasing of climate events. Another possible application of the PCMCI+ method involves comparing various experiments, such as different climatic scenarios. This approach facilitates the discovery of new dynamics or the observation of changes in the intensity of existing ones, leading to an improved understanding of models' behaviours under different environmental conditions. Applying the method to climate change scenarios will improve our understanding of the inter-model spread of projected variables (e.g. NPP). Future studies could extend this analysis to a larger ensemble of models and simulations, potentially enabling clustering approaches (Couespel et al., 2024) to identify systematic patterns in causal relationships across this larger range of ESMs.

Author contributions. All authors contributed to the development of the study, the interpretation of the results, and the writing of the manuscript. The lead author processed the data, obtained the results, and proposed the visualization of the results.

Competing interests. The authors declare that they have no conflict of interest

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