



Estimating ocean heat content from the ocean thermal expansion parameters using satellite data

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7 Abstract. Ocean heat content (OHC) is a depth-integrated physical oceanographic variable used to precisely measure ocean warming. Because of the limitations associated with in-situ CTD data and Ocean Reanalysis system products, satellite-based 8 9 approaches have gained importance in estimating the daily to decadal variability of OHC over the vast oceanic region. Efforts to minimize the biases in satellite-based OHC estimates are needed to realize the actual response of the ocean to the brunt of 10 climate change. In the current study, an attempt has been made to better implement the satellite-based ocean thermal expansion 11 12 method to estimate OHC at 17 depth extents ranging from the surface to 700m. To achieve this objective, an artificial neural network (ANN) model was developed to derive thermosteric sea level (TSL) from a given dataset of sea surface temperature, 13 sea surface salinity, geographical coordinates, and climatological TSL. The model-derived TSL data were used to estimate 14 15 OHC changes based on the thermal expansion efficiency of heat. Statistical analysis showed high correlation coefficients and low errors in satellite-derived TSL / OHC at 700 m water depth (N 388469, R 0.9926 / 0.9922, RMSE 1.16 m / 1.56 GJ m⁻², 16 17 MBE -0.1917 m / -0.2400 GJ m⁻², MBPE -0.4560% / -0.0290%, MAE 0.763 m / 1.029 GJ m⁻², and MAPE 2.34% / 0.13%) 18 and nearly similar results at the remaining depth extents. These results suggest that the proposed ANN models are capable of 19 accurately estimating OHC changes on real-time data and three-dimensional distribution patterns of depth-integrated OHC 20 trends in the global ocean. In addition, the first-ever attempt to estimate the ocean thermal expansion component (*i.e.*, TSL) 21 from satellite data was successful and the model-derived TSL can be used to obtain high-end sea-level rise products in the 22 global ocean.

23 1. Introduction

Owing to the vast heat capacity and spatial coverage, the oceans balance the planet's temperatures by absorbing 93% of the excess atmospheric heat caused by the greenhouse effect and global warming (Abraham et al., 2013; IPCC, 2014; Roemmich et al., 2015; Riser et al., 2016; Trenberth et al., 2016; Meyssignac et al., 2019). A precise understanding of the depth-wise penetration of this heat and its accumulation in the upper oceanic layers is inevitable (Liang et al., 2015; Baxter, 2016; IPCC, 2022). Ocean heat content (OHC), a depth-integrated physical oceanographic variable that refers to the amount of heat energy

29 accumulated between any two depths, has gained attention in various studies of the Earth Energy Imbalance (Von Schuckmann





et al., 2016; Trenberth et al., 2016; Cheng et al., 2017; Meyssignac et al., 2019; Cheng et al., 2022). Thus, accurate estimation
of OHC changes at various depth extents is vital and the motivation of the current study.

To obtain a complete picture of OHC changes at different depths, the direct measurements of in-situ conductivity, 32 33 temperature, and depth (CTD) profiles are necessary. These in situ measurements of the ocean properties are limited in terms 34 of depth and spatial coverages, leading to the biased global reconstruction of OHC estimates owing to the sparse measurement 35 data and spatial coverage deficiencies (Jagadeesh et al., 2015; Meyssignac et al., 2019; Marti et al., 2022). However, the insitu CTD profile measurements have been used to develop and validate the different OHC models (Momin et al., 2011; 36 Jagadeesh et al., 2015; Su et al., 2020; Prakash and Shanmugam, 2022). In addition, synthetic CTD profile data generated by 37 38 the Ocean Reanalysis systems (ORA) have been used to compute OHC variability in spatial and temporal scales (Balmaseda 39 et al., 2015; Palmer et al., 2017). More recently, satellite-based methods have become crucial to overcome the limitations in 40 the in-situ measurements of OHC changes, to ensure the OHC trend at a global scale, and to understanding the evolution of the Earth's climate system (Meyssignac et al., 2019; Prakash and Shanmugam, 2022). 41

42 The existing satellite-based OHC algorithms can be broadly grouped into three approaches based on the employed 43 principles/parametrizations: (i) internal tide oceanic tomography (ITOT), (ii) ocean net surface heat fluxes, and (iii) ocean 44 thermal expansion. Apart from these approaches, research is exploring ways to make use of tidal magnetic satellite observations (Irrgang et al., 2019), electrical conductance (Trossman and Tyler, 2019), and atmospheric oxygen & carbon dioxide 45 concentrations (Resplandy et al., 2018) to infer OHC changes. The ITOT technique involves correlating the satellite altimeter-46 derived internal tide phase changes with ocean warming to estimate the OHC variability. This technique is still at the proof-47 48 of-concept level and the associated challenges remain to be addressed (Zhao, 2016; Meyssignac et al., 2019). The OHC 49 estimation through the ocean net surface heat fluxes employs several assumptions and approximations in deriving the input parameters to compute the radiative and turbulent heat fluxes, which in turn leads to a higher uncertainty of global OHC 50 changes (Wild et al., 2015; L'Ecuyer et al., 2015; Meyssignac et al., 2019). On the other hand, the ocean thermal expansion 51 52 method is a promising technique for the estimation of OHC by considering the thermosteric sea level (TSL) and expansion 53 efficiency of heat (EEH). Numerous satellite-based OHC models have been developed based on the sea surface height anomaly 54 data from altimeters, water mass change equivalent sea level anomaly data from the Gravity Recovery and Climate Experiment mission (GRACE), sea surface temperature from the various radiometers onboard satellites, and wind speed/stress from 55 scatterometers/numerical weather models. Pioneering work done by White and Tai (1995), Chambers et al. (1997), Polito et 56 57 al. (2000), and Sato et al. (2000) have attempted to implement the ocean thermal expansion method based on a relationship 58 between OHC and satellite altimeter-based sea surface height anomaly (SSHA). It should be mentioned that regardless of the 59 source, the density of seawater changes when it is subjected to heating/cooling, and it eventually reflects in sea surface topography. The SSHA data recorded by the satellite altimeters comprise the sea surface topography changes due to tides, 60 atmospheric pressure, salinity (haline), and barotropic flows along with the thermal effects. The SSHA changes due to the tides 61 and atmospheric pressure can be corrected, but the effects of salinity and barotropic flows remain unresolved with the OHC 62 63 estimates produced by Wang and Tai (1995) and Chambers et al. (1997). Sato et al. (2000) have introduced a haline correction





factor as the integral product of the haline contraction coefficient and salinity anomaly from in-situ CTD profile data. Owing 64 to the limitations associated with in-situ data, the in-situ-based haline correction cannot be applied to satellite altimeter-based 65 SSHA data while correlating with the space and time-varying OHC data. Jayne et al. (2003) have proposed the Alt-GRACE 66 67 approach to resolve the effect of barotropic flows in sea surface topography by subtracting the satellite gravimetry-derived water mass change component from SSHA data. Though the Alt-GRACE approach has improved the accuracy of satellite-68 69 based OHC estimates compared to Wang and Tai (1995), Chambers et al. (1997), Polito et al. (2000), and Sato et al. (2000), 70 the issues associated with the haline effects and other approximations on the ocean thermal expansion coefficient and seawater density data have led to significant uncertainties in satellite-based OHC estimates. With the advancement of artificial 71 72 intelligence, several researchers have attempted to model OHC by directly relating it with the satellite-based parameters by 73 using deep-learning regression techniques (Jagadeesh and Ali, 2006; Momin et al., 2011; Chacko et al., 2015; Jagadeesh et al., 74 2015; Su et al., 2020, 2021; Marti et al., 2022). These deep-learning models have oversimplified the OHC problem by 75 neglecting the effects of salinity and barotropic flows. In addition, no previous work have accounted for the space and timevarying nature of the ocean thermal expansion coefficient and seawater density in OHC computations. The other common 76 77 drawbacks with the existing work are discussed in Sect. 4.3. Consequently, there is a need for developing a satellite-based 78 model to accurately implement the ocean thermal expansion method to estimate OHC by resolving all the issues associated 79 with salinity variation, barotropic flows, ocean thermal expansion, seawater density, choice of temperature and its units.

80 Given the above background, we have made a major attempt to develop and implement a satellite-based ocean thermal expansion model for estimating OHC changes at various depth extents such as 20 m, 30 m, 40 m, 50 m, 100 m, 150 m, 200 m, 81 82 250 m, 300 m, 350 m, 400 m, 450 m, 500 m, 550 m, 600 m, 650 m, and 700 m. For this, artificial neural network (ANN) 83 architectures were developed to estimate TSL for the given sea surface temperature (SST), sea surface salinity (SSS), geographical coordinates, and climatological TSL. The model-derived TSL estimates were then used to estimate OHC changes 84 by accounting the expansion efficiency of heat. The proposed models are capable of estimating TSL and OHC accurately at 85 86 multiple depth extents. The robustness of the new models was tested by comparison of satellite-derived TSL and OHC with 87 in-situ data.

