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# Classification of synoptic circulation patterns with a two-stage clustering algorithm using the modified structural similarity index metric (SSIM)

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- Abstract. We develop a new classification method for synoptic circulation patterns with the aim to extend the evaluation routine for climate simulations. This classification is applicable to any region of the globe of any size given the reference data. Its unique novelty is the use of the modified structural similarity index metric (SSIM) instead of traditional distance metrics for cluster building. This classification method combines two classical clustering algorithms used iteratively, hierarchical agglomerative clustering (HAC) and k-medoids, with only one pre-set parameter - the threshold on the similarity between two synoptic patterns expressed as the structural similarity index measure SSIM. This threshold is set by the user to imitate the
- human perception of the similarity between two images (similar structure, luminance and contrast), whereby the number of final classes is defined automatically.
   We apply the SSIM-based classification method to the geopotential height at the pressure-level of 500hPa from the reanalysis

data ERA-Interim 1979-2018 and demonstrate that the built classes are 1) consistent to the changes in the input parameter, 2) well separated, 3) spatially stable, 4) temporally stable, and 5) physically meaningful.

20 We demonstrate an exemplary application of the synoptic circulation classes obtained with the new classification method for evaluating CMIP6 historical climate simulations and an alternative reanalysis (for comparison purposes): output fields of CMIP6 simulations (and of the alternative reanalysis) are assigned to the classes and the Jensen-Shannon distance is computed for the match in frequency, transition and duration probabilities of these classes. We propose using this distance metric to supplement a set of commonly used metrics for model evaluation.

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# **1** Introduction

- 30 Research institutions around the world conduct climate studies and share their knowledge with the society and policy makers through The Intergovernmental Panel on Climate Change (IPCC, <u>www.ipcc.ch</u>). The climate simulations used in the IPCC reports are available to other scientists, besides those who run the models, through the Coupled Model Intercomparison Project (CMIP, <u>www.wcrp-climate.org/wgcm-cmip</u>). The first two phases (CMIP1 and CMIP2) of this initiative addressed the ability of numerical climate models to simulate the present climate and to respond to an increase of carbon dioxide concentration in
- 35 the atmosphere (Meehl et al., 1997; Meehl et al., 2000). The extended follow-up phase CMIP3 (Meehl et al., 2007) provided output of coupled ocean-atmosphere model simulations of 20<sup>th</sup>-22<sup>nd</sup> century climate for the 4<sup>th</sup> Assessment Report (AR4) of IPCC (www.ipcc.ch/report/ar4/syr/). As the number of climate simulations in the subsequent projects CMIP5 (Taylor et al., 2012) and CMIP6 (Eyring et al., 2016) continued to increase, new requirements on the "quality" and "reliability" of such simulations emerged. Having multiple models at their disposition, final users have a choice to use all models or only those
- 40 models, which pass a quality check i.e. an evaluation routine. Although testing and comparing models may create an illusion of finding the best one in all its features, we emphasize here: there is no universally valid and absolutely objective evaluation procedure for all purposes. It is important to include a broad suite of metrics into the evaluation spectrum, but various applications may require different subsets of these metrics.

Hannachi et al (2017) emphasized the importance of the correct representation of weather regimes, their spatial patterns, and persistence properties in global circulation models as they could properly simulate the climate variability and long-term

- climatic changes under an external forcing such as, for example, the global warming. However, traditional techniques for climate model evaluation, which are rooted in evaluation techniques for numerical weather prediction models, mainly focus on individual variables and derived indices as summarized by Gleckler et al. (2008). These techniques use scalar variables, called "metrics", and often illustrate symptoms of problems without explaining their causes that possibly may originate from
- 50 incorrect simulation of synoptic weather. As some studies have already demonstrated that the performance of a model varies as a function of weather types (Díaz-Esteban et al., 2020; Nigro et al., 2011; Perez et al., 2014; Radić and Clarke, 2011) we suggest to account for models synoptic behaviour in evaluation routines. But how to capture the correctness of the large scale atmospheric dynamics in models?

The atmospheric circulation is a continuum that gradually changes and its dynamics can be described by a finite number of

- 55 representative "states"/"typical patterns" i.e. classes. Hochman et al. (2021) showed that such representation of the atmosphere by quasi-stationary circulation patterns, often also termed as weather regimes, is a physically meaningful way to describe the atmosphere (and not only a useful statistical categorization as it may be argued). Muñoz et al. (2017) also suggested using the weather-typing approach to diagnose a range of variables in a physically consistent way helping to understand causes of model biases. For evaluation purposes, any climate model simulation can be represented as a sequence of typical synoptic situations,
- 60 previously classified. Common variables used for representing the synoptic circulation are the sea level pressure, geopotential

heights and wind vector fields. Statistical measures, such as frequency and duration of each class, computed from the assigned sequence can be evaluated against reference data derived, for example, from a reanalysis.

Many questions arise when building a classification of weather situations:

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- On which spatial and temporal scales should weather situations be classified?
- Do the frequency and persistence of each weather situation play a role in the classification?
- How many classes are sufficient to describe the atmospheric circulation?

Answers to these questions are not trivial and strongly depend on the purpose of the classification. Weather patterns can be defined at a regular temporal step, typically one day (Lamb, 1972; Hess and Brezowsky, 1952; Fabiano et al., 2020; Cannon, 2012) and be classified independent on their duration (James, 2006; Cannon, 2012; Beck et al.,

2007; Fettweis et al., 2010). Alternatively, only recurrent, quasi-stationary and temporally persistent states of the atmospheric circulation would be classified (Dorrington and Strommen, 2020; Hochman et al., 2021) eliminating short-term patterns in the final set of classes.

There is no "universally correct" recipe on how to build synoptic classes and how many of them. Each application requires a number of classes constructed in a way best suitable for its purposes. A set of classes can be determined subjectively by an

- 75 expert, as the well-known Hess-Brezowski Grosswetterlagen (Gerstengarbe and Werner, 1993; James, 2006; Hess and Brezowsky, 1952) or the Lamb weather types (Lamb, 1972), or using an automated classification method. Multiple different synoptic classifications have been developed over years as summarized by Yarnal et al. (2001) and Huth et al. (2008). An overview and systematization of existing classification methods for synoptic patterns was compiled in a joint effort of multiple European Institutions in the COST Action 733 and summarized in the final project report (Tveito et al., 2016). A
- 80 large number of classes is often used in classification methods that root in synoptic meteorology. Such methods for example, the ZAMG-classification with 43 classes (Baur, 1948; Lauscher, 1985) and the Grosswetterlagen-based classification by James (2006) with 58 weather types (29 for winter and 29 for summer) give priority to a high structural differentiation among synoptic patterns, at the same time trying to maximize the homogeneity inside classes. This attempt may produce some classes, which have a small number of members or could be even empty. On the other hand, methods
- 85 that use a small number of classes focus on large-scale circulation regimes and can be used for investigating possible precursors for their changes, for example shifts of the jet stream (Dorrington and Strommen, 2020). These methods may handle the pattern diversity in a sub-optimal way: prioritize a low number of classes over the high intra-class homogeneity and leave multiple synoptic patterns unclassified.

Our purpose is to extend a traditional evaluation routine for climate models, which typically rests on a set of metrics for scalar

90 variables (Gleckler et al., 2008), by a set of diagnostics considering the correctness of weather pattern representation. We are not the first ones to evaluate model dynamics in such way. Riediger and Gratzki (2014) evaluated climate indices (mean values or hot, cold, wet and dry days) computed for five global circulation models and a reanalysis conditioned on different weather types in a recent and a future climate using a threshold based classification method for the Central European region (Dittmann et al., 1995). Cannon (2020) used two atmospheric classifications constructed on two reanalyses for evaluating historical

- 95 simulations of 15 pairs of global climate models from CMIP5 and CMIP6 datasets; the number of circulation classes used in this study was 16 as suggested in the COST733cat database over smaller European domains (Philipp et al., 2010). Herrera-Lormendez et al. (2021) used Jenkinson-Collison classification adapted to Europe for evaluating some CMIP6 models against three reanalyses and analysed future changes in circulation for these models.
- A "good" set of weather types should be able to describe all physically admissible states and events in the climate system i.e. 100 rain fall events and heat periods can be explained by an occurrence of individual weather types or a particular sequence of certain weather types. Muños et al. (2017) and Nguyen-Le and Yamada (2019) investigated rainfall intensities in dependence of weather types. Adams et al. (2020) found that extreme temperature events, as well as cold anomalies, are related to circulation patterns. As we keep in mind the possible linkage between weather types and extreme weather, we would like to have an automated classification that
- 105
- produces structurally differentiated classes (similar as it is done in synoptic meteorology),
  - is applicable to any domain on the globe,
  - provides high homogeneity inside classes, and
  - encompasses almost all synoptic situations leaving no/or very few situations unclassified.

In our opinion, the last condition is especially important because rare synoptic situations may be linked to severe weather and should be carefully handled in the evaluation procedure for climate models. Therefore, the wide variety of classification methods that focus on very few quasi-stationary weather regimes do not suite our purpose as they eliminate rare synoptic patterns from the analysis. Semi-automated classifications do not suite our purpose of model evaluation either, because these methods require expert knowledge to define weather types in the considered region; this would limit our future options of evaluation to only regions with available experts' knowledge.

- 115 A relatively new group of synoptic classification methods uses self-organizing maps (Kohonen, 2001). These SOM methods employ a neural network algorithm that discovers patterns in data in an unsupervised way. Such algorithms have an advantage as compared to methods based on the principal component analysis (PCA) and subsequent clustering of data as the SOM do not require orthogonality and stationarity of identified classes. Studies that use the SOM-technique to classify synoptic patterns and relate these patterns to local weather (Cassano et al., 2006; Gervais et al., 2016; Hewitson and Crane, 2002; Jiang et al.,
- 120 2011) typically use a pre-defined number of classes and employ the Euclidean distance measure for similarity between data elements and centroids for representing cluster centres. Also the majority of classification methods included in the COST733cat database (Philipp et al., 2010) and in the literature (Cannon et al., 2001; Hochman et al., 2021; Grams et al., 2017; Muñoz et al., 2017; Fabiano et al., 2020) uses the *k-means* clustering algorithm (Milligan, 1985) in conjunction with the Euclidean distance as a metric to measure the degree of similarity between clustered data elements. In this paper we elaborate
- 125 on the draw-backs of using mean fields as cluster centres in the classification of atmospheric data fields and suggest an alternative representation of cluster centres.

Distance metrics typically used in classification algorithms are often Euclidean norms ( $L^2$ -norms), mean squared error (MSE) or Pearson's Distance. MSE remains the standard criterion for comparing modelled and observed signals in climate science

and in optimization routines despite of its weak performance and serious shortcomings in comparing structured signals

130 (pressure or geopotential fields can also be seen as "images") as thoroughly discussed by Wang and Bovik (2009). Following the suggestions of Wang and Bovik (2009), we refrain from using MSE as a distance measure in classifying weather types, and propose using the alternative Structural Similarity Index Metric (SSIM) introduced by Wang et al. (2004) for comparing geopotential fields.