88 2. Data

For this study, in-situ CTD profile data (collected by Argo floats) were obtained from the World Ocean Database-2018 of the NOAA's National Centers for Environmental Information Data Archive for the period of 2005-2020 (Boyer et al., 2018a). These data have been extensively used by the research community for various ocean applications (Levitus et al., 2009; Momin et al., 2011; Levitus et al., 2012; Cheng et al., 2014; Roemmich et al., 2015; Jagadeesh et al., 2015; Su et al., 2020). The World Ocean Database (WOD) comprises the oceanographic data of diverse biogeochemical parameters that have been collected by various institutions, agencies, individual researchers, and data recovery initiatives. The quality-controlled CTD profile data (*accepted_value* flag) of standard depth levels recommended by the International Association of Physical Oceanography





(1936) were considered in this study to compute the TSL_d and OHC_d parameters and to obtain the SST and SSS data. The 96 97 standard depth levels considered for deriving the TSL and OHC are given as 20 m, 30 m, 40 m, 50 m, 100 m, 150 m, 200 m, 98 250 m, 300 m, 350 m, 400 m, 450 m, 500 m, 550 m, 600 m, 650 m, and 700 m. The in-situ TSL_d and OHC_d parameters were 99 computed by applying the integration formula (Eqs. 1 & 2) on the CTD profile data of depth range from the ocean surface to 100 the respective standard depth (d) as well as the SST and SSS data corresponding to the ocean surface. Similarly, the 101 climatological parameters such as TSLclim,d and OHCclim,d were computed from the monthly climatological temperature and 102 salinity data of 41 vertical levels obtained from the World Ocean Atlas-2018 (WOA) (Boyer et al., 2018b). The theoretical considerations of computing OHC change at a depth can be found in Prakash and Shanmugam (2022) (Prakash and 103 104 Shanmugam, 2022), which were adopted in this study. The Gibbs-SeaWater (GSW) Oceanographic Toolbox of TEOS-10 105 (IOC et al., 2010) was used to compute the in-situ-based parameters including

$$106 \quad OHC_d = \int_0^d \rho C_P \Theta \, dz \tag{1}$$

107
$$TSL_d = \int_0^d \alpha \Theta \, dz \tag{2}$$

where OHC_d refers to the heat energy accumulated in an oceanic layer of depth range from the surface to a stipulated depth (d) and is given in the units of joules per unit area (J m⁻²). Similarly, TSL_d (in meters) refers to the thermosteric sea level integrated from the surface to a stipulated depth (d). And, Θ is the conservative temperature in K (derived from in-situ temperature, absolute salinity, and pressure), ρ is the seawater density in kg m⁻³ (derived from the conservative temperature, absolute salinity, and pressure), C_P is the specific heat capacity (= 3991.87 J kg⁻¹ K⁻¹), and α is the thermal expansion coefficient in K⁻¹ (derived from the conservative temperature, absolute salinity, and pressure).

Python programming was used to prepare the individual databases for all the standard depth levels by extracting CTD profile data from the WOD and WOA NetCDF files with the help of NetCDF4, NumPy, Pandas, and GSW libraries. Each database was divided into two datasets, one for the model development spanning from 2005-2016 and one for validating the model spanning from 2017-2020, by ensuring a well distribution in spatiotemporal scales over the global open ocean. The spatial distribution of data points used to model TSL₇₀₀ and OHC₇₀₀ is shown in Fig. A1. The in-situ CTD profiles of depth coverage shallower than 700 m are also included in this process of deriving the TSL and OHC of other depth extents. Indeed, the number of CTD profiles and their distribution in global oceans is higher than the CTD profile density as shown in Fig. A1.

121 **3. Methodology**

122 **3.1. Theoretical formulations**

Ocean thermal expansion is the best proxy to model the heat content accumulated in an oceanic layer. Unlike freshwater, seawater expands when it warms and contracts when it cools for temperatures above its freezing point. The volumetric expansion of seawater is non-isotropic in nature due to the differences in the degree of constraint in different directions. In a vertical direction, atmospheric pressure exerts a normal force on the seawater parcel at the surface. The magnitude of this





(5)

- normal/vertical force is less compared to the horizontal forces exerted by physical barriers such as continental boundaries and geographic features on the ocean floor. It allows the ocean thermal expansion of seawater in the vertical direction rather than the horizontal direction, as the seawater is less constrained in the vertical direction compared to the horizontal direction. The amount of change in seawater volume in response to the net warming/cooling depends on the absolute conservative temperature and ocean thermal expansion coefficient (Eq. 2). Following are the GSW functions (Eqs. 3-5) (IOC et al., 2010) involved in the calculation of TSL (Eq. 2) for the given set of measured temperature (T), practical salinity (SP), pressure (P), longitude (x), and latitude (y).
- 134Absolute salinity $(SA) = gsw.SA_from_SP(SP, P, x, y)$ (3)135 $\Theta = gsw.CT_from_T(SA, T, P)$ (4)
- 136 $\alpha = gsw. Alpha(SA, \Theta, P)$
- 137 Hence, an attempt has been made in this study to model TSL as a function of SST, SSS, and geographical coordinates. The
- 138 existing correlations between the proposed input parameters and the targeted output parameter were explored by employing
- 139 in-situ-based data used in the model development process (Fig. 1).



140

141 Figure 1. Heatmap showing the Pearson correlation coefficients between the input parameters (*i.e.*, SST, SSS, and
142 geographical coordinates) and the output parameter (TSL) of various depth extents.

143 It is observed that SST has an almost one-to-one correlation with TSL at shallower depth extents, and can be solely 144 used to model the thermal expansion of upper oceanic layers. Despite a decreasing trend in correlation strength when moving 145 towards a deeper depth, SST plays a primary role in accounting for TSL variations at deeper depths, because of its strong 146 correlations with TSL. Observed weaker correlations between SSS and TSL which are plausible owing to the salinity's 147 secondary role in TSL variations as compared to the temperature variable. However, an increasing trend in correlation 148 coefficients between SSS and TSL is observed towards the deeper depth extents. Hence, SST and SSS are complementary to 149 each other in resolving the TSL variations, and their combination plays a major role in modelling TSL of all depth extents considered in this study. Apart from these physical parameters, absolute salinity used in the computation of seawater density, 150 conservative temperature, and ocean thermal expansion coefficient is a function of geographical coordinates along with 151 152 practical salinity and pressure (Eq. 3). By considering all these theoretical considerations and observed correlations, an attempt 153 has been made to model TSL of various depth extents by employing SST, SSS, and geographical coordinates as the input





- 154 parameters along with the climatological TSL (Fig. 2). Here, TSL_d is an external manifestation of OHC_d stored in an oceanic
- 155 layer based on EEH_d (Eq. 6). The model-derived TSL is further used to estimate OHC changes (as shown in Fig. 2 along with
- 156 climatological OHC) as follows,

$$157 \quad OHC_d = \frac{TSL_d}{EEH_d} \tag{6}$$

where *EEH* is a conversion factor that explains the relationship between the relative changes in ocean heat content and the corresponding seawater thermal expansion. As it varies as a function of temperature, salinity, and pressure, EEH is not a constant value over the global ocean. Hence, ANN modelling is employed in this study to derive OHC from TSL by accounting the complex variations in EEH.



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Figure 2. Flow chart representing the parameters involved in TSL and OHC modelling. The red and blue dashed boxes
 represent the TSL and OHC frameworks employed in ANNs, respectively.

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166 **3.2. ANN model description**

167 This section explains the various steps and architectures involved in the ANN modelling of TSL and OHC. The multilayer perceptron regressor algorithm of deep neural networks was used to model both TSL and OHC (Pedregosa et al., 2011). It is 168 169 observed that the input data of geophysical parameters are given in different units and scales. The range and order of SST, SSS, latitude, and longitude data are -1.8 °C to 34.15 °C & $O(10^1)$, 2.53 PSU to 40.45 PSU & $O(10^1)$, -76° to 80° & $O(10^1)$, 170 and -180° to 180° & $O(10^2)$, respectively. In addition, the range and order of TSL_{clim.d} and OHC_{clim.d} are also distinct and vary 171 172 with water depth. Hence, the input data were normalized using the StandardScaler class of Scikit-Learn and feed-forwarded 173 through the neural networks. This StandardScaler normalizes the raw data to ensure the mean and standard deviation of each input parameter as 0 and 1, respectively. It allows the ANN model to focus on the relative importance and relationships between 174 175 the input parameters rather than their magnitude. The standardized input data were injected into the corresponding neurons in 176 the input layer and forward propagated through the hidden layers and then the output layer by applying the random weights 177 and rectified linear unit (ReLU) activation function at each neuron. The mathematical formulations and schematic





representation related to ANN architecture are shown in Fig. 3. The model outputs were compared with the actual data and computed mean squared error (MSE) using a loss function (Eq. 7). In addition, L2 regularization (α_{L2}) was employed to add a penalty term to the loss value to prevent overfitting. The observed error was then backpropagated through the network to update weights and biases using the Adam optimizer based on the learning rate and gradient of the error (see Eq. 8 in Prakash and Shanmugam, 2022). This process is repeated until the validation score improves more than 0.0001.

183
$$MSE = \frac{1}{N} \sum (Y_{pred,i} - Y_{act,i})^2$$

(7)

where N is the number of samples, $Y_{pred,i}$ is the predicted data, and $Y_{act,i}$ is the actual data. The model development work was carried out by employing both the input and output parameters from the in-situ sources. It enables the ANN models to implement the input data of any remote sensing sources to produce OHC estimates subject to the reliability and accuracy of those data sources. The particle swarm optimization technique (Kennedy and Eberhart, 1995; Shi and Eberhart, 1998) was employed for hyperparameter tuning, and the hyperparameters' combinations corresponding to each modelling depth are presented in Table 1. The Joblib module of Scikit-Learn library was used to save all the TSL and OHC models of various depths considered in this study, and the same module was used to load the TSL and OHC models of desired depth with the help of a unified Python script.