Following the above mentioned arguments, we introduce the new two-stage classification method for synoptic circulation

- 135 patterns as an alternative to existing methods of clustering. The novel approach allows accounting for rare synoptic situations, which may be linked to severe weather and builds synoptic classes automatically without prior experts' knowledge. This alternative method, in our opinion, bears its own scientific value, because as the very least it corroborates previous results, but it even improves upon those previous results in both statistical (number of classes is defined automatically) and climatological aspects (all synoptic situations are classified, applicable to arbitrary regions of the globe without further experts' knowledge).
- 140 The novelty of this method consists of the following features:
  - it classifies all input data without pre-filtering and pre-initialization of classes,
  - it builds classes with strong structural differentiation and high inter-class homogeneity,
  - it uses a structural similarity metric instead of a distance-metric for classifying data,
  - it represents classes by their medoids instead of centroids, and
- it uses an iterative combination of the hierarchical agglomerative algorithm with a partitioning *k-medoids* algorithm to determine the number of clusters automatically.

This classification algorithm does not need an initial distribution of elements and gradually continues building and reviewing clusters until there is no more clusters to be built and reviewed according to a given threshold of similarity.

We demonstrate that the new classification produces a set of well-separated classes, not necessarily of similar size, consistent (small changes in the pre-set parameter do not alter classes strongly), stable with respect to the temporal selection of data (for example randomly chosen and shuffled), stable across various spatial resolutions and data volumes, and physically interpretable (i.e. final classes represent real synoptic situations).

In this paper we describe the new classification method and demonstrate its application to evaluation of global circulation models. The final result of the evaluation is expressed as the Jensen-Shannon distance that can be computed on models statistics.

155 statistics

The paper is structured in the following way: 1) introduction, 2) data and domain description, 3) description of the classification method, 4) presentation of resulting classes, 5) presentation of weather extremes affiliated with the synoptic classes, 6) use of the derived classes in computing the distance metric for evaluating CMIP6 climate simulations, and 7) our conclusions and an outlook for future applications.

#### 160 2 Data

We use four datasets in this study.

<u>The first dataset</u>, a dataset of synthetic data, is used to demonstrate the performance of the classification method explaining why modifications to the classical *k-means* algorithm are necessary. We generated this synthetic data using Gaussian-shaped anomalies trying to mimic the smooth shape of geopotential patterns (the real data we wish to use later) and to illustrate how

- 165 such anomalies are treated by the classification algorithm. The synthetic data are generated randomly and have no genuine structure of the geopotential patterns. However, any clustering algorithm should produce clusters governed by the position of the largest anomaly in the domain and its sign. The original circular shapes of the synthetic generated data help to illustrate how such shapes are grouped into classes by classifications in a simpler manner as if we would have used the real data for this demonstration (using real data makes these distortions less obvious).
- 170 The synthetic data of 1000 elements was generated for the domain of 22x22 grid points. Each field includes one large and 10 smaller Gaussian-shaped superimposed anomalies with randomly chosen sizes, randomly placed within the domain and with randomly chosen signs (negative or positive anomaly); additionally, a randomly generated linear shift of the mean is added to each field. Examples of generated anomaly fields are shown in Figure 1.



- 175 Figure 1: Examples of synthetic data fields. Fields are shown pairwise (a1-b1, a2-b2,...) for demonstrating how visually perceived similarity is quantified in terms of SSIM and MSE given under the lower plot for each pair. Contour lines show the amplitude of negative anomalies (black) and positive anomalies (red) with interval of 0.25. Pairs are ordered by their SSIM-values from a dissimilar pair (on the left) to a strongly similar pair (on the right). Note: smaller MSE does not guarantee larger SSIM-values as for the pair a1-b1.
- 180 <u>The second dataset</u>, reanalysis data, the Reanalysis ERA-Interim (Dee et al., 2011) for the period of 1979-2018 is used as a realistic historical representation of the atmospheric circulation in Europe. The original spatial resolution of this data is approximately 80 km (T255 spectral) on 60 levels. Simulated synoptic regimes are represented by the geopotential height (*zg*)

at the pressure level of 500hPa sampled daily at 12:00 UTC for two practical reasons: 1) it often matches the mid-day peak in extreme weather conditions and 2) it is a typically available time for model output (for subsequent model evaluation). There

- 185 is no necessity of using more frequent fields, for example 1-, 3-, or 6-hourly, as this would increase the data volume but would not add more information on the synoptic patterns: these patterns do not replace each other in few hours but extend over large spatial scales and may persist for several days or longer. Data fields zg are sampled on a grid of  $2^{\circ}x3^{\circ}$  as suggested by participants of the COST Action 733 (Tveito et al., 2016). The coarse-scale sampling is sufficient due to the fact that the synoptic-scale 500-hPa geopotential height does not require high resolution to reproduce the key physical mechanisms (Muñoz 190 et al., 2017). The chosen domain (Figure 2) has 22x22 grid points with the lower left corner at (20°W, 29°N).



Figure 2: Domain for classification of synoptic circulation patterns: crosses show sample points every 2° in latitude and every 3° in longitude directions, 22x22 grid points in total. The solid black line shows the outer edge of the domain.

195 Some typical synoptic patterns may occur in different seasons but should be grouped into one class. As the mean and the variance of the geopotential change seasonally (larger in summer, smaller in winter) the original data should be pre-processed in order to reduce the sensitivity of the classification to the summer variance and the mean in the data. To allow this, we preprocess the original geopotential height fields (zg): removing the seasonal amplitude from the original daily data and normalize the resulting fields by the daily standard deviation as in Eq. (1):

$$200 \quad zg_a = \left(zg - \mu_{zg}\right) / \sigma_{zg} \tag{1}$$



The mean  $\mu_{zg}$  and the standard deviation  $\sigma_{zg}$  are calculated for each grid point and for each day of the year from the 40-years of reanalysis data; both fields are smoothed in time with 151-days running average for each grid cell of the domain. The long smoothing period was chosen with the purpose to produce smooth seasonal curves of the mean 500hPa-geopotential and its standard deviation. Using such smooth mean and standard deviation curves for the normalization of the geopotential fields

205 (prior to clustering) we preserve much of the fields anomaly. The resulting geopotential anomaly fields  $zg_a$  are used in the classification.

Additionally to *zg*, we retrieve ERA-Interim daily near-surface atmosphere temperature (*tas*) and daily total precipitation (*pr*) for demonstrating potential weather extremes affiliated with each synoptic class (See Chapter 5). For these daily variables we compute 90th-percentile map on the original spatial resolution within the chosen domain over the period 1979-2018. For each

210 daily variable we create a map of exceedance: locations where the variable exceeds its  $90^{\text{th}}$ -percentile gets the value of 1, otherwise – 0. These binary maps are summed up for days of the same synoptic class and normalized by the number of days in this class. Final map represents the exceedance probability for the synoptic class.

<u>The third data set</u> is the alternative reanalysis NCEP1 (Kalnay et al., 1996). Any other reanalysis dataset may be taken. Assuming that the alternative reanalysis captures the synoptic circulation of the reference data ERA-Interim (both reanalysis

215 product use and share at least some portion of global weather observations) better than any unconstrained global circulation model, the evaluation of an alternative reanalysis gives an estimate of the lower bound for the attainable value of the distance metric.

<u>The 4<sup>th</sup> dataset of climate model output from the Coupled Model Intercomparison Project Phase 6 (CMIP6, https://www.wcrpclimate.org/wgcm-cmip/wgcm-cmip6, (Eyring et al., 2016)). Based on data availability we chose 32 global circulation models</u>

220 for the historical period 1979-2014, preferably simulation version r1i1p1f1, when available, or r1i1p1f2/r1i1p1f3 otherwise. We use the output data for geopotential at 500hPa of 32 the chosen models to demonstrate a possible evaluation routine that uses the synoptic classes derived on the reference reanalysis.

# 3 Method

- A frequently used approach for identifying circulation regimes is to apply the *k-means* clustering algorithm (Milligan, 1985) to the synoptic circulation data: an overview can be found in the COST733cat database (Philipp et al., 2010) and in the recent literature (Cannon et al., 2001; Hochman et al., 2021; Grams et al., 2017; Muñoz et al., 2017; Fabiano et al., 2020). *K* is the number of classes to be built (this number must be set prior to the classification) and *Means* denotes the average of data elements within each class (also called centroid). The *k-means* method partitions the input data into *K* clusters, so that each data element belongs to the cluster with the nearest centroid minimizing within-cluster variances; the *k-means* method is simple
- and always converges to a solution. Although *k-means* and its multiple variants, as well as the more general group of SOMbased methods with neighbour radius  $\geq 1$ , are commonly applied in the field of the atmospheric science, they exhibit serious limitations with regard to our aims:

- use of centroids (means of all elements in a cluster) to represent classes: using mean fields as cluster centres in the classification of atmospheric data fields may be suboptimal and lead to building classes with dissimilar elements (as shown later in this paper),
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- 2) require a pre-specified number of classes,
- 3) use of structure-insensitive distance metrics (e.g. Euclidean distance) for the optimization of the element assignment among classes. The *k-means* clustering assigns every data element to the cluster centre that is closest to it. This makes the method sensitive to noise in the data and may lead to an assignment of a data element to a structurally dissimilar cluster centre (Falkena et al., 2021); a pair of data fields is structurally dissimilar when it shows patterns perceived by an observer (or characterized with any structural similarity measure) as dissimilar.

The mean squared error (MSE) and the Pearson correlation coefficient (PCC) are probably the dominant quantitative performance metrics in the field of model evaluation and optimization. The *k-means* clustering algorithm typically uses the MSE to measure the distance between clustered data elements. However, Wang and Bovik (2009) demonstrated that the MSE

- has serious disadvantages when applied on data with temporal and spatial dependencies and on data where the error is sensitive to the original signal. Mo et al. (2014) in turn demonstrated that the PCC as a metric is insensitive to differences in the mean and variance. However, atmospheric data (pressure, geopotential, temperature fields) often reveal dependencies in time and space, as well as shifts in the mean and differing variances. Both studies mentioned above (Mo et al., 2014; Wang and Bovik, 2009) recommend using an alternative measure for signal/image similarity, the Structural Similarity (SSIM) index, to quantify
- 250 the goodness of match of two patterns. The SSIM (Wang et al., 2004) simulates the human visual system that "recognizes" structural patterns and error-signal dependencies, and shows a superior performance as a similarity measure over the MSE and PCC.