- 210 **Table 1.** The ANN model hyperparameters employed in TSL (regular font) and OHC (bold font) modelling of various depth
- 211 extents.

Depth (m)	Hidden layers	Batch size	α_{L2}	Learning rate	No. of iterations
20	38, 10, 55	178	0.00422	0.0004	14
20	49, 12, 34	183	0.09023	0.0001	26
20	100, 97, 36	165	0.00001	0.0001	14
30	11, 50, 55	58	0.00079	0.0001	16
40	64, 71, 5	106	0.00001	0.0001	16
40	57, 89, 46	148	0.09691	0.0001	19
50	64, 99, 30	241	0.01478	0.0001	17
50	56, 59, 10	139	0.07188	0.0001	22
100	70, 100, 100	256	0.00001	0.0009	30
100	25, 36, 63	256	0.03556	0.0016	44
150	47, 83, 92	60	0.00001	0.0005	34
150	49, 77, 28	69	0.05176	0.0318	16
200	100, 100, 16	256	0.00315	0.0022	33
200	27, 48, 67	202	0.05638	0.0367	18
250	56, 82, 67	174	0.00001	0.0019	39
250	2, 100, 77	73	0.00001	0.0037	22
300	83, 28, 74	128	0.00001	0.0028	36
500	48, 92, 10	87	0.01364	0.0459	12
350	85, 25, 67	128	0.04606	0.0013	20
550	27, 53, 48	141	0.08585	0.0851	14
<u> </u>	89, 75, 96	64	0.04859	0.0007	26
400	49, 1, 80	138	0.00001	0.0031	20
450	51, 83, 95	128	0.08582	0.0005	42
430	47, 27, 52	32	0.00263	0.0055	24
500	71, 100, 62	128	0.00001	0.0012	27
500	45, 100, 63	126	0.05162	0.0607	15
550	47, 89, 91	256	0.00843	0.0011	44
550	64, 75, 78	114	0.05176	0.0634	15
600 -	98, 65, 6	16	0.00001	0.0001	48
000	63, 17, 10	180	0.04654	0.0538	23
650 -	100, 69, 75	16	0.00001	0.0001	18
050	53, 74, 40	176	0.07072	0.0048	20
700	98, 37, 37	164	0.04262	0.0015	32
/00	83, 63, 79	216	0.01217	0.0742	19





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Figure 3. Schematic of the ANN architecture employed in the modelling of TSL and OHC parameters. The flow of the modelling and the associated mathematical transformations/formulations are given by considering a typical ANN architecture with n input parameters, one output parameter, p hidden layers, and q1 to qp neurons in each hidden layer.

217 4. Results and discussion

The performance of TSL and OHC models on unseen data from the in-situ and satellite sources was assessed using density scattergrams and statistical metrics. These metrics include mean bias error (MBE), mean bias percentage error (MBPE), mean absolute error (MAE), mean absolute percentage error (MAPE), root mean square error (RMSE), Pearson correlation coefficient (R), slope, and intercept (also referred and presented in Prakash and Shanmugam, 2022). To better understand the model performance, mean values of in-situ data were computed for the validation period and used to compute the weighted average of validation metrics across all the depth extents.





224 4.1. Validation with independent in-situ data

225 The main objective of the independent validation using in-situ data is to evaluate the generalization ability and overall accuracy 226 of TSL and OHC-ANN models on unseen data. For this purpose, the in-situ measured variables such as SST, SSS, and latitude / longitude were inputted into these models to output the predicted values which were then compared with in-situ TSL and 227 228 OHC data. The number of independent validation data points and their spatial distribution are presented in Table 2 and Fig. 229 A1(b). The results in the form of density scattergrams are shown in Figs. 4 and 5. These results showed high correlation and low errors with the model-predicted values. From Table 2 and Fig. 4, the performance of the TSL models is exceptionally 230 231 good on unseen data of all the depth extents without any overfitting. Similar model performance can also be observed in the 232 case of OHC estimates as it primarily depends on the TSL estimates (Table 2 and Fig. 5). The high values of R indicate a 233 strong positive correlation between the predicted and in-situ OHC (TSL) values. This suggests that the models are generally 234 capable of capturing OHC (TSL) patterns in the data. The slope and intercept of the regression line between predicted and actual values are close to 1 and 0, respectively. This suggests that the model-predicted values have good agreement with the 235 236 actual values with a minimal bias. The RMSE values are notably small implying that the predicted OHC values have a little 237 random error when compared to the actual data. The MBE and MBPE values are close to zero, indicating that the modelpredicted values have a negligible systematic error when compared to the actual values. The low MAE and MAPE values are 238 also indicating a high accuracy with the model-predicted OHC values. These results clearly demonstrate that the proposed 239 ANN models succeeded in generalizing and accurately predicting the measured OHC (TSL) data with a high accuracy. 240

241 Spatial distribution of mean percentage error (MPE) over the global open oceanic region was computed by averaging 242 the observed percentage errors of all modelling depths available at each pixel (Fig. A2) for estimating the OHC changes. It is observed that the models' performance is comparatively low over the north-western parts of the North Atlantic gyre, 243 southwestern parts of the South Atlantic gyre, Kuroshio extension, and Antarctic circumpolar regions. An elaborate note on 244 the potential sources of the observed MPE values is given in Sect. 4.4. Further, the entire validation dataset was divided into 245 246 two parts in terms of the observed overestimation and underestimation of data. In the cases of overestimation (underestimation), 247 95% of the data points have a MPE of less than or equal to 0.47% (0.44%). The lower values of MPE indicate that the proposed ANN models succeed in capturing the OHC patterns in all major oceanic basins and can be used to produce accurate OHC 248 products based on their implementation on real-time data. 249







Figure 4. Density scatterplots showing the observed agreement between model-predicted TSL values and in-situ measured
 TSL values during insitu-based independent validation.







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Figure 5. Density scatterplots showing the observed agreement between model-predicted OHC values and in-situ measured 256 OHC values during insitu-based independent validation.





Table 2. Statistical results from the insitu-based independent validation data of TSL (regular font) and OHC (bold font) against
unseen Argo measured in-situ data. The units for the various metrics used in TSL & OHC validations are given as follows:
Mean (m & GJ m⁻²), RMSE (m & GJ m⁻²), MBE (m & GJ m⁻²), MBPE (%), MAE (m & GJ m⁻²), MAPE (%), and intercept (m
& GJ m⁻²).

	<u>N</u>		-	-	RMSE	MBE	MBPE	MAE	MAPE	Slope	Intercept
Depth (m)	Data for model development	Data for independent validation	Mean R								
20	801303	536719	1.44	0.9997	0.01	-0.0007	0.0575	0.006	0.60	0.9981	0.002
20	001505	550717	23.91	0.9997	0.02	-0.0011	-0.0047	0.009	0.04	0.9987	0.030
30	794166	532149	2.15	0.9993	0.03	0.0029	0.3764	0.015	0.99	0.9982	0.007
	794100		32.85	0.9992	0.04	0.0010	0.0027	0.021	0.06	0.9992	0.030
40	0 787074	526571	2.85	0.9988	0.05	-0.0009	0.1325	0.027	1.28	0.9988	0.002
			47.78	0.9988	0.07	-0.0008	-0.0014	0.038	0.08	0.9978	0.103
50	779134	520102	3.54	0.9984	0.07	-0.0008	0.0861	0.042	1.47	0.9975	0.008
	119131	520102	59.70	0.9984	0.10	0.0015	0.0028	0.057	0.10	0.9972	0.169
100	731065	476709	6.80	0.9974	0.18	-0.0129	-0.1725	0.120	2.09	0.9960	0.015
100	751005	470709	119.00	0.9973	0.25	-0.0279	-0.0233	0.169	0.14	0.9981	0.196
150	712120	460278	9.83	0.9967	0.29	-0.0407	-0.3419	0.205	2.41	0.9905	0.053
100	,12120	100270	177.97	0.9965	0.40	-0.0369	-0.0198	0.279	0.16	0.9867	2.331
200	697314	446979	12.64	0.9961	0.38	-0.0001	0.0571	0.272	2.51	0.9960	0.050
200	077514		236.62	0.9959	0.53	-0.0076	-0.0029	0.372	0.16	0.9939	1.426
250	686378	436906	15.28	0.9959	0.46	-0.0361	-0.1803	0.332	2.49	0.9943	0.051
230	250 080578		295.04	0.9957	0.63	-0.0242	-0.0078	0.450	0.15	0.9918	2.392
300	678526	429501	17.80	0.9956	0.55	-0.0471	-0.0023	0.392	2.53	0.9851	0.218
500			353.29	0.9954	0.74	-0.0155	-0.0039	0.525	0.15	0.9889	3.902
350	672148	423688	20.23	0.9949	0.65	-0.1035	-0.3383	0.462	2.59	0.9860	0.179
550	072140		411.40	0.9947	0.87	-0.0357	-0.0081	0.613	0.15	0.9861	5.676
400	666605	418686	22.57	0.9947	0.72	-0.0425	-0.0526	0.505	2.52	0.9887	0.213
400	000005		469.39	0.9945	0.97	-0.0067	-0.0010	0.676	0.14	0.9879	5.683
450	661336	413987	24.83	0.9946	0.78	-0.1227	-0.4726	0.547	2.47	0.9916	0.087
450	001550		527.25	0.9943	1.06	-0.1681	-0.0315	0.741	0.14	0.9872	6.588
500	651990	408240	27.03	0.9949	0.80	-0.0604	-0.1866	0.558	2.29	0.9945	0.089
500	034880		585.03	0.9947	1.07	-0.0761	-0.0127	0.747	0.13	0.9894	6.105
550	640950	403357	29.14	0.9948	0.85	-0.0462	-0.0937	0.586	2.19	0.9911	0.213
550	049850		642.69	0.9945	1.15	0.0347	0.0057	0.787	0.12	0.9900	6.479
6 00	645150	398855	31.21	0.9945	0.91	-0.0390	-0.0205	0.623	2.18	0.9883	0.327
000			700.28	0.9942	1.23	0.0298	0.0046	0.838	0.12	0.9873	8.937
650	640470	392921	33.18	0.9941	0.99	0.0185	0.0903	0.670	2.19	0.9949	0.189
050	040479		757.74	0.9939	1.33	0.0086	0.0014	0.892	0.12	0.9904	7.296
700	633004	388469	35.13	0.9941	1.04	-0.1928	-0.4791	0.711	2.17	0.9858	0.307
/00			815.15	0.9938	1.41	-0.2413	-0.0292	0.960	0.12	0.9836	13.134
Weighted everage			0.9961	0.74	-0.0620	-0.1591	0.513	2.29	0.9927	0.177	
weighted average				0.9960	1.03	-0.0515	-0.0087	0.708	0.13	0.9914	6.648





262 4.2. Satellite-based independent validation

263 The performance of the proposed ANN models in satellite-based applications has been assessed by injecting daily SST and 264 SSS data from the satellite sources in place of the in-situ sources. The choice of satellite sources for SST and SSS data is completely subjective to the intended application and their compatibility in terms of spatial and temporal resolutions, whereas 265 266 geographical coordinates data can be employed from WOA corresponding to the climatological TSL and OHC data. It is recommended to resample SST and SSS data to the WOA grid to eliminate the discrepancies arising from the non-uniform 267 268 spatial references among the input data. In the current study, the NOAA Advanced Very High-Resolution Radiometer 269 (AVHRR) Optimum Interpolation Sea Surface Temperature products (OISST v2.1) were used for daily SST data of 0.25° 270 spatial resolution (Huang et al., 2021). Daily SSS data of the same spatial resolution were obtained from the ORAS5 reanalysis 271 system of the European Centre for Medium-Range Weather Forecasts at the CMEMS portal (Product ID: 272 GLOBAL_REANALYSIS_PHY_001_031) (Zuo et al., 2017). The NetCDF4 and NumPy Python libraries were used to read and resample satellite data to the WOA-18 grid, and to collocate with the corresponding Argo in-situ data points. The accuracy 273 274 of the satellite-based SST and SSS was verified by Argo-measured SST and SSS profile data (N = 244722). The observed R, RMSE, MBE, and MAE values in SST & SSS validations are 0.99 & 0.99, 0.51°C & 0.26 PSU, -0.05°C & -0.006 PSU, and 275 276 0.33°C & 0.12 PSU, respectively. High correlation coefficients and low errors indicate the minimal deviation of satellite-based data from actual (in-situ) data and ensure the reliability of satellite data in accurately representing the physical oceanographic 277 conditions. The satellite-based SST, SSS, latitude, and longitude data were then given as the inputs to the ANN models for 278 279 producing TSL and OHC estimates of all the depth extents considered in this study. Consequently, the model-derived TSL and 280 OHC estimates were compared with Argo-measured in-situ data, and the satellite-based independent validation results are presented in this section (Table 3 and Figs. 6 and 7). 281

The performance of the proposed ANN models on satellite-based independent validation data (Table 3, Figs. 6 and 282 283 7) is rather similar to their performance on in-situ-based independent validation data (Table 2, Figs. 4 and 5). However, the 284 models' performance on satellite-based independent validation data was marginally low as compared to the in-situ-based 285 validation data, likely due to the errors associated with the satellite-derived products. According to the statistical results, the R 286 values were observed to be slightly lower by an average percentage decrease of 0.11% across all depth extents. Similarly, the RMSE, MBE, MBPE, MAE, and MAPE were slightly larger than those values observed during the in-situ-based independent 287 288 validation datasets. This relatively lower performance of the proposed models on the satellite-based independent validation 289 datasets can be observed by comparing the spatial maps and the distribution of MPE (Figs. A2 and A3). The relatively higher 290 magnitudes of MPE can be observed over the northwestern parts of the North Atlantic gyre, southwestern parts of the South 291 Atlantic gyre, Kuroshio extension, and Antarctic circumpolar regions based on in-situ-based validation data. And, 95% of the 292 data have a MPE of less than or equal to 0.56% (0.5%) in the cases of overestimation (underestimation), which is higher than 293 those reported in Sect. 4.1. Though the performance of the proposed models' on satellite-based data is comparatively lower 294 than the in-situ-based validation data, the observed difference in various validation metrics is rather insignificant. It





- substantiates the efficiency of the proposed models in estimating OHC from satellite data at various depth extents over the major oceanic basins. However, it should be noted that the validation results presented in this section are subject to vary with
- 297 the other sources of satellite-based SST and SSS data.



298 299

Figure 6. Density scatterplots showing the observed agreement between model-predicted TSL values and in-situ measured
 TSL values during satellite-based independent validation.







Figure 7. Density scatterplots showing the observed agreement between model-predicted OHC values and in-situ measured
 OHC values during satellite-based independent validation.





Table 3. Statistical results from satellite-based independent validation data of TSL (regular font) and OHC (bold font) against
unseen Argo measured in-situ data. The units for the various metrics used in TSL & OHC validations are given as follows:
Mean (m & GJ m⁻²), RMSE (m & GJ m⁻²), MBE (m & GJ m⁻²), MBPE (%), MAE (m & GJ m⁻²), MAPE (%), and intercept (m
& GJ m⁻²).

	N		-	-	-		-		-		
Depth (m)	Data for model development	Data for independent validation	Mean	R	RMSE	MBE	MBPE	MAE	MAPE	Slope	Intercept
20	20 801303	536719	1.44	0.9987	0.03	-0.0034	-0.0822	0.016	1.67	0.9960	0.002
20	801303	550717	23.91	0.9987	0.04	-0.0049	-0.0201	0.023	0.09	0.9965	0.080
30	794166	532149	2.15	0.9984	0.04	-0.0008	0.2562	0.027	1.88	0.9961	0.008
50	794100	552149	32.85	0.9984	0.06	-0.0043	-0.0118	0.037	0.10	0.9969	0.108
40	0 787074	526571	2.85	0.9980	0.07	-0.0054	0.0211	0.041	2.08	0.9969	0.003
40	787874	520571	47.78	0.9980	0.09	-0.0070	-0.0143	0.057	0.12	0.9959	0.191
50	779134	520102	3.54	0.9977	0.09	-0.0060	-0.0262	0.057	2.17	0.9960	0.008
50	777154	520102	59.70	0.9976	0.12	-0.0056	-0.0090	0.077	0.13	0.9956	0.257
100	100 731065	476709	6.80	0.9966	0.20	-0.0206	-0.2651	0.140	2.56	0.9951	0.013
100	751005	470707	119.00	0.9965	0.28	-0.0385	-0.0322	0.194	0.16	0.9971	0.301
150	712120	460278	9.83	0.9958	0.32	-0.0496	-0.4165	0.229	2.81	0.9897	0.052
150	/12120		177.97	0.9956	0.44	-0.0491	-0.0266	0.311	0.17	0.9858	2.474
200	697314	446979	12.64	0.9951	0.43	-0.0091	-0.0022	0.300	2.83	0.9951	0.053
200	077314		236.62	0.9950	0.59	-0.0200	-0.0081	0.409	0.17	0.9929	1.653
250	686378	436906	15.28	0.9948	0.52	-0.0450	-0.2117	0.364	2.79	0.9928	0.065
230	080378		295.04	0.9946	0.71	-0.0365	-0.0119	0.492	0.17	0.9904	2.807
300	678526	429501	17.80	0.9943	0.62	-0.0556	-0.0279	0.428	2.79	0.9837	0.235
300	078520		353.29	0.9941	0.83	-0.0271	-0.0071	0.571	0.16	0.9875	4.398
350	672148	423688	20.23	0.9939	0.71	-0.1052	-0.3291	0.494	2.80	0.9846	0.206
330	072148		411.40	0.9936	0.95	-0.0381	-0.0086	0.655	0.16	0.9847	6.264
400	666605	418686	22.57	0.9935	0.79	-0.0450	-0.0422	0.540	2.72	0.9869	0.252
400	000005		469.39	0.9933	1.06	-0.0103	-0.0017	0.723	0.15	0.9860	6.557
450	661336	413987	24.83	0.9934	0.87	-0.1234	-0.4559	0.586	2.67	0.9898	0.129
430	001550		527.25	0.9931	1.17	-0.1694	-0.0316	0.792	0.15	0.9854	7.508
500	651990	408240	27.03	0.9934	0.91	-0.0707	-0.2034	0.605	2.50	0.9924	0.134
500	034880	408240	585.03	0.9933	1.21	-0.0909	-0.0151	0.807	0.14	0.9874	7.293
550	C40950	403357	29.14	0.9932	0.97	-0.0484	-0.0768	0.636	2.40	0.9887	0.280
550	049830		642.69	0.9929	1.30	0.0315	0.0053	0.851	0.13	0.9876	8.021
(00	645150	398855	31.21	0.9930	1.03	-0.0431	-0.0139	0.675	2.38	0.9861	0.392
000	645150		700.28	0.9927	1.39	0.0242	0.0039	0.906	0.13	0.9850	10.52
(50	640479	392921	33.18	0.9926	1.11	0.0193	0.1132	0.719	2.37	0.9925	0.267
050			757.74	0.9924	1.48	0.0092	0.0015	0.957	0.13	0.9880	9.090
700	633004	388469	35.13	0.9926	1.16	-0.1917	-0.4560	0.763	2.34	0.9835	0.387
700			815.15	0.9922	1.56	-0.2400	-0.0290	1.029	0.13	0.9813	14.982
XX7 * 1 / 1			0.9950	0.83	-0.0657	-0.1645	0.554	2.54	0.9909	0.224	
weighted average				0.9948	1.15	-0.0566	-0.0104	0.763	0.14	0.9896	7.799