#### 3.1 Structural Similarity Metric SSIM and its modification.

We use the Structural Similarity index SSIM (Wang et al., 2004) for measuring the similarity between synoptic patterns (SP) represented by the geopotential height anomalies  $zg_a$ . These fields are highly structured images, meaning that the sample points of these images have strong spatial dependencies, and these dependencies carry important information about the structures of the highs and lows in the field. The SSIM incorporates three perception-based components of image difference: structure (covariance), luminance (mean) and contrast (variance):

$$SSIM(x,y) = \frac{(2\mu_x\mu_y+c_1)(2\sigma_{xy}+c_2)}{(\mu_x^2+\mu_y^2+c_1)(\sigma_x^2+\sigma_y^2+c_2)}$$
(2)

260 where

*x*, *y* – non-negative signals/images,  $\mu_x$ ,  $\mu_y$  - average values for *x* and *y*,  $\sigma_x$ ,  $\sigma_y$  - variance for *x* and *y*,

 $\sigma_{xy}$  - covariance of x and y,

265  $c_1$ ,  $c_2$  - stabilizing constants for weak denominator.

For each pair of images the *SSIM-value* is computed, which ranges  $-1 \le SSIM(x,y) \le 1$ . The *SSIM(x,y)*=1 if and only x=y (x and y are two identical images). In practice, most *SSIM-values* are positive and *SSIM(x,y)*<1 identifying some difference between two images. Negative values of SSIM only occur when the covariance term  $\sigma_{xy}$  is negative. The *SSIM-value* is usually computed for multiple sliding windows inside the image. But for simplicity here, only one *SSIM-value* is computed for the whole domain.

270 As the selected domain is relatively large and extends to high latitudes, areal weighting was applied to all fields prior to computing SSIM.

From the formulation of SSIM (2) it is important to note that it is applicable as similarity metric only to same-sign data. However data in climate-related applications are often mixed-sign and/or normalized (with the mean around zero). Therefore, SSIM in its original form (2) cannot be used as the product of means  $\mu_x$  and  $\mu_y$  with different signs in combination with the

275 negative covariance term  $\sigma_{xy}$  as it would yield a positive *SSIM-value*. To overcome this limitation Mo et al. (2014) proposed to "shift" x and y by the minimum value of the two fields:  $x' = x - \psi_{xy}$  and  $y' = y - \psi_{xy}$  are non-negative, where  $\psi_{xy} = min(x_n, y_n | n=1, 2, ..., N)$ . However, this modification weakens the sensitivity of SSIM to the difference between the means as a result of enlarged denominator.

We suggest an alternative modification, which only moderately modifies the magnitude of the denominator preserving the 280 difference between the original means  $\mu_x$  and  $\mu_y$ :

$$SSIM(x,y) = \frac{(2\mu'_x\mu'_y + c_1)(2\sigma_{xy} + c_2)}{((\mu'_x)^2 + (\mu'_y)^2 + c_1)(\sigma_x^2 + \sigma_y^2 + c_2)}$$
(3)

where

$$\mu_x' = \frac{|\mu_x| + |\mu_y|}{2} \tag{4}$$

$$\mu'_{y} = \mu'_{x} + |\mu_{x} - \mu_{y}|.$$
<sup>(5)</sup>

285 The latter formulae (3) is applicable to floating-point data with mixed-sign.

The choice of stabilizing constants is "somewhat arbitrary" as SSIM is "fairly insensitive" to these values - the authors say (Wang et al., 2004). Baker et al. (2022) suggest that  $c_1$  and  $c_2$  should be the same as to make both terms equally influential and propose  $c_1$  and  $c_2$  to be "small enough to not disproportionately influence" the final *SSIM-value*. We set  $c_1 = c_2 = 1e-8$  as suggested by Baker et al. (2022).

# 290 **3.2 Examples of MSE and SSIM as a measures of similarity.**

We get the first glance at the ability of SSIM to capture the structural similarity from its application on the synthetic data (Figure 1). Figure 1 shows fields of the synthetic pairs of maps  $(a_i,b_i)$  for i=1,2,... and their respective values of structural similarity  $SSIM(a_i,b_i)$  and the mean square error  $MSE(a_i,b_i)$  under each pair. Assuming MSE and SSIM are capable measures for similarity between two signals we expect MSE to decline with growing SSIM as the distance between more similar signals chould be smaller than the distance between large similar signals.

should be smaller than the distance between less similar signals. We ordered exemplary pairs in Figure 1 by their increasing



SSIM-value (from left to right side of the plot), but see that respective MSE-values of these pairs do not decline monotonously with increasing similarity. It is remarkable that  $MSE(a_1, b_1) \le MSE(a_2, b_2)$  i.e. the distance between the pair of signals  $(a_1, b_1)$  is smaller than the distance between the pair  $(a_2, b_2)$ , although signals  $a_1$  and  $b_1$  are obviously less similar to each other (they have anomalies of different sizes and placements) as signals  $a_2$  and  $b_2$ . This example implies that using MSE in a clustering algorithm would rather group the pair  $(a_1, b_1)$  into the same class than the pair  $(a_2, b_2)$ . Such preference results from the insensitivity of

MSE to the spatial correlation and could lead to building classes with structurally dissimilar members. Using SSIM instead of

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MSE helps to capture the degree of similarity between clustered signals in a better way on the exemplary synthetic data. Now we show that SSIM applied to real geopotential height anomalies  $zg_a$  is preferable over MSE: in Figure 3 both pairs of geopotential anomalies have MSE(a,b)=MSE(a,c)=0.1, however the pair a-b has a high value of SSIM(a,b)=0.7, whereas for the other pair SSIM(a,c) = -0.3 that indicates dissimilarity. In other words, the MSE does not detect "obviously" dissimilar





Figure 3: The pairs of geopotential anomaly fields *a-b* and *a-c* have same small MSE=0.1 but are strongly different in terms of SSIM: SSIM (a, b) = 0.7 means fields a and b are similar, SSIM (a, c) = -0.3 means fields a and c are dissimilar. Contour lines show the 310 amplitude of anomalies with interval of 1.

These two examples, with the synthetic data (Figure 1) and the real geopotential data (Figure 3), illustrate the weakness of the MSE as similarity metric for comparison (and subsequent clustering) of structured data fields as compared to the SSIM. Therefor we propose using SSIM as similarity measure in a new clustering algorithm.

#### 3.3 Modifications of *k-means* applied to synthetic data

For supporting our previous arguments (about deficiencies of MSE distance measure) we setup and run three experimental 315 classifications on the synthetic data: 1) the classical k-means clustering algorithm with the distance measure MSE (k-means-MSE), 2) the k-means with the alternative similarity measure SSIM (k-means-SSIM), and 3) the k-medoids with the similarity measure SSIM (*k-medoids-SSIM*). For obtaining comparable results, we initialize all three experimental classifications with the same 9 class centres (Figure 4a), which we a-priori derived by an independent run of the hierarchical agglomeration clustering (*HAC*) algorithm (with the SSIM-measure for cluster merging) on the synthetic data set. The *HAC*-algorithm belongs to a family of hierarchical algorithms and uses a completely different strategy for cluster building as opposed to the partitioning algorithms *k-means* and *k-medoids*. This insures that the classes obtained with *HAC* for the subsequent initialization of the *k-means* and *k-medoids* algorithms do not provide any hidden advantage for either of these algorithms.

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325 Figure 4: Cluster centres: a) derived by *HAC*-algorithm and used for the subsequent initialization of the partitioning algorithms, resulted from b) *k-means-MSE* classification, c) *k-means-SSIM* classification, and d) *k-medoids-SSIM* classification. Contour lines show the amplitude of negative (black) and positive anomalies (red) with interval of 0.25. In panels b), c) and d) above each plot numbers of elements (in brackets) in each class are shown.

Results of *k-means-MSE* classification (Figure 4b): these class centres (centroids) visibly deviate from the corresponding initialization fields (Figure 4a) in first place by the reduced magnitude of anomalies as a result of averaging multiple fields. Classes 3, 5 and 9 also have skewed shapes of anomalies, originally circular, as a result of averaging multiple patterns with variously placed anomalies. We already showed (Figure 1 and Figure 3) that small MSE does not guarantee the structural

similarity of compared patterns. Classes built with *k-means-MSE* show very little structural detail as a result of building cluster centroids over multiple class elements, whose structural similarity remained unaccounted. The danger of having such classes

- 335 "with vanishing structure" is that they may serve as attractors for further elements as the clustering algorithm runs targeting at minimizing MSE only. This leads to the so-called "snowballing" effect i.e. the more elements are assigned to this class, the less structure shows its centroid, the more elements are assigned and so on. Cluster 9 (Figure S1) is a good example of such "snowball"-class: although all shown elements have comparable small MSE to the final class centre, their visual (for an observer) and computed similarity (value of SSIM) differs strongly as shown for a group of the first 28 elements (out of 132)
- 340 indicating a strong structural inhomogeneity of patterns contained in one class. This example demonstrates the danger of building "snowball" classes when using MSE as distance metric for data with highly structured patterns. <u>Results of *k*-means-SSIM classification (Figure 4c):</u> in an attempt to avoid building structurally inhomogeneous clusters we replaced the Euclidean distance metric MSE by the structural similarity measure SSIM in the classification algorithm, yielding the *k*-means-SSIM classification. Retrieved classes show some structural patterns that resemble the initial anomaly patterns in
- 345 the data, although weakly pronounced: the amplitude of the large anomaly is reduced and smaller anomalies have nearly vanished by averaging. We see: using SSIM instead of MSE helped to preserve circular shapes of the initial anomalies to some degree, implying that only structurally similar patterns are grouped into one class. However, resulting classes are too smooth in structure (reduced amplitude of anomalies) due to averaging by building centroids.
- Assuming the synthetic data represents some physically meaningful field, for example a pressure or a geopotential field, the 350 weakening of the anomalies amplitude by *k-means-SSIM* and *k-means-MSE* may have serious implications on the interpretability of the resulting classes i.e. these classes do not represent any of the original data elements and, therefore, none of the realistic states of the atmosphere associated with these data. Additionally, such smooth fields would not be able to represent synoptic situations with extreme gradients that may be linked to extreme weather.
- <u>We construct a new *k-medoids-SSIM* classification (Figure 4d)</u> as we keep the similarity metric SSIM (it showed advantages in structure-preserving as compared to MSE) but replace the representation of cluster centres in the clustering algorithm by single "representative" elements – medoids (Kaufman and Rousseeuw, 1990). A medoid is the element of the class with the smallest dissimilarity to all other elements in this class. Each medoid itself is part of the data. Retrieved classes (Figure 4d) show strong anomaly amplitudes and not necessarily resemble their initialization fields, except classes 2 and 7 those medoids remained nearly "untouched" by the classification. The distribution of cluster elements in *k-medoids-SSIM* is done at each step
- 360 of the algorithm by computing the medoid (= element with most mean similarity to all cluster elements) of each cluster. This procedure is less sensitive to the addition of new elements to the cluster than the re-computation of centroids: new cluster elements do not necessarily modify the clusters medoid defined at the previous step of the algorithm. This robustness of the *k-medoids* algorithm (Kaufman and Rousseeuw, 1990) with regard to outliers and noise helps to avoid "snowballing" in cluster building and explains the match of classes 2 and 7 to their initial fields i.e. the initialization of these classes was a "good guess"
- 365 that proved to be robust throughout the *k-medoids-SSIM* algorithm (Note: initial fields ought not to be "good guesses" and to remain preserved by the algorithm).
  - 13

Following the arguments resulting from the application of the three classification algorithms on the synthetic data with structured patterns and structured errors, we propose using *k-medoids* algorithm with the similarity metric SSIM for classification of the real geopotential data as only this algorithm builds a set of classes that represent data elements and include only structurally similar elements.