309 4.3. Comparison with the contemporary satellite-based OHC models

Comparison of our ANN models with the existing models is crucial to determine the relative uncertainty in the OHC estimates. 310 Previously, an ANN algorithm suite was developed by the National Remote Sensing Centre (NRSC) of ISRO to disseminate 311 the daily OHC products over the North Indian Ocean (40°E-120°E, 0°-30°N) at a spatial resolution of 0.25 degree (Ali et al., 312 313 2012; Jagadeesh et al., 2015). This algorithm suite includes ANN models to estimate OHC at multiple depth extents such as 314 50 m, 100 m, 150 m, 200 m, 300 m, 500 m, and 700 m for the given input data of sea level anomaly (SLA), SST, and OHC_{clin.d}. It estimates OHC changes by utilizing the satellite altimetry-based SLA data from AVISO (Archiving, Validation, and 315 316 Interpretation of Satellite Oceanographic data) data portal, SST from the Advanced Microwave Scanning Radiometer-2 (AMSR2) onboard JAXA's Global Change Observation Mission 1st-Water (GCOM-W1), and climatological OHC from the 317 World Ocean Atlas-2009 monthly climatological CTD profiles. The multilayer perceptron regressor algorithm of neural 318 319 networks with three hidden layers was used to estimate OHC of all seven depth extents. The number of data points used to develop and validate the NRSC-ANN algorithm were 11472 and 2479, respectively. To estimate OHC changes at different 320 321 depths, this algorithm employs the Celsius scale, in-situ temperature, and average density data instead of the Kelvin scale, 322 conservative temperature, and instantaneous density, respectively (see Eq. 3 in Jagadeesh et al., 2015).

For this inter-comparison purpose, validation datasets were prepared for the period of 2017-2020 by calculating insitu OHC in both Kelvin and Celsius scales for the depth extents of 50 m, 100 m, 150 m, 200 m, 300 m, 500 m, and 700 m. Daily OHC data were obtained from the NRSC's Bhuvan portal and collocated with the corresponding Celsius-scaled in-situ OHC data to evaluate the NRSC-ANN model products. Similarly, satellite-based SST and SSS data, and climatological TSL and OHC data were extracted by collocating with Kelvin-scaled in-situ OHC data for our ANN model to generate the OHC products. Evaluation of these two OHC products was done separately by means of the normalized metrics such as R, MBPE, and MAPE (Table 4).

330 Table 4. Statistical results for our ANN model and NRSC-ANN model obtained from another independent dataset of different

depth extents used in this study.

	N		R	MBI	PE (%)	MAPE (%)		
Depth (m)		NRSC- ANN model	Proposed ANN model	NRSC- ANN model	Proposed ANN model	NRSC- ANN model	Proposed ANN model	
50	15595	0.9223	0.9303	-0.0012	0.0227	1.4762	0.1104	
100	14546	0.8575	0.8780	-0.3539	0.0303	2.5145	0.1732	
150	14303	0.7678	0.8215	-0.6887	-0.0263	3.2401	0.2053	
200	13513	0.7169	0.8152	-1.1048	0.0072	3.4667	0.1903	
300	12833	0.7732	0.8690	-1.2656	0.0218	3.1671	0.1525	
500	12410	0.8965	0.9346	-0.6996	-0.0052	2.3939	0.1073	
700	11959	0.9447	0.9628	-0.6214	-0.0370	2.0035	0.0891	

332





As expected, our ANN model gave more accurate OHC estimates for all depth extents and hence yielded higher correlation coefficients and lower errors as compared to the NRSC-ANN model. The accuracy of OHC estimates produced by our ANN model also increased with depth in contrast to that of NRSC-ANN OHC estimates. Our ANN model was accomplished with the selection of key input parameters based on a precise theoretical basis, accurate computation of in-situ parameters, and selection of separate ANN architectures.

339 It should be mentioned that SLA is the combined outcome of temperature (thermosteric), salinity (halosteric), and water mass changes in the oceanic water column. The direct use of satellite altimeter-derived SLA without eliminating 340 halosteric and water mass change components results in weaker correlations with OHC of various depth extents. Moreover, 341 342 the different time spans were used in the computation of the mean sea level at AVISO (1993-2012) and monthly climatology 343 data at WOA09 (1955-2006). The pair of merged SLA data from AVISO/CMEMS and climatological OHC data from WOA 344 could lead to discrepancies in OHC estimates. Under these considerations, the present study was focused on TSL modelling rather than the Alt-GRACE approach (Meyssignac et al., 2019) to implement the ocean thermal expansion method to estimate 345 OHC changes. 346

347 Celsius scale can be used to compute in-situ OHC where the temperature gradient is always on the positive side. The 348 usage of the Celsius scale when the temperatures are less than zero and greater than the seawater freezing point is not 349 appropriate because of the potential negative values. In addition, the conservative temperature is an accurate variable compared 350 to the direct in-situ temperature or potential temperature. It represents the actual heat content of a mixture of two water masses which are characterized by variations of salinity, pressure, and temperature (Pawlowicz, 2013). Thus, the 9conservative 351 352 temperature is defined in absolute scale (Kelvin scale) and used to calculate the in-situ OHC. On the other hand, employing 353 instantaneous density rather than average density is essential to account for the variations in seawater density which is 354 determined by temperature and salinity changes.

The vertical distribution of conservative temperature varies from equatorial to polar regions, and it follows a nonlinear profile with a mixed layer at the top, a thermocline at the middle, and a deep ocean layer at the bottom. This suggests that it is appropriate to customize the ANN hyperparameters for each modelling depth. In this study, hyperparameter tuning was performed for each modelling depth and it resulted in a better understanding of OHC patterns at various depth extents.

Though a clear improvement was achieved with the proposed OHC models, a relatively lower correlation was observed for our ANN models in the depth range of 100-300 m over the North Indian Ocean (refer to Table 4). Similar results were obtained for the NRSC-ANN models as well. It implies that the proposed ANN models less generalized the OHC patterns at the intermediate depths over the North Indian Ocean. The underlying factors for the less generalized OHC patterns are described in the following section. Nevertheless, the results demonstrated that the proposed ANN models contributed to improving the accuracy and quality of OHC products through the ocean thermal expansion method.





365 4.4. Potential sources of uncertainty in OHC estimates

The relationship between the surficial parameters (SST and SSS) and depth-integrated parameters (TSL and OHC) is the prime 366 factor for determining the efficiency of the proposed OHC models of various depth extents (Klemas and Yan, 2014). This 367 relationship is mainly influenced by a wide range of geophysical processes including ocean currents, vertical mixing 368 (upwelling/downwelling), stratification, fronts, gyres, eddies, and air-sea interface processes. In addition, different climate 369 370 modes and oscillations, solar radiation, sea ice, phytoplankton growth, freshwater inputs, and winds can also be considered in this context. Monthly climatological CTD profiles obtained from the WOA-18 database were objectively analyzed to calculate 371 372 the mean SST and SSS fields over a period of 1955-2017. Hence, these climatological data along with real-time SST and SSS 373 data enabled the ANN models to better generalize the prevailing geophysical processes and subsequent patterns in TSL & OHC of various depth extents. The same can be perceived from the improved accuracy levels observed during the independent 374 375 validations carried out on unseen data (refer to Sects. 4.1 and 4.2) and the comparison with NRSC-OHC model products (Sect. 4.3). 376

377 It should be noted that the established relationship between the input parameters (surficial and climatological) and 378 output parameters (TSL & OHC patterns) may not hold great in the events of the above complex geophysical processes where 379 the physical oceanographic conditions differ significantly from the prevailing conditions. Moreover, the relative contributions of these geophysical processes are subject to vary depending on the time and location of the water parcel in oceans. Slightly 380 lower accuracy of the proposed ANN models can be attributed to the influence of these complex geophysical processes. The 381 382 in-situ and satellite-based retrieval of all these atmospheric/surface/subsurface processes and their incorporation into the ANN 383 models is difficult because of the scarcity/sparsity of the required datasets in different spatial, temporal, and vertical scales. The above factors constitute a potential source of uncertainty in OHC estimates and reduce the generalization ability of the 384 model. Further efforts are needed to better understand, quantify, and eliminate the different sources of observed uncertainties 385 caused by the complex geophysical oceanic processes. More number of in-situ CTD profiles are required to be collected and 386 387 analyzed in such oceanic regions to address the associated complex patterns and processes. Future releases of WOA will 388 certainly resolve the complex patterns in OHC data with the inclusion of newly collected CTD profiles over various oceanic 389 basins.

390 5. A preliminary analysis of global OHC data

This section presents a map of the global distribution of model-derived OHC estimates and its variation from 1993 to 2020. This time period (1993-2020) was chosen based on the availability of satellite-based input data. The NOAA's AVHRR OISST version 2.1 products are available from 1981 to present, but the ECMWF's ORAS5 SSS data are available from 1993 to 2020 only. Thus, for this preliminary analysis, daily OHC estimates were generated for the period from 1993 to 2020 and the corresponding annual mean estimates were computed as shown in Figs. 8a and 8b. Subsequently, the OHC anomalies (OHCA) were estimated by subtracting the annual mean data of 2020 from those of 1993 (Fig. 8c). It is worth mentioning that the heat





content estimates presented in this section cover all the modelling depths. The bathymetry values of each pixel were rounded off to the nearest and lowest modelling depth (d) with the help of GEBCO-2020 bathymetry data (GEBCO Compilation Group, 2020), and the corresponding OHC_d values were considered for that pixel. As the proposed models are built for open oceanic regions, the regions covered by sea ice are masked in both north and south poles by verifying the corresponding daily sea ice concentration data obtained from the National Snow and Ice Data Center (Meier et al., 2021).

402 The spatial patterns of annual OHC product are nearly identical in both 1993 and 2020 (Figs. 8a and 8b). The relatively higher OHC values (830 GJ m⁻² - 840 GJ m⁻²) at a depth of 700 m are observed over the North Atlantic subtropical gyre, Gulf 403 stream, north Arabian sea, eastern Mediterranean sea, and southeastern side of the Madagascar. Next, the OHC values of range 404 820 GJ m⁻² - 830 GJ m⁻² are observed over a vast portion of the major oceanic basins, namely the western parts of the north 405 Pacific ocean ($105^{\circ} \text{ E} - 150^{\circ} \text{ W}, 0^{\circ} - 35^{\circ} \text{ N}$), the western and central parts of the south Pacific ocean ($115^{\circ} \text{ E} - 100^{\circ} \text{ W}, 0^{\circ} - 100^{\circ} \text{ W}$). 406 40° S), the north Atlantic ocean (90° W – 30° E, 0° – 40° N, excluding the north Atlantic subtropical gyre, the Gulf stream, 407 and the eastern Mediterranean sea), the southwestern half of the south Atlantic ocean (55° W – 15° E, 15° S – 40° S), and the 408 Indian ocean ($25^{\circ} \text{ E} - 150^{\circ} \text{ E}, 25^{\circ} \text{ N} - 40^{\circ} \text{ S}$, excluding the north Arabian sea and the southeastern side of the Madagascar). 409 Subsequently, the OHC values in the range of 810 GJ m⁻² - 820 GJ m⁻² are observed over the eastern part of the Pacific ocean 410 and equatorial Pacific ocean ($170^{\circ} \text{ E}-70^{\circ} \text{ W}, 45^{\circ} \text{ S}-40^{\circ} \text{ N}$), northeastern part of the north Atlantic ocean ($50^{\circ} \text{ W}-5^{\circ} \text{ W}$, 411 $40^{\circ} - 55^{\circ}$ N), the equatorial Atlantic ocean, the northeastern half of the south Atlantic ocean (60° W $- 25^{\circ}$ E, 0° S $- 45^{\circ}$ S), 412 and the southeastern parts of the Indian ocean ($60^{\circ} \text{ E} - 150^{\circ} \text{ E}$, $30^{\circ} \text{ S} - 50^{\circ} \text{ S}$). And, the OHC values in the range of 780 GJ 413 m^{-2} - 810 GJ m^{-2} are observed in the latitudinal range of $40^{\circ} - 70^{\circ}$ in both the hemispheres with a decreasing trend from 40° 414 415 to 70°N. In the case of oceanic regions shallower than 700 m, the OHC values are observed to vary widely as shown in Figs. 8a and 8b. 416

Though the spatial patterns and magnitudes of OHC are almost same during the years 1993 and 2020, well-marked warming/cooling regions can be observed in the order of $O(10^{0})$ during 2020 with reference to 1993 (Fig. 8c). The ocean warming of 1.5 GJ m⁻² - 5 GJ m⁻² is observed over the Red Sea, Kuroshio extension, Gulf Stream, and southern side of the Africa (30° S – 45° S). On the other hand, cooling of the same range is observed over the north Atlantic subpolar gyre and southern parts of the Indian Ocean. In addition, several eddy regions are also seen with warming/cooling patterns (Fig. 8c).

In a broader perspective, the observed spatial patterns in OHC and its temporal variation can be attributed to consistent/anomalous warming/cooling in response to the ocean / atmospheric circulations, anthropogenic climate change and internal variability. Consequently, a comprehensive analysis is to be carried out to gain new insights into the underlying phenomena responsible for the observed OHC distributions and its variation in a separate study.

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- 427







20 50 100 200 300 400 500 600 700 750 760 770 780 790 800 810 820 830 840 850 OHC [GJ m⁻²]



750 760 770 HC [GJ m⁻²] 810 820 OHC [GJ m



Figure 8. Maps showing the spatial distribution of OHC during (a) 1993 and (b) 2020, and (c) the observed variation in 2020 with reference to 1993. The oceanic regions shallower than 20 m depth and/or covered with sea ice are masked with a dark gray flag.

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432 6. Conclusion

433 Accurate reconstruction of OHC and analysis of its regional patterns and long-term global records are critical for estimating 434 the Earth Energy Imbalance and understanding the evolution of the climate change. Owing to the lack of instrumentation to cover geographic and depth ranges, OHC estimates from the in-situ measured temperatures are temporally limited and 435 436 insufficiently widespread to capture its spatiotemporal changes and structures. OHC estimates from either different mapping 437 methods or Ocean reanalyses (ORAs) have yielded large uncertainties in past studies. Thus, improving OHC estimates through 438 a novel satellite-based method is the major step forward to overcome sparse observations and reduce the uncertainty in OHC 439 trends. In this study, we proposed an artificial network model to estimate OHC changes in global oceans. The proposed ANN 440 model incorporates the ocean thermal expansion method as a promising tool to estimate OHC changes from satellite data. 441 Accurate implementation of the ocean thermal expansion method was challenging due to the inability of the present-day 442 satellite systems to directly measure the ocean thermal expansion/contraction component. In this study, we proposed a satellitebased novel approach to better implement the ocean thermal expansion method by establishing a relationship between the 443 444 surficial parameters such as SST & SSS and subsurface T-S profiles. This model predicts the depth-integrated TSL component by making use of SST & SSS data and then utilizes the predicted TSL to estimate OHC changes. For this application, we 445 developed ANN models for TSL and OHC of various depth extents such as 20 m, 30 m, 40 m, 50 m, 100 m, 150 m, 200 m, 446 250 m, 300 m, 350 m, 400 m, 450 m, 500 m, 550 m, 600 m, 650 m, and 700 m. The performance of these TSL & OHC models 447 was assessed by using in-situ-based independent data and satellite-based independent validation data, which were extracted 448 449 from the unseen in-situ CTD profiles of the Argo program. Observed high correlations and low errors indicated that the 450 proposed ANN models performed exceptionally good on unseen data of all depth extents without any overfitting and can be used in conjunction with the sea ice thermodynamics-based OHC model of the ice-covered oceanic regions (Prakash and 451 Shanmugam, 2022) to better study the trends and patterns in three-dimensional distribution of OHC in the global oceans. 452

453 The model development and validation databases were prepared by using in-situ CTD profiles obtained from the Argo 454 program and collocated with the corresponding satellite-based daily data of SST (AVHRR v2.1) and SSS (ORAS5). The 455 multilayer perceptron regressor algorithm of deep neural networks was used and its architecture was optimized by evaluating 456 different combinations of hyperparameters for each modelling depth using the particle swarm optimization technique. Precise consideration of theoretical aspects in the selection of input parameters, accurate computation of in-situ OHC, and customized 457 458 ANN architectures enabled the proposed models to establish the accurate relationships between the surficial parameters and 459 depth-integrated OHC (TSL) of various depths extents. The overall performance of the proposed models on satellite data was 460 good, suggesting that these models can be used for a variety of applications subjected to the accuracy requirements and can 461 produce accurate satellite-based OHC (TSL) estimates at various depth extents than previously possible. However, the influence of complex geophysical processes on the generalization ability of ANN models is discussed, and realized that the 462 463 proposed models relatively less generalized the data in the events of complex geophysical processes. Further research should 464 focus on implementation of these models over the oceanic regions with complex geophysical processes. More number of in-





situ CTD profiles need to be collected and analyzed in such oceanic regions to address the associated complex patterns. Future releases of WOA will certainly resolve the complex patterns in OHC data with the inclusion of newly collected CTD profiles over various oceanic basins. However, the scope of the current research includes minimizing the observed marginal gap by exploring new methods/parametrizations in satellite-based OHC modelling approaches.