370 on

# 3.4 Initialization of classes

There are multiple ways of defining the number of classes for the partitioning algorithm *k-medoids* (similarly to *k-means*) ranging from a random guess to the analysis of the data based on principal component analysis PCA, also known as empirical orthogonal functions, Huth (2000). Lee and Sheridan (2012) suggested the initialization of the clustering algorithm by selected

- 375 PCAs. The reason for this statement was the common assumption that the first few modes returned by PCA are physically interpretable and match the underlying signal in the data. However, Fulton and Hegerl (2021) tested this signal-extraction method and demonstrated that it has serious deficiencies when extracting multiple additive synthetic modes (false dipoles instead of monopoles, which may lead to serious misinterpretation of extracted modes). They also found that PCA tends to mix independent spatial regions into single modes. Huth and Beranová (2021) demonstrated that unrotated PCAs (still often
- 380 used) result in patterns that are rather artefacts of the analysis than true modes of variability. Additionally, methods that apply the PCA-filtering to input data, do not suite our purpose as these methods eliminate rare synoptic patterns from the analysis taking into account only a few PCAs with the largest Eigen-values and prevent building classes for rare synoptic situations. Guarded by the above mentioned ideas, we decided not to use the PCA-based initialization of the clustering algorithm. For the initialization of *k-medoids* we suggest using another classical clustering algorithm hierarchical agglomerative clustering
- (*HAC*). An example of *HAC*-retrieved initial classes we described in chapter "3.3 Modifications of *k-means* applied to synthetic data" with the synthetic data: the *HAC*-algorithm builds classes whose centres are used to initialize the subsequent partitioning algorithm. Furthermore, we suggest using a combination of the two clustering algorithms *HAC* and *k-medoids* interactively i.e. merge similar clusters at the first step (HAC) and distribute all data elements to the new clusters at the second step. This two-stage algorithm stops, when no similar clusters are left to combine. This is the final set of clusters. The centres (medoids) of final clusters give the set of classes. We describe the new two-stage clustering algorithm below.

#### 3.5 New classification method: two-stage clustering algorithm

Following the previous considerations, we made three essential decisions to modify the classic *k-means* algorithm in order to construct an algorithm better suitable (from our perspective) for building classes of synoptic patterns:

- Decision 1: use an alternative similarity measure
- 395
- Decision 2: use medoids to represent classes
  - Decision 3: use a two-stage algorithm for the stepwise determination of the number of classes

The two-stage clustering algorithm combines two clustering methods - the hierarchical agglomerative clustering (HAC) and the *k-medoids* clustering - in such way that the output from the first is used as input into the second and vice versa. It inherits the strengths of both contributing algorithms.

- 400 Initially each data element represents its own cluster. Similarity between each pair of synoptic patterns is computed as structural similarity index metric SSIM. The *HAC* is a very flexible clustering method that can use any distance or [dis]similarity measure as it allows different rules for aggregating data into clusters (Schubert and Rousseeuw, 2021). At each step, *HAC* determines the number of clusters and their medoids using a threshold on the *SSIM-value* for merging similar elements into one cluster. The merging threshold *TH<sub>merge</sub>* is set by the user and intuitively means the minimal human-perceived similarity of a pair of
- data elements to be included/merged into one cluster. *K-medoids* builds clusters (similarly to the widely-known method of *k-means*) using the medoid-prototypes and an arbitrary [dis]similarity measure SSIM for cluster elements (D'urso and Massari, 2019; Schubert and Rousseeuw, 2021): it rearranges all data elements among medoid-prototypes (an operation that *HAC* cannot do) in order to maximize the within-cluster homogeneity. *K-medoids* in few iterations produces optimized clusters. The new medoids are computed and initialize the next step of *HAC* and so on.
- 410 At each iteration of the two-stage clustering, the two steps are done in the following way:

#### The 1st Step: *HAC* (merge clusters):

1.

1.1. Clusters with sufficient similarity  $SSIM > TH_{merge}$  are merged: clusters with higher similarity are merged prior to those with lower similarity (the similarity between two clusters is measured as the similarity between their medoid fields)

415 1.2. Temporary cluster medoids are recomputed

# 2. The 2nd Step: *k-medoids* (recompose clusters):

- 2.1. Temporary cluster medoids from the first step are used to initialize the *k-medoids* clustering algorithm
- 2.2. Each data element is assigned to the cluster with the most similar medoid
- 2.3. Cluster medoids are recomputed
- 420 2.4. *K-medoids* clustering is repeated until an optimum (for the given number of medoids!) distribution of all data elements is achieved

Both steps are repeated until there is no sufficiently similar pair of clusters left to be merged.

The presented classification method, as any other classification method, requires some pre-set parameters. The final number of clusters produced by the two-stage clustering algorithm depends on the threshold  $TH_{merge}$  for merging elements into clusters and, eventually, on the amount of data to be clustered. Although the choice of  $TH_{merge}$  is crucial, there is no statistical or analytical formula for computing this threshold, it can only be chosen subjectively by comparing pairs of synoptic patterns (SPs) and asking observers about their perception of similarity. Examples of "similar" synoptic patterns are shown in Figure 5. We analysed multiple pairs of SPs and, based on the personal perception of similarity (our own as well as of persons not involved in the development of this classification method), estimated that the threshold value  $TH_{merge}$  must lie between 0.40

- 430 and 0.45 for recognizable similarity i.e. pairs with SSIM-value less than 0.40 being generally perceived as dissimilar. Figure 5
  - 15

illustrates examples of similarity between three exemplary reference SPs and arbitrarily chosen SPs with *SSIM-values* of 0.60, 0.50, 0.45, 0.40, and -0.10 to each reference. SPs with  $SSIM \ge 0.60$  are "strongly similar" to the reference, SPs with the  $0.40 \le SSIM < 0.60$  are "similar", and with the SSIM < 0.40 - "weakly similar" to the reference. SPs with SSIM < 0 are "dissimilar" to the reference as, by definition of SSIM, the negative values of SSIM result from negative covariance of compared patterns.





Figure 5: Examples of three synoptic patterns  $zg_a$  (left column "reference"). Each row contains examples of alternative synoptic patterns with the *SSIM-value* to the "reference". Contour lines show the amplitude of anomalies with interval of 1.

- The definition of the threshold  $TH_{merge}$  implies that a reduction of its value loosens the requirement on data similarity for cluster building and provides a smaller number of final classes. In contrary, an increase of  $TH_{merge}$  tightens the requirement on the data similarity for cluster building and, therefore, leads to a larger number of final classes. At the same time, the higher  $TH_{merge}$  also loosens the requirement of separation between classes and permits a higher similarity among them. Thus varying the value of  $TH_{merge}$  may be used, to some extent, to steer the clustering algorithm to produce the number of final classes of a particularly desired magnitude.
- 445 Keeping in mind the intended application (evaluation of climate models) the question arises: how many classes do we need to describe the synoptic flow? In the present study, we use 40 years of daily synoptic patterns, 14600 daily data fields, which is a usual number of available reference data in climate research for the industrial time. How many classes do we need to represent synoptic situations of these 40 years? Would 10 or 100 be sufficient? The answer to this question is not trivial. The number of derived classes depends on the pre-set parameter  $TH_{merge}$ . Whereas, values of  $TH_{merge}$  smaller than 0.40 were mainly discarded
- 450 by observers, testing higher values remains reasonable. We test three values for the threshold  $TH_{merge}$  0.40, 0.425, and 0.45. Thus we produce three sets of classes whose separability in dependence of the  $TH_{merge}$  can be analysed.

#### 3.6 Criteria for the evaluation of the clustering algorithm. Choice of the threshold THmerge for class merging.

We analyse the performance of the new method using four criteria suggested by Huth (1996): The clusters should (i) be consistent when pre-set parameters are changed, (ii) be well separated both from each other and from the entire data set, (iii) be stable in space and time, and (iv) reproduce realistic synoptic patterns.

- 455 be stable in space and time, and (iv) reproduce realistic synoptic patterns. <u>Cluster consistency.</u> The consistent evolution of classes implies that small changes in the pre-set parameter  $TH_{merge}$  lead only to small changes in the classes. For illustrating the sensitivity of the clustering algorithm to the choice of  $TH_{merge}$  it was run for three values chosen in the previous chapter, the reference value 0.40 and two higher values 0.425 and 0.45. Classes are consistent if an increase in the number of classes caused by a change in  $TH_{merge}$  is realized predominantly by splitting a few
- 460 classes, with others remaining almost unchanged. Such evolution is difficult to quantify. The consistency of the clusters is illustrated by similarity diagrams - diagrams that resemble the "arrow diagrams" in Huth (1996) - for the sets of classes built with the varying parameter  $TH_{merge}$ .

<u>Cluster separability.</u> We calculate two metrics introduced in the COST Action 733 report (Tveito et al., 2016) for characterizing the separability and within-class variability. Additionally we introduce a new indicator of class separability in

465 terms of similarity. The separation of clusters from randomly chosen data is addressed by the comparison of the metrics/indicators calculated on the clusters to the metrics calculated on "random groups". The "random groups" are generated for each cluster as groups of the same size but of randomly chosen data elements (one realization).

Metric 1: The explained variation EV of the data is determined as the residual between 1.0 and the ratio of the sum of squares within classes (synoptic types) *WSS* to the total sum of squares *TSS*:

$$470 \quad EV = 1 - \frac{WSS}{TSS} \tag{6}$$

Metric 2: The distance ratio *DRATIO* is the ratio of the mean distance between elements assigned to the same class *DI* and the mean distance between elements assigned to different classes *DO*. The Euclidean distance is used for computing *DI* and *DO*:  $DRATIO = \frac{DI}{DO}$ (7)

$$SSIMRATIO = \frac{SSIM_{in}}{SSIM_{out}}$$
(8)

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The mean similarity within classes  $SSIM_{in}$  is calculated as the mean "internal" similarity of all classes, where mean similarityvalue of each element *j* to each element *k* of the same class *i* is computed:

$$SSIM_{in} = \frac{1}{n} \sum_{i=1}^{n} SSIM_{internal,i}$$
<sup>(9)</sup>

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$$SSIM_{internal,i} = \frac{1}{m_i} \sum_{j=1}^{m_i} \frac{1}{m_i} \sum_{k=1}^{m_i} SSIM(j,k),$$
 (10)

where n – number of classes,  $m_i$  – number of elements in class i, SSIM(j, k) – similarity of element j to element k of the same class i.

Mean similarity to other classes  $SSIM_{out}$  is calculated as the mean similarity of all class elements to all class elements of all other classes except its own:

 $485 \quad SSIM_{out} = \frac{1}{n} \sum_{i=1}^{n} SSIM_{external,i}$ (11)

$$SSIM_{external,i} = \frac{1}{m_i} \sum_{j=1}^{m_i} \frac{1}{\sum_{k=1,k\neq j}^n m_k} \sum_{k=1,k\neq j}^n SSIM(j,k),$$
(12)

where n – number of classes,  $m_i$  – number of elements in class i, SSIM(j, k) – similarity of element j to element k of any other class but not of the same class,  $\sum_{k=1,k\neq j}^{n} m_k$ - number of all elements in all classes except class j.

Indicator *SSIMRATIO* could be viewed as an indicator of separability of classes in terms of pairwise similarity value: larger values tell us about stronger within-class similarity in comparison to similarity of other classes.

Note: After comparing the computed metrics and indicators, we discuss the choice of the threshold  $TH_{merge}$ . Once chosen, this value of  $TH_{merge}$  will be used for further analysis throughout the paper.

According to the stop-criterion of the clustering algorithm, each pair of derived classes has similarity value less than  $TH_{merge}$  i.e. in the classification obtained with  $TH_{merge}$ =0.40 each pair of final class medoids is less similar to each other than this

- 495 threshold. Although the classes are represented by the cluster medoids in the clustering algorithm, it is also reasonable to require that the resulting cluster centroids (means) be at least not "strongly similar" (SSIM < 0.60) to each other. We compute matrices of similarities for medoids and for centroids and analyse how well the medoid-separation algorithm provides the separation of centroids in the final set of classes.
- <u>Cluster temporal stability</u>. The amount of input of synoptic data is crucial for building the representative set of classes. In periods of only few years of data important synoptic circulations might be simply un- or under-represented because of longterm variability and, therefore, missing in the final set of classes. The clustering algorithm is run on a continuously increasing data volume of 1,2,...,40 years taken in the chronological order: classes for 1979-1979 (1-year period), classes for 1979-1980 (2-year period), ... classes for 1979-2018 (40-year period). This input data used in chronological order is called "reference data".
- 505 However, the classification method may produce a different number of classes for data of the same volume but different years. Therefore, in order to produce estimations of class numbers that are robust to the choice of the data, we run additionally 60 classifications for the same data volumes of 1,2,...,40 years but picking the data randomly:

- 30 classifications are built with data sampled randomly out of the whole data set (bootstrap method for data selection i.e. data elements may be repeated), cluster centres are initialized as described above in the method: clusters with higher similarity are merged prior to those with lower similarity
- 2) 30 other classifications are built on the data selected randomly (but without repetitions) and cluster centres are initialized randomly: cluster pairs are merged randomly without the preference for more similar pairs (also in a case when the input data is the same as the "reference data", the random initialization of cluster centres yields different pathways of class merging)

515 The first group of the 30 classifications serves to prove the robustness of the classification method to the selection of the input data. The second group of the 30 classifications serves to illustrate the robustness to the initialization of clusters by the input data. We call both of two groups together "randomized data".

We expect that after a certain critical data amount is accumulated, further increase does not lead to a discovery of new classes and the temporal stability of the method is achieved. The minimum critical data amount, *minNYR* (=minimum number of years of data), is set when the number of resulting classes "levels out" and stabilizes.

- The total 61 classifications (obtained on 1 "reference data" + 60 "randomized data") are compared to each other in the following way:
  - search for each class *i* of the classification *k* its counterpart (most similar class) *j* in the classification *l*: each pair of counterparts (*i*,*j*) is detected by maximizing SSIM(*i*,*j*) for all *i* and *j*;
  - weight the similarity value SSIM(i, j) by the frequency of i in the classification k: SSIM(i, j)\*HIST(i), where HIST(i) is the relative frequency of class i in the classification k;
    - compute the total mean weighted similarity, *mwSSIM*, of the classification k to the classification l as the sum of weighted similarity values for all pairs of classes and their counterparts:

# $mwSSIM(k, l) = \sum_{i}^{N} SSIM(i, j) * HIST(i)$

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530 where N – is the number of classes in the classification k, i=1,..N,

j – is the counterpart of class i (class i belongs to the classification k, class j is belongs to the classification l and is the most similar element to i),

(13)

HIST(i) – frequency of the class *i* in the classification *k*.

- We compute the matrix of *mwSSIM* values using the 61 classifications retrieved on at least *minNYR* years of data (note: the number *minNYR* is defined on the "reference data" as the minimum number of years of input data necessary to represent possibly all classes i.e. further increase of this number does not increase the number of resulting classes). We require this matrix to have all elements  $mwSSIM_{i,j}>0.40$ , i.e. each pair of classifications derived on the same volume of data must be on average similar to each other. This "mean similarity" of the classifications indicates the temporal stability of the classes.
- <u>Cluster spatial stability.</u> The stability of the method in space cannot be addressed by applying the clustering algorithm straightforwardly to the data on lower/higher spatial resolution because the pre-set threshold for cluster merging  $TH_{merge}$  is not directly transferable to other spatial grids. The reason for this is simple: a pair of images at a high resolution that appears dissimilar to an observer may have similar low-resolution prototypes (when similarity-determining details are averaged out). However, it can be required that the method determines structurally similar classes at any spatial resolution. To test this, the clustering algorithm is run on the same data but of reduced (4°x6°) and increased (1°x1.5°) spatial resolution. The corresponding
- 545 data sets were built by a resampling of the original data on the low-resolution (4°x6°) and on the high-resolution (1°x1.5°). The retrieved classes from these data sets are compared to the classes on the reference grid (2°x3°). <u>Cluster reproduction and representativity.</u> The method uses medoids as cluster centres and, therefore, the resulting class

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representatives (set of medoids) are elements of the original data and are physically interpretable/plausible synoptic patterns.

However, it is necessary to demand that a cluster medoid represents all cluster elements and their whole entity as a group. For

- 550 each cluster, we compare the cluster centre (medoid) to the cluster mean (centroid) and calculate their similarity value. Based on the similarity values we analyse the representativity of the cluster elements by the medoids. We require that all medoids are strongly similar (SSIM>0.60) to their centroids. Representing a cluster by a medoid guarantees that the medoid has a minimum similarity to each of the cluster elements, furthermore, it is the element with the largest total similarity to all of cluster elements. If a centroid and a medoid of some class are dissimilar, this indicates that there is a group of elements in the class that are
- 555 dissimilar to the medoid.

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#### 3.7 Statistics for model evaluation and the Jensen-Shannon distance metric

The classification done on the "reference data" (reanalysis ERA-Interim of 1979-2018) yields the set of "reference SP-classes". Each data element of the reference data itself, of an alternative reanalysis data (NCEP1) and of each CMIP6-model are assigned to one of the "reference SP-classes" to which it has the maximal similarity. We suggest to compare different datasets assigned to the "reference SP-classes" using the following statistics: histogram of frequencies (*HIST*) for SP-classes through all years and seasons, histograms of frequencies for each season (*HIST*<sub>DJF</sub>, *HIST*<sub>MAM</sub>, *HIST*<sub>SON</sub>), the matrix of transitions

- (TRANSIT) between available classes (frequency for each SP-class to follow another SP-class), and probability of persistence (*PERSIST*) of each SP-class for 1, 2,... 25 days. Whereas, statistics *HIST*, *HIST*<sub>DJF</sub>, *HIST*<sub>MAM</sub>, *HIST*<sub>JJA</sub>, and *HIST*<sub>SON</sub> are one-dimensional vectors with the number of components equal to the number of SP-classes, the *TRANSIT* and *PERSIST* are two-
- 565 dimensional matrices. In case of high dimensionality i.e. many SP-classes, the comparison of these vectors and matrices may become awkward and ambiguous. Therefore for quantifying differences between pairs of such statistics we suggest to weight contributions of each class by its frequency. We compute Jensen-Shannon divergence (Eq.14, similar to the widely used Kullback-Leibler divergence but symmetric and it always has a finite value): frequent elements govern contributions to the distance measure, and vice versa, rare elements make smaller contributions. The Jensen–Shannon divergence, *JSD*, used here
- 570 to measure the similarity between two probability distributions P and Q defined on the same probability space  $\chi$ , is computed in this way:

$$JSD(P \parallel Q) = \frac{1}{2} \sum_{x \in X} P(x) \ln \frac{P(x)}{M(x)} + \frac{1}{2} \sum_{x \in X} Q(x) \ln \frac{Q(x)}{M(x)}$$
(14)

where the probability distributions P and Q are the normalized (the sum of all elements is 1.0) frequency histograms, transitionand persistence-matrices of the reference (Q) and a model (P); space  $\chi$  is a one- or two-dimensional space; M is the mean probability distribution:

575 probability distribution:  

$$M = \frac{P+Q}{2}$$
(15)

It is common to compute the square root of *JSD* as a true metric for distance, the Jensen–Shannon distance (Eq.16):  $JS(P \parallel Q) = \sqrt{JSD(P \parallel Q)}$ (16)

Such distance measure is robust against the "noise" from rare classes and as well as rare class-to-class transitions, but not

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insensitive to them. We show Jensen-Shannon distance metric on various pairs of distributions Figure S2 and discuss its sensitivity in supplement chapter "Sensitivity of Jensen-Shannon distance metric".

# **4** Results

# 4.1. Synoptic classes, effect of the threshold TH<sub>merge</sub> on the number of classes

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We run the classification algorithm on the "reference data" of consistently increasing data volume of 1, 2,.. 40 years and perform 60 additional runs with the "randomized data" for the same data volumes. We repeat every run three times varying the threshold  $TH_{merge}$  – the threshold on similarity between two SPs that defines when these SPs are merged into one class. In total (1+60)\*3 = 183 runs of classification algorithm, each yielding a set of classes, are available for the analysis. Figure 6 shows the evolution of the number of classes in dependence on the volume of input data for three values of  $TH_{merge}$ . Figure 6 illustrates the influence of tightening the requirement on similarity for building clusters: higher thresholds TH<sub>merge</sub> produce larger numbers of final classes with higher within-class similarity of its members. However, at the same time the higher TH<sub>merge</sub> also loosens the requirement to separation among classes (higher similarity between classes is possible).