469 CRediT authorship contribution statement

470 Vijay Prakash Kondeti: Conceptualization, Data curation, Formal analysis, Funding acquisition, Investigation, Methodology,

471 Software, Validation, Visualization, and Writing - original draft. Palanisamy Shanmugam: Conceptualization, Formal

472 analysis, Funding acquisition, Investigation, Methodology, Project administration, Resources, Supervision, and Writing -

473 review & editing.

474 Code and Data availability

475 Data will be made available on request.

476 Declaration of competing interest

477 The authors declare no known competing financial or personal interests in this paper.

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483 References

Abraham, J. P., Baringer, M., Bindoff, N. L., Boyer, T., Cheng, L. J., Church, J. A., Conroy, J. L., Domingues, C. M., Fasullo,
J. T., Gilson, J., Goni, G., Good, S. A., Gorman, J. M., Gouretski, V., Ishii, M., Johnson, G. C., Kizu, S., Lyman, J. M.,
Macdonald, A. M., Minkowycz, W. J., Moffitt, S. E., Palmer, M. D., Piola, A. R., Reseghetti, F., Schuckmann, K., Trenberth,
K. E., Velicogna, I., and Willis, J. K.: A review of global ocean temperature observations: Implications for ocean heat content
estimates and climate change, Rev. Geophys., 51, 450–483, https://doi.org/10.1002/rog.20022, 2013.

Ali, M. M., Jagadeesh, P. S. V., Lin, I. I., and Hsu, J. Y.: A neural network approach to estimate tropical cyclone heat potential
in the Indian Ocean, IEEE Geosci. Remote Sens. Lett., 9, 1114–1117, https://doi.org/10.1109/LGRS.2012.2190491, 2012.





491 Balmaseda, M. A., Hernandez, F., Storto, A., Palmer, M. D., Alves, O., Shi, L., Smith, G. C., Toyoda, T., Valdivieso, M., Barnier, B., Behringer, D., Boyer, T., Chang, Y. S., Chepurin, G. A., Ferry, N., Forget, G., Fujii, Y., Good, S., Guinehut, S., 492 493 Haines, K., Ishikawa, Y., Keeley, S., Köhl, A., Lee, T., Martin, M. J., Masina, S., Masuda, S., Meyssignac, B., Mogensen, K., 494 Parent, L., Peterson, K. A., Tang, Y. M., Yin, Y., Vernieres, G., Wang, X., Waters, J., Wedd, R., Wang, O., Xue, Y., Chevallier, 495 M., Lemieux, J. F., Dupont, F., Kuragano, T., Kamachi, M., Awaji, T., Caltabiano, A., Wilmer-Becker, K., and Gaillard, F.: 496 The ocean reanalyses intercomparison project (ORA-IP), J. Oper. Oceanogr., s80-s97. 8. https://doi.org/10.1080/1755876X.2015.1022329, 2015. 497

Baxter, J. M.: Explaining Ocean Warming: Causes, scale, effects and consequences, edited by: Laffoley, D. and Baxter, J. M.,
IUCN, International Union for Conservation of Nature, https://doi.org/10.2305/IUCN.CH.2016.08.en, 2016.

Boyer, T. P., Baranova, O. K., Coleman, C., Garcia, H. E., Grodsky, A., Locarnini, R. A., Mishonov, A. V, Paver, C. R.,
Reagan, J. R., Seidov, D., Smolyar, I. V, Weathers, K. W., and Zweng, M. M.: NOAA Atlas NESDIS 87. World Ocean
Database 2018, 1–207, 2018a.

Boyer, Tim P.; Garcia, Hernan E.; Locarnini, Ricardo A.; Zweng, Melissa M.; Mishonov, Alexey V.; Reagan, James R.;
Weathers, Katharine A.; Baranova, Olga K.; Seidov, Dan; Smolyar, Igor V. (2018b). World Ocean Atlas 2018. NOAA National
Centers for Environmental Information. Dataset. https://www.ncei.noaa.gov/archive/accession/NCEI-WOA18. Accessed 11

506 October, 2020.

507 Chacko, N., Dutta, D., Ali, M. M., Sharma, J. R., and Dadhwa, V. K.: Near-real-time availability of ocean heat content over
508 the north indian ocean, IEEE Geosci. Remote Sens. Lett., 12, 1033–1036, https://doi.org/10.1109/LGRS.2014.2375196, 2015.

Chambers, D. P., Tapley, B. D., and Stewart, R. H.: Long-period ocean heat storage rates and basin-scale heat fluxes from
TOPEX, J. Geophys. Res. Ocean., 102, 10525–10533, https://doi.org/10.1029/96JC03644, 1997.

511 Cheng, L., Zhu, J., and Sriver, R. L.: Global representation of tropical cyclone-induced ocean thermal changes using Argo data
512 - Part 2: Estimating air - sea heat fluxes and ocean heat content changes, Ocean Sci. Discuss., 11, 2907–2937,
513 https://doi.org/10.5194/osd-11-2907-2014, 2014.

514 Cheng, L., Trenberth, K. E., Fasullo, J., Boyer, T., Abraham, J., and Zhu, J.: Improved estimates of ocean heat content from
515 1960 to 2015, Sci. Adv., 3, 1–11, https://doi.org/10.1126/sciadv.1601545, 2017.

516 Cheng, L., Foster, G., Hausfather, Z., Trenberth, K. E., and Abraham, J.: Improved Quantification of the Rate of Ocean 517 Warming, J. Clim., 35, 4827–4840, https://doi.org/10.1175/jcli-d-21-0895.1, 2022.





Huang, B., Liu, C., Banzon, V., Freeman, E., Graham, G., Hankins, B., Smith, T., and Zhang, H. M.: Improvements of the
Daily Optimum Interpolation Sea Surface Temperature (DOISST) Version 2.1, J. Clim., 34, 2923–2939,
https://doi.org/10.1175/JCLI-D-20-0166.1, 2021.

522 IOC, SCOR, and IAPSO: The international thermodynamic equation of seawater-2010: Calculation and use of thermodynamic
 523 properties Intergovernmental Oceanographic Commission, 2010.

IPCC: Climate Change 2014: Synthesis Report. Contribution of Working Groups I, II and III to the Fifth Assessment Report
 of the Intergovernmental Panel on Climate Change, J. Cryst. Growth, 2014.

526 IPCC: Changing Ocean, Marine Ecosystems, and Dependent Communities, 447–588 pp., 527 https://doi.org/10.1017/9781009157964.013, 2022.

Irrgang, C., Saynisch, J., and Thomas, M.: Estimating global ocean heat content from tidal magnetic satellite observations,
Sci. Rep., 9, 1–8, https://doi.org/10.1038/s41598-019-44397-8, 2019.

Jagadeesh, P. S. V. and Ali, M. M.: Estimation of upper ocean heat content from remote sensing observations in the Arabian
Sea, Remote Sens. Model. Atmos. Ocean. Interact., 6404, 64041C, https://doi.org/10.1117/12.699319, 2006.

Jagadeesh, P. S. V., Suresh Kumar, M., and Ali, M. M.: Estimation of Heat Content and Mean Temperature of Different Ocean
Layers, IEEE J. Sel. Top. Appl. Earth Obs. Remote Sens., 8, 1251–1255, https://doi.org/10.1109/JSTARS.2015.2403877,
2015.

Kennedy, J., & Eberhart, R.: Particle Swarm Optimization, in: In Proceedings of ICNN'95-international conference on neural
networks, IEEE, 1942–1948, https://doi.org/10.1007/978-3-319-46173-1_2, 1995.

Klemas, V. and Yan, X. H.: Subsurface and deeper ocean remote sensing from satellites: An overview and new results, Prog.
Oceanogr., 122, 1–9, https://doi.org/10.1016/j.pocean.2013.11.010, 2014.

L'Ecuyer, T. S., Beaudoing, H. K., Rodell, M., Olson, W., Lin, B., Kato, S., Clayson, C. A., Wood, E., Sheffield, J., Adler, R.,
Huffman, G., Bosilovich, M., Gu, G., Robertson, F., Houser, P. R., Chambers, D., Famiglietti, J. S., Fetzer, E., Liu, W. T.,
Gao, X., Schlosser, C. A., Clark, E., Lettenmaier, D. P., and Hilburn, K.: The observed state of the energy budget in the early
twenty-first century, J. Clim., 28, 8319–8346, https://doi.org/10.1175/JCLI-D-14-00556.1, 2015.

Levitus, S., Antonov, J. I., Boyer, T. P., Locarnini, R. A., Garcia, H. E., and Mishonov, A. V.: Global ocean heat content 1955-543 2008 in revealed instrumentation problems, Geophys. Res. 544 light of recently Lett., 36. 1-5.545 https://doi.org/10.1029/2008GL037155, 2009.