Figure 6: Number of classes depends on the threshold TH<sub>merge</sub> and on the amount of clustered data. For each tested value of TH<sub>merge</sub> the black solid line shows the mean number of classes computed on 61 classifications (1 with "reference data" + 60 with "randomized 595 data"); the shaded area shows the range of one standard deviation from the mean. The circles show numbers of classes from

# classifications with the "reference data"; circles with crosses highlight class numbers with $TH_{merge}$ =0.425. The horizontal dashed lines show the mean number of classes for each $TH_{merge}$ -value computed on the "reference data" of 40 years.

The application of three values for the threshold  $TH_{merge}$  = 0.40, 0.425, and 0.45 to the "reference data" of maximal volume of 40 years produce 37, 52 and 89 classes, respectively. Computed on all 61 classifications (1 with "reference data" + 60 with "randomized data") for varying  $TH_{merge}$  the numbers of classes (mean ± standard deviation) are estimated 42±6, 59±4, and

- $84\pm5$ , respectively (Figure 6). As expected, the higher values of  $TH_{merge}$  provide larger numbers of classes, although not larger standard deviations of these numbers from their means, as a result of tightening the requirement for within-class similarity. One of the features of our new two-stage clustering algorithm is that it classifies all synoptic patterns including rare ones. This is the reason for the high number of classes build by this algorithm. Figure 7 shows the 37 classes built on the 40 years of the
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"reference data" with  $TH_{merge}=0.40$ : the six most frequent classes SP1, SP3, SP4, SP6, SP15 and SP27 represent together ~42% of the input data, 10 most rare classes (SP11, SP20, SP21, SP23, SP26, SP30, SP31, SP34, SP35, SP37) represent together less than 5% of the input data.



Figure 7: SP-classes (anomalies of geopotential height) obtained on the "reference data" (ERA-Interim Reanalysis, 1979-2018) with the threshold for similarity *TH<sub>merge</sub>=0.40*. Frequencies of SP-classes are shown above the corresponding plots.

At the first glance at Figure 7 all 37 classes may look "patchy" and not different enough from each other. However, all these classes are not similar according to our definition as each pair of them has a similarity value smaller than 0.40 (the threshold

chosen for the classification algorithm). It is important to note that as the class separation is done in terms of SSIM these classes do not have to be differentiated in terms of MSE. We showed previously (Figure 1 and Figure 3) examples of pairs of

- 615 patterns that are similar in terms of MSE, but differ in terms of SSIM. We take a closer look at the six most frequent SP-classes and their full fields (mean + anomaly) as shown in Figure 8. We compare these six classes to the 29 synoptic weather patterns GWL-REA v1.3 fields (personal communication) developed in German Meteorological Service (Deutscher Wetterdienst, <u>www.dwd.de</u>) - Hess-Brezowksy Grosswetterlagen identified on reanalysis data based on correlations in combination with Lamb Weather Type statistics (James and Ostermöller, 2022). For
- 620 each of the six SP-classes we compare its similarity value to each of the GWL-REA v1.3 field (Geopotential) and identify the most similar one/pair:
  - SP1: Cyclonic South-Westerly (SWZ- Südwestlage zyklonal)/Cyclonic Westerly (WZ Westlage zyklonal)
  - SP6: Low over Central Europe (TM- Tief Mitteleuropa)
  - SP27: Low over the British Isles (TB Tief Britische Inseln)
  - SP15: Anticyclonic Westerly (WA- Westlage antizyklonal)

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- SP4: Anticyclonic South-Easterly (SEA Südostlage antizyklonal)
- SP3: Anticyclonic North-Westerly (NWA Nordwestlage antizyklonal)

Correspondences of the six frequent classes to the patterns GWL-REA v1.3 provide us with an evidence that, albeit not tuned to and not required to mimic semi-manual classifications, the new classification method determines not just arbitrary synoptic patterns but meaningful synoptic situations described by experts.



Figure 8: Geopotential Height [m] for six most frequent SP-classes. The contour lines show the geopotential height levels every 100 m (labelled). The number of the SP-class and its frequency are on the top of each plot.

635 The three sets of classes obtained on the "reference data" of the full volume with varying  $TH_{merge}$  are further analysed with respect to consistency, separability, stability, and representativity of the data.

#### 4.2 Cluster consistency

The evolution of classes built with different values of *TH<sub>merge</sub>* is presented in the form of a diagram (Figure 9), which is also called "arrow diagram" suggesting that lines show how classes are related among different sets of classes. For the "arrow diagram" in Figure 9 the classes are derived by running the clustering algorithm on the data of one full year. We chose this minimal data volume to build classes with few elements for demonstrating the tightening similarity constrain (by the threshold *TH<sub>merge</sub>*) in the best way as classes with large numbers of elements may reveal similarities among subsets of some elements and overload the diagram. In Figure 9 identical classes (SSIM=1 for the medoids) are connected with thick solid black lines, strongly similar classes (0.60≤SSIM<1) are connected with dashed thick black lines, similar classes (0.40≤SSIM<0.60) are connected by thin grey lines, where connections with 0.40≤SSIM<0.425 are dashed. When increasing the merging threshold 0.40 → 0.425 the total number of classes rises 31 → 34 with 26 classes remaining identical or "strongly similar", 5 remain</li>

- without a strongly similar counterpart and 8 new classes emerge. Further rising the threshold value  $0.425 \rightarrow 0.45$  leads to building of 39 classes with 36 classes remaining identical or strongly similar, 2 classes remain without a strongly similar counterpart and 7 new classes emerge. The new emerging classes may have similarity to more than one previous class. We see
- 650 that 23 classes retain their medoids through the two steps of tightening the similarity constrain  $(0.40 \rightarrow 0.425 \rightarrow 0.45)$ . It is important to note: the identical classes have only one counterpart in each set of classes that means they are "transferred" to the next set of classes obtained with a higher  $TH_{merge}$  and not "split" into new classes. The "strongly similar" classes typically have only one or - rarely - only few counterparts i.e. they are rarely split. New emerging classes may have similarities to multiple original classes. The fulfilment of the demand on the consistency of class evolution is shown by the prevalence of identical
- 655 classes in the diagram, indicating one-to-one correspondence between classes of different sets. The identical classes, which remain unchanged, are connected with thick solid lines and are often accompanied by a 'bunch' of thin lines. Such 'bunches' are mainly produced by the breaking off some elements from the class on the left side into its own class on the right side; the medoid of the original class on the left side remains preserved. For new emerging classes (on the right side) similarities to multiple original classes (on the left side) are acceptable as new classes may contain elements broke off from multiple original
- 660 left side classes. An unwanted form of the diagram would be a distribution of classes from set to set connected with thin lines, without clearly preserved identical types.





Figure 9: Similarity between classes derived with different merging threshold: (left) 31 classes obtained with  $TH_{merge}=0.40$ , (middle) 34 classes with  $TH_{merge}=0.425$ , and (right) 39 classes with  $TH_{merge}=0.45$ . Black thick lines connect identical classes (SSIM=1), black dashed lines connect "strongly similar" classes ( $0.60 \le SSIM \le 1$ ), grey lines connect similar classes ( $0.40 \le SSIM \le 0.60$ ), where connections with  $0.40 \le SSIM \le 0.425$  are dashed. Following the black solid lines from left-to-right: 23 classes retain their medoids.

#### 4.3 Cluster separability

The metrics *EV*, *DRATIO* and indicators *SSIM<sub>in</sub>*, *SSIM<sub>out</sub>*, *SSIMRATIO* computed on the classes obtained with increasing *TH<sub>merge</sub>* illustrate the importance of the choice of this threshold and its influence on the number of derived classes and their separability. Table 1 presents the values of the chosen metrics and indicators. Please note: metrics *EV* and *DRATIO* illustrate only (!) the influence of the *TH<sub>merge</sub>* on the final set of classes and do not describe the quality of classes as they are computed



using the Euclidean Distance – a measure that was not optimized by the clustering algorithm. Therefore, EV and DRATIO should not be used to assess the absolute performance of the classification, but the relative performance depending on  $TH_{merge}$ .

Classifications with larger numbers of classes achieve a better skill EV than those with less classes due to the natural fact that

- 675 a larger number of classes captures a higher fraction of the variation. The extreme case, when the total variation is explained completely (EV=1), is achieved when the number of classes is equal to the number of data. Therefore, it would be dangerous to favour classifications with larger numbers of classes based on this metric. In the present study, the set of classes obtained with  $TH_{merge}=0.45$  provides the highest ratio of explained variation. Clusters of randomly chosen groups, as expected, show nearly no explained variation at all (see Table 1).
- 680 Values of the metric DRATIO < 1.0 indicate that, on average, elements within classes have shorter Euclidean distance to each other than to elements of other classes. Smaller values of DRATIO indicate a stronger separation of classes. The highest value of  $TH_{merge}=0.45$  provides the lowest value of DRATIO and, therefore, shows the best separation of classes in terms of Euclidean distance. In randomly chosen groups the value of DRATIO is close to 1, as also shown in Table 1, because of nearly equal distances between elements of the same class and of different classes.
- Table 1: Metrics for classes obtained in three experiments with varying merging-threshold (*TH<sub>merge</sub>*) applied on the "reference data" of 40 years. Values after "/" are those computed on random groups.

THmerge	Number	EV	DRATIO	SSIM <sub>in</sub>	SSIM <sub>out</sub>	SSIMRATIO	
	of	classes/random	classes/random	classes/random	classes/random	classes/random	
	classes						
0.40	37	0.3825/0.0028	0.6059/0.9968	0.3252/0.0317	0.0158/0.0316	20.58/1.00	
0.425	52	0.4055/0.0042	0.5839/0.9954	0.3412/0.0319	0.0180/0.0316	19.96/1.01	
0.45	89	0.4476/0.0066	0.5447/0.9929	0.3695/0.0317	0.0215/0.0316	17.19/1.00	

Indicators  $SSIM_{in}$  and  $SSIM_{out}$  represent the influence of the similarity constrain by  $TH_{merge}$  on the separability/homogeneity of the final classes. A good performance of the classification is achieved when similarity among elements of one class  $SSIM_{in}$  is

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the final classes. A good performance of the classification is achieved when similarity among elements of one class  $SSIM_{in}$  is much higher than the similarity to elements of other classes  $SSIM_{out}$  i. e. SSIMRATIO should be maximized. The maximal mean similarity among elements of the same class ( $SSI_{in}=0.3695$ ) is given by  $TH_{merge}=0.45$ , however, the mean similarity between pairs of elements of different classes ( $SSI_{out}=0.0215$ ) is also the highest for this threshold indicating stronger similarities among elements of different classes as well. Finally, SSIMRATIO – an indicator of class separation on terms of similarity - is highest (20.58) for  $TH_{merge}=0.40$  and shows the favourable separation of classes in terms of similarity among elements.

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At this point we make an important decision and choose the classification obtained with the merging threshold of  $TH_{merge} = 0.400$  for further analysis for two reasons: 1) this threshold provides good class separation; 2) using this value we produce fewer classes, which can be meaningfully statistically analysed (a higher threshold value would produce

more classes with fewer members). It is also important to note that a smaller number of classes is easier to describe verbally, more intuitive to understand and to separate visually.

The stop-criterion in the clustering algorithm guarantees that the maximum similarity between final classes is less than  $TH_{merge}$ . In other words, there is no pair of final medoids similar to each other, otherwise they would have ended up in the same cluster. Although it cannot be demanded that cluster centroids (means) also satisfy the same criterion on the maximum pairwise similarity, it can be demanded that cluster centroids are at least not "strongly similar" i.e. pairwise *SSIM*<0.60. Figure 10

shows matrices of pairwise similarities for medoids (left) and for corresponding centroids (right). Some pairs of centroids have a similarity value higher than any pair of medoids (circles show  $SSIM \ge 0.40$ ) due to the fact, that the similarity of medoids but not of centroids was the optimized quantity in the clustering algorithm. The maximal similarity for a pair of centroids is SSIM=0.542 (for centroids 1 and 22) i.e. there is no pair of "strongly similar" centroids. This gives an evidence that the twostage clustering algorithm that uses medoids as class centres produces classes with also meaningfully separated centroids.



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Figure 10: Matrix of pairwise similarity values for 37 classes derived with  $TH_{merge}=0.40$ . Left panel: the matrix of SSIM for cluster medoids. Right panel: the matrix of SSIM for cluster centroids. Circles show similarity values greater than 0.40. Only the upper left half of each matrix is shown due to the symmetry; diagonal elements have SSIM=1.

# 715 4.4 Cluster stability

<u>Temporal stability</u>. As we apply the classification algorithm on the data volume of 1,2, ... 40 years. The number of derived classes "levels off" after approximately 30 years of daily data for all values of  $TH_{merge}$  (Figure 6): this means that all possible synoptic patterns are likely to be captured within 30 years. This data volume matches with periods typically used for assessing the variability of other climate variables. Thus, we recommend the minimum critical data amount *minNYR=30* years of data for a temporally stable classification. To support this recommendation, we compute the matrix of the "mean weighted

similarity" *mwSSIM* for 61 sets of classes retrieved on 30, 35 and 40 years of data. We require this matrix to have all elements  $mvSSIM_{i,j} > 0.40$  i.e. each pair of sets of classes must be on average similar to each other.

The number of classes in all 61 sets generated on *minNYR*=30 years of data varies from 36 to 59 classes, with the mean number of classes 42. For all 61 sets of classes, we computed the pairwise mean weighted similarity *mwSSIM* (Figure 11). The value

- of mwSSIM(k,l) shows the match of all classes from the set k to all classes from the set l, weighted by the frequency of the classes in the set k. The matrix of pairwise mwSSIM values is not symmetric:  $mwSSIM(k,l) \neq mwSSIM(k,l)$  as the sets k and l may have different numbers of classes and also the classes differ. When the numbers of classes in sets k and l are different, the following may occur: for class i from set k the class j from set l is the most similar counterpart, but (!) for the class j from the set l a different class h from set k is the most similar one, leaving the class i being the second most similar counterpart for j. In
- a case of a "perfect match" the *mwSSIM*=1 i.e. indicating the identity of two sets of classes. Negative values of *mwSSIM* would indicate two different sets of classes without any element from one set similar to any element in the other set. In our analysis we only consider *mwSSIM* for different pairs of classifications (diagonal elements of the *mwSSIM* matrix are always 1.0 anyway). The maximum *mwSSIM* = ~1.00 (almost identity!) is attained by 7% of all pairs, strong similarity with *mwSSIM* ≥ 0.60 show 54% of all pairs. The mean value of pairwise *mwSSIM* for all [different] classifications is 0.63. Figure 11 shows
- that all sets of classes are similar to all sets of classes in a pairwise comparison i.e. all pairwise similarity values are greater than the threshold ( $TH_{merge}=0.40$ ) with the minimum mwSSIM=0.53. This is indeed a good result. This allows us to say that the two-stage classification produces similar sets of clusters also when initialized by randomly chosen subsets of the input data.



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Figure 11: Mean weighted similarity, *mwSSIM*, for each of 61 sets of classes to each other. Each set of classes was derived on *minNYR* =30 years of input data. The diagonal elements are not shown because *mwSSIM*=1 of a set of the classes to itself. The matrix is not symmetric: *mwSSIM(k,l)*  $\neq$ *mwSSIM(k,l)* as the sets of classes k and l may have a different number of classes.

We repeat the calculation of *mwSSIM* on 35 and 40 years of data (not shown) in order to make sure that the classification algorithm produces similar sets of classes on larger data volumes as well. When the data volume is set *minNYR*=35 the number of classes varies from 31 to 48 among 61 sets of classes, with minimum mwSSIM = 0.55 and mean mwSSIM = 0.65. On the maximal data volume (40 years) number of classes varies from 35 to 49, with minimum mwSSIM = 0.54 and mean mwSSIM = 0.64. These calculations of mwSSIM on other data volumes only support our previous findings: all pairwise values of

*mwSSIM* are greater than the similarity threshold indicating that our two-stage clustering algorithm applied to randomly chosen data builds sets of similar classes.

- 750 <u>Spatial stability</u>. For testing the stability of the method in space, additionally to the classes on the reference data set  $(2^{\circ}x3^{\circ})$ , two sets of classes were built on the low-resolution  $(4^{\circ}x6^{\circ})$  and on the high-resolution  $(1^{\circ}x1.5^{\circ})$  by resampling the original reanalysis fields to these spatial resolutions. The clustering algorithm was run with the data on each spatial resolution using the same threshold  $TH_{merge}=0.40$ . This poses some restrictions on the interpretation of the results. First: two images on different spatial resolutions derived from the same original image are not necessarily identical (!) in terms of SSIM because they contain
- 755 different amounts of information. The SSIM-value deteriorates with the increasing spatial resolution as the degree of detail in
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the images grows. Following this argument, it would be impossible to build the same set of classes at various spatial resolutions with the same threshold on similarity. However, it can be required that some classes emerge at all spatial resolutions. Examples of such SP-classes are shown in Figure 12 at three spatial resolutions.



- 760 Figure 12: Examples of SP-classes on three spatial resolutions. The middle column shows reference SPs built from the "reference data" (2°x3°, 22x22 grid cells) with their frequencies (%). The left-side column shows corresponding patterns on the low-resolution (4°x6°, 11x11 grid cells), the right-side column on the high-resolution (1°x1.5°, 44x44 grid cells). Both plots for low- and high-resolution counterparts show the SSIM-value to the reference SP-class on top of each plot.
- Figure 12 shows six SP-classes at the original resolution (middle plots) and their counterparts in the low- and high-resolution sets of classes. Please note: the SP-classes are built at each resolution independently and are not just re-sampled copies of the same classes. Therefore, some discrepancy must be tolerated among the classes at different resolutions as they are medoids of independently formed classes. Despite of such discrepancies the SP-classes show essentially the same geopotential anomalies

at all spatial resolutions. Although it is not required, classifications on the three spatial resolutions have 37 classes each. The mean similarity for all 37 SP-classes built on the "reference data" to their counterparts on the low-resolution is 0.53; to their

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mean similarity for all 37 SP-classes built on the "reference data" to their counterparts on the low-resolution is 0.53; to their counterparts on the high-resolution is 0.52. These high numbers (>0.40) indicate the ability of the new clustering algorithm to reproduce similar SP-classes on different spatial resolutions i.e. spatial stability of this algorithm.

# 4.5 Cluster reproduction and representativity

The two-stage classification method uses medoids for representing clusters for the reasons of stability. A medoid of a cluster can be seen as "the representative element" of this cluster i.e. element most similar to all other elements in the cluster (definition of the medoid). Once the cluster is changed (merged with another one by the hierarchical step for example) the medoids are recomputed. Every new attribution of an element to a cluster is done to the most similar medoid (this ensures exclusive attribution of similar elements to clusters). For the final set of classes we demonstrate that the medoids are strongly similar to cluster means (centroids) i.e. cluster medoids effectively represent the mean patterns of their classes. We analyse the set of 37 classes built on the "reference data" and compute for each class the similarity value between its centroid and medoid (Table

- 2). A good representativity is achieved when medoid and centroid of each class are "strongly similar". The Table 2 shows exactly this:  $SSIM(medoid_i, centroid_i) \ge 0.60$  for all classes *i*. If the medoid and the centroid are "strongly similar", it guarantees that there are no or negligibly few "extravagantly" dissimilar members in that class. Otherwise, the mean (centroid) would have lost its similarity to the medoid being distorted by the averaging with dissimilar members. The "strong similarity" between medoids and centroids for all 37 classes was found indicating the very good representability of clusters by their medoids. The
- 785 mean similarity between medoids and centroids over all 37 classes is 0.78; weighted by the class frequency is 0.79. This is a very good result that shows the strong resemblance between medoids and centroids of the clusters and illustrates the representativity of classes by their medoids.

Table 2: Set of 37 SP-classes on "reference data" with  $TH_{merge}=0.40$ : index of Synoptic Pattern (SP), Fraction (Fr) in percent of the class in the "reference data" and the Similarity (SSIM) value between medoid and centroid of the class.

SP	Fr [%]	SSIM									
1	11.6	0.77	11	0.5	0.71	21	0.1	0.67	31	0.2	0.75
2	4.4	0.85	12	2.2	0.79	22	3.9	0.77	32	1.6	0.76
3	4.9	0.81	13	3.3	0.78	23	0.9	0.70	33	3.8	0.84
4	5.2	0.81	14	2.3	0.83	24	1.0	0.76	34	0.9	0.73
5	3.7	0.80	15	5.7	0.80	25	1.0	0.76	35	0.5	0.81
6	8.0	0.79	16	3.7	0.76	26	0.5	0.84	36	1.7	0.76
7	3.7	0.81	17	3.3	0.80	27	6.5	0.76	37	0.3	0.74
8	1.8	0.79	18	2.1	0.82	28	1.5	0.72	-	-	-
9	3.1	0.77	19	2.0	0.74	29	1.1	0.75	-	-	-
10	2.4	0.77	20	0.4	0.73	30	0.3	0.79	-	-	-

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Figure 13 illustrates medoids and centroids for the five most frequent SP-classes. As expected, each medoid has a higher amplitude of anomalies and the corresponding centroid shows essentially the same pattern but with weaker anomalies. The Mean Absolute Difference (the sum of absolute differences between each element in the class and its medoid) between the two shows the highest values at the locations of strong amplitudes in the medoid fields and lower values at locations on "edges"

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of synoptic patterns. This is expectable because the covariance term of SSIM (Eq. 3) penalizes a displacement of anomalies stronger than a mismatch of anomalies' amplitudes i.e. steers the clustering method to prefer correctly placed anomalies over their correctly estimated amplitudes (by a false placement). Figure 13 shows the high similarity between the class medoids and their centroids and indicates that these classes are not "snowballs": although the classes may have many members, they show pronounced and similar (within the class) structural patterns. This illustrates that the clustering method sensitively groups SPpatterns with similar composition of the anomalies into classes using the SSIM as a similarity measure for pairs of geopotential fields.