- 546 Levitus, S., Antonov, J. I., Boyer, T. P., Baranova, O. K., Garcia, H. E., Locarnini, R. A., Mishonov, A. V, Reagan, J. R.,
- 547 Seidov, D., Yarosh, E. S., and Zweng, M. M.: World ocean heat content and thermosteric sea level change (0–2000 m), 1955–
- 548 2010, Geophys. Res. Lett., 39, 1–5, https://doi.org/10.1029/2012GL051106, 2012.
- Liang, X., Wunsch, C., Heimbach, P., and Forget, G.: Vertical redistribution of oceanic heat content, J. Clim., 28, 3821–3833,
 https://doi.org/10.1175/JCLI-D-14-00550.1, 2015.
- Marti, F., Blazquez, A., Meyssignac, B., Ablain, M., Barnoud, A., Fraudeau, R., Jugier, R., Chenal, J., Larnicol, G., Pfeffer,
 J., Restano, M., and Benveniste, J.: Monitoring the ocean heat content change and the Earth energy imbalance from space
 altimetry and space gravimetry, Earth Syst. Sci. Data, 14, 229–249, https://doi.org/10.5194/essd-14-229-2022, 2022.
- 554 Meier, W. N., F. Fetterer, A. K. Windnagel, and J. S. Stewart. (2021). NOAA/NSIDC Climate Data Record of Passive
- 555 Microwave Sea Ice Concentration, Version 4 [Data Set]. Boulder, Colorado USA. National Snow and Ice Data Center.
- 556 https://doi.org/10.7265/efmz-2t65. Accessed on 15 November, 2023.
- Meyssignac, B., Boyer, T., Zhao, Z., Hakuba, M. Z., Landerer, F. W., Stammer, D., Köhl, A., Kato, S., L'Ecuyer, T., Ablain,
 M., Abraham, J. P., Blazquez, A., Cazenave, A., Church, J. A., Cowley, R., Cheng, L., Domingues, C., Giglio, D., Gouretski,
 V., Ishii, M., Johnson, G. C., Killick, R. E., Legler, D., Llovel, W., Lyman, J., Palmer, M. D., Piotrowicz, S., Purkey, S.,
 Roemmich, D., Roca, R., Savita, A., Schuckmann, K. von, Speich, S., Stephens, G., Wang, G. G., Wijffels, S. E., and
 Zilberman, N.: Measuring global ocean heat content to estimate the earth energy imbalance, Front. Mar. Sci., 6, 1–31,
 https://doi.org/10.3389/fmars.2019.00432, 2019.
- Momin, I. M., Sharma, R., and Basu, S.: Satellite-derived heat content in the tropical Indian Ocean, Remote Sens. Lett., 2,
 269–277, https://doi.org/10.1080/01431161.2010.519001, 2011.
- 565 Palmer, M. D., Roberts, C. D., Balmaseda, M., Chang, Y. S., Chepurin, G., Ferry, N., Fujii, Y., Good, S. A., Guinehut, S.,
- 566 Haines, K., Hernandez, F., Köhl, A., Lee, T., Martin, M. J., Masina, S., Masuda, S., Peterson, K. A., Storto, A., Toyoda, T.,
- 567 Valdivieso, M., Vernieres, G., Wang, O., and Xue, Y.: Ocean heat content variability and change in an ensemble of ocean
- 568 reanalyses, Clim. Dyn., 49, 909–930, https://doi.org/10.1007/s00382-015-2801-0, 2017.
- 569 Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., Blondel, M., Prettenhofer, P., Weiss, R.,
- 570 Dubourg, V., and Vanderplas, J.: Scikit-learn: Machine learning in Python, J. Mach. Learn. Res., 12, 2825–2830, 2011.
- Polito, P. S., Sato, O. T., and Liu, W. T.: Characterization and validation of the heat storage variability from TOPEX/Poseidon
 at four oceanographic sites, J. Geophys. Res. Ocean., 105, 16911–16921, https://doi.org/10.1029/1999JC000048, 2000.



582



Prakash, K. V. and Shanmugam, P.: Artificial Neural Network Model for Estimating Ocean Heat Content in the Sea Ice-574 10. 109544-109557, 575 Covered Arctic Regions Using Satellite Data. IEEE Access. 576 https://doi.org/10.1109/ACCESS.2022.3213942, 2022.

- Resplandy, L., Keeling, R. F., Eddebbar, Y., Brooks, M. K., Wang, R., Bopp, L., Long, M. C., Dunne, J. P., Koeve, W., and 577
- 578 Oschlies, A.: Quantification of ocean heat uptake from changes in atmospheric O2 and CO2 composition, Nature, 563, 105-108, https://doi.org/10.1038/s41586-018-0651-8, 2018. 579
- 580 Riser, S. C., Freeland, H. J., Roemmich, D., Wijffels, S., Troisi, A., Belbéoch, M., Gilbert, D., Xu, J., Pouliquen, S., Thresher,

A., Le Traon, P. Y., Maze, G., Klein, B., Ravichandran, M., Grant, F., Poulain, P. M., Suga, T., Lim, B., Sterl, A., Sutton, P., 581

Mork, K. A., Vélez-Belchí, P. J., Ansorge, I., King, B., Turton, J., Baringer, M., and Jayne, S. R.: Fifteen years of ocean 583 observations with the global Argo array, Nat. Clim. Chang., 6, 145–153, https://doi.org/10.1038/nclimate2872, 2016.

584 Roemmich, D., Church, J., Gilson, J., Monselesan, D., Sutton, P., and Wijffels, S.: Unabated planetary warming and its ocean 585 structure since 2006, Nat. Clim. Chang., 5, 240–245, https://doi.org/10.1038/nclimate2513, 2015.

Sato, O. T., Polito, P. S., and Liu, W. T.: Importance of salinity measurements in the heat storage estimation from 586 TOPEX/POSEIDON, Geophys. Res. Lett., 27, 549-551, https://doi.org/10.1029/1999GL011003, 2000. 587

588 Von Schuckmann, K., Palmer, M. D., Trenberth, K. E., Cazenave, A., Chambers, D., Champollion, N., Hansen, J., Josey, S.

A., Loeb, N., Mathieu, P. P., Meyssignac, B., and Wild, M.: An imperative to monitor Earth's energy imbalance, Nat. Clim. 589

Chang., 6, 138–144, https://doi.org/10.1038/nclimate2876, 2016. 590

- Shi, Y., & Eberhart, R.: A Modified Particle Swarm Optimizer Algorithm, in: IEEE international conference on evolutionary 591 computation proceedings, 69-73, https://doi.org/10.1109/ICEMI.2007.4350772, 1998. 592
- 593 Su, H., Zhang, H., Geng, X., Qin, T., Lu, W., and Yan, X. H.: OPEN: A new estimation of global ocean heat content for upper 594 2000 meters from remote sensing data, Remote Sens., 12, https://doi.org/10.3390/rs12142294, 2020.
- Su, H., Qin, T., Wang, A., and Lu, W.: Reconstructing ocean heat content for revisiting global ocean warming from remote 595 596 sensing perspectives, Remote Sens., 13, https://doi.org/10.3390/rs13193799, 2021.
- Trenberth, K. E., Fasullo, J. T., von Schuckmann, K., and Cheng, L.: Insights into Earth's energy imbalance from multiple 597 598 sources, J. Clim., 29, 7495-7505, https://doi.org/10.1175/JCLI-D-16-0339.1, 2016.
- Trossman, D. S. and Tyler, R. H.: Predictability of Ocean Heat Content From Electrical Conductance, J. Geophys. Res. Ocean., 599 600 124, 667-679, https://doi.org/10.1029/2018JC014740, 2019.





White, W. B. and Tai, C.: Inferring interannual changes in global upper ocean heat storage from TOPEX altimetry, J. Geophys.
Res. Ocean., 100, 24943–24954, https://doi.org/10.1029/95JC02332, 1995.

- 603 Wild, M., Folini, D., Hakuba, M. Z., Schär, C., Seneviratne, S. I., Kato, S., Rutan, D., Ammann, C., Wood, E. F., and König-
- 604 Langlo, G.: The energy balance over land and oceans: an assessment based on direct observations and CMIP5 climate models,
- 605 Clim. Dyn., 44, 3393–3429, https://doi.org/10.1007/s00382-014-2430-z, 2015.
- 606 Zhao, Z.: Internal tide oceanic tomography, Geophys. Res. Lett., 43, 9157–9164,
 607 https://doi.org/10.1002/2016GL070567.Abstract, 2016.
- Zuo, H., Balmaseda, M. A., and Mogensen, K.: The new eddy-permitting ORAP5 ocean reanalysis: description, evaluation
 and uncertainties in climate signals, Clim. Dyn., 49, 791–811, https://doi.org/10.1007/s00382-015-2675-1, 2017.
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617 Appendix A



618
619 Figure A1. The spatial distribution of in-situ data points used for (a) model development (N=633004 Argo CTD profiles) and
620 (b) validation (N=388469 unseen Argo CTD profiles) in the case of TSL₇₀₀ and OHC₇₀₀.

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Figure A2. Spatial distribution of mean percentage errors observed during the insitu-based independent validation of OHC
 models. The oceanic regions shallower than 20 m and/or covered with sea ice are marked with a dark gray color.







629

630 Figure A3. Spatial distribution of mean percentage errors observed during the satellite-based independent validation of OHC.

631 The oceanic regions shallower than 20 m and/or covered with sea ice are marked with a dark gray color.