Figure 13: Medoids (left column), means/centroids (centre column) and their Mean Absolute Difference (right column) for five most frequent SP-classes. Frequency of each SP-class is shown on top of each medoid plot, SSIM between medoid and centroid is shown on the top of each plot of the mean.

#### 5 Weather extremes affiliated with the synoptic classes

We compute maps of exceedance probabilities for two variables - daily near-surface air temperature *tas* and daily total precipitation pr – for each synoptic class using maps of exceedance of 90<sup>th</sup>-percentile for days in corresponding clusters. The computed for each class map of exceedance probability is limited to the area of Germany only as we were able to validate

- 810 these data using data-sources of national observations. Figure 14 shows the maps of exceedance probabilities of 90<sup>th</sup>-percentile for temperature and precipitation affiliated with four exemplary synoptic classes. The class SP5, not a very rare one with occurrence of 3.7% in the data, has no indication to exceptionally warm or wet weather as both maps of exceedance probability remain "empty" (no exceedance). For the class SP2 the map of exceedance probability for precipitation shows a frequent exceedance of 90<sup>th</sup>-percentile everywhere in Germany with a higher probability in the southern region. The class SP35, one of
- the rare classes with only 0.5% of data, appears to be frequently "hot". The class SP29, also a rare one, frequently exhibits warm and wet weather conditions.



Figure 14: Examples of synoptic classes and corresponding maps of exceedance probability for temperature (*tas*) and precipitation 820 (*pr*).

Maps of exceedance probabilities for all classes are shown in supplementary material (Figure S3 - Figure S7). Some clusters show no exceedances of 90th-percentile for either variable (SP3, 5, 9, 14, 17, 37), but some others do. Apart from the type of extreme events, which materialize through persistence of possibly not very rare circulation types (SP 1, 2, 6, 7, 15), there are others that are related to rare circulation patterns. Rare classes (with occurrence of less than 2% in total data) SP 25, 28, 29,

825 30, 34 and 35 are often very warm. Rare classes SP 19, 20, 21, 23, 24, 29, 30, 31, 32, 36 show high probabilities of intense precipitation. Precipitation is an especially "difficult" variable to evaluate in models. Dry/wet biases in models may result from bad physical parameterisations or/and from models disability to reproduce the correct synoptic pattern. Therefore, knowing that a particular synoptic pattern often goes along with strong precipitation, we can check if a model is able to reproduce this pattern or not. This knowledge would help to attribute precipitation errors to errors in models physics or dynamics.

#### 830 6 Statistics and the Jensen-Shannon distance metric for evaluation of CMIP6 historical climate simulations

In Figure 15 we show examples of the three statistics: histogram of class frequencies *HIST*, class-to-class transition matrix *TRANSIT*, and matrix of persistence *PERSIST* of each class for 1,2,..8 days. We chose to present these statistics for only three data sets - the reference and two models - for demonstration purposes. Figure 15a shows the large spread of frequencies of SP-classes that conditions high spread in frequencies of transition matrices (Figure 15b) and persistence matrices (Figure 15c).

- As we suggest using the statistics *HIST, TRANSIT* and *PERSIST* for evaluation of climate models, a question on the robustness of these statistics may arise. We take 40 sub-samples (30 years each) of the original ERA-Interim full data set of 1979-2018 and assign these data to the final 37 synoptic classes. For each statistic we compute the mean and the standard deviation (*sd*) of these 40 re-samples. As a very rough, zeroth-order check of robustness we compare the estimated values in the frequency histograms and the *TRANSIT/PERSIST* matrices with two times their resampling standard deviation. We discuss the results of
- 840 this analysis of robustness in detail in the supplement ("Analysis of the robustness of the estimates for the statistics HIST/TRANSIT/PERSIST").

For evaluation of CMIP6 climate historical simulations, we assign each models output to the set of reference SP-classes and compute the Jensen–Shannon distance (Eq.12) for this model to the reference. As each class is represented by its medoid, the class separation is sharper and the assignment of data samples less ambiguous as compared to the common practices of using

845 centroids. The attribution of each data element to a class is done using SSIM with respect to the class medoids.



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Figure 15: Examples of statistics for the reference data and two CMIP6-models: a) HIST – histogram of frequencies for each SPclass; b) TRANSIT matrices for each pair of SP-classes; where diagonal elements show transition for the same class i.e. persistence, c) PERSISTENCE matrices that show number of events when each SP-class persisted for 1,2, ..8 days (this statistic is shown in absolute values - non-normalized – for better readability).

The Jensen–Shannon distance (*JS*) is computed for the one-dimensional statistics (*HIST*, *HIST*<sub>DJF</sub>, *HIST*<sub>MAM</sub>, *HIST*<sub>JJA</sub>, *HIST*<sub>SON</sub>) as well as for the two-dimensional *TRANSIT*, *PERSIST* between the two probability distributions for each model and the reference. Resulting values of *JS* (Table 3) can be combined to suit objectives of the model evaluation, for example, seasonally separated  $JS(HIST_{DJF})$ ,  $JS(HIST_{MAM})$ ,  $JS(HIST_{JJA})$ ,  $JS(HIST_{SON})$  can be used in evaluating seasonal frequencies of synoptic patterns, JS(PERSIST) for evaluating of the duration of synoptic patterns. In this paper, we equally weight all *JS*s and compute the Mean Jensen-Shannon distance (Table 3). A Jensen-Shannon distance of 0.0 indicates the identity between the model and

the reference. The benchmark for this study: the Mean Jensen-Shannon distance for the alternative reanalysis NCEP1 is 0.034

and can be viewed as the best possible *JS* for a model.

860 **Table 3: CMIP6 Models and their Jensen-Shannon distances (JS). The mean Jensen-Shannon distance (***Mean JS***) is computed for** each model as the mean of its individual *JSs* for each model statistic. The two last rows contain the mean (*MEAN*) and the standard deviation (*STDDEV*) of all *JSs* for the same statistic across 32 CMIP6 models.

N		JS for individual statistics							
Nr	Model name	HIST	<i>HIST</i> <sub>DFJ</sub>	HIST <sub>MAM</sub>	HIS <sub>JJA</sub>	HIST <sub>SON</sub>	TRANSIT	PERSIST	Mean JS
-	ERAINT(ref.reanalysis)	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000
-	NCEP (alt.reanalysis)	0,013	0,017	0,020	0,028	0,021	0,079	0,062	0,034
1	ACCESS-CM2	0,057	0,115	0,065	0,125	0,080	0,165	0,128	0,105
2	AWI-ESM-1-1-LR	0,072	0,097	0,092	0,126	0,114	0,170	0,125	0,114
3	BCC-CSM2-MR	0,061	0,096	0,085	0,140	0,111	0,168	0,122	0,112
4	BCC-ESM1	0,067	0,113	0,106	0,143	0,104	0,171	0,124	0,118
5	CanESM5	0,061	0,124	0,097	0,091	0,096	0,174	0,128	0,110
6	CESM2	0,064	0,093	0,081	0,116	0,101	0,164	0,126	0,107
7	CESM2-FV2	0,079	0,125	0,087	0,138	0,120	0,181	0,136	0,124
8	CESM2-WACCM-FV2	0,074	0,118	0,113	0,151	0,089	0,174	0,132	0,122
9	CMCC-CM2-SR5	0,073	0,111	0,080	0,161	0,100	0,176	0,125	0,118
10	CNRM-CM6-1	0,059	0,105	0,081	0,150	0,088	0,169	0,128	0,111
11	CNRM-ESM2-1	0,043	0,098	0,087	0,119	0,089	0,164	0,126	0,104
12	EC-Earth3	0,054	0,091	0,076	0,137	0,095	0,164	0,120	0,105
13	EC-Earth3-Veg	0,068	0,091	0,081	0,165	0,085	0,170	0,117	0,111
14	FGOALS-f3-L	0,068	0,147	0,104	0,173	0,076	0,170	0,124	0,123
15	FGOALS-g3	0,073	0,141	0,097	0,145	0,081	0,175	0,138	0,121
16	GISS-E2-1-G	0,061	0,127	0,097	0,178	0,093	0,171	0,120	0,121
17	HadGEM3-GC31-LL	0,050	0,108	0,078	0,107	0,086	0,161	0,132	0,103
18	HadGEM3-GC31-MM	0,054	0,090	0,084	0,116	0,077	0,163	0,122	0,101
19	INM-CM4-8	0,071	0,106	0,096	0,170	0,110	0,182	0,136	0,124
20	INM-CM5-0	0,059	0,089	0,095	0,121	0,123	0,166	0,139	0,113
21	IPSL-CM6A-LR	0,065	0,099	0,099	0,181	0,131	0,169	0,132	0,125
22	IPSL-CM6A-LR-INCA	0,056	0,124	0,094	0,176	0,131	0,168	0,136	0,126
23	KACE-1-0-G	0,051	0,090	0,081	0,125	0,079	0,163	0,130	0,103
24	MIROC6	0,063	0,105	0,076	0,136	0,094	0,164	0,136	0,111
25	MPI-ESM-1-2-HAM	0,061	0,104	0,085	0,127	0,104	0,168	0,122	0,110
26	MPI-ESM1-2-HR	0,057	0,105	0,082	0,098	0,088	0,166	0,118	0,102
27	MPI-ESM1-2-LR	0,056	0,103	0,070	0,112	0,085	0,164	0,124	0,102
28	MRI-ESM2-0	0,052	0,090	0,098	0,122	0,079	0,161	0,118	0,103
29	NorESM2-LM	0,077	0,124	0,134	0,175	0,126	0,180	0,142	0,137
30	NorESM2-MM	0,065	0,108	0,087	0,127	0,126	0,172	0,129	0,116
31	TaiESM1	0,060	0,121	0,091	0,119	0,091	0,166	0,134	0,112
32	UKESM1-0-LL	0,060	0,073	0,082	0,139	0,089	0,161	0,128	0,105
-	MEAN (32 models)	0,062	0,107	0,089	0,138	0,098	0,169	0,128	0,113
-	STDDEV(32 models)	0,008	0,016	0,013	0,024	0,017	0,006	0,007	0,009

The mean Jesnsen-Shannon distance, meanJS, indicates how well the respective model captures the synoptic circulation in the

- reference data ERA-Interim (smaller distance better match between the model and the reference, and vice versa). This 865 distance metric can be easily transformed into a quality index using the formulae of Sanderson et al. (2015) and together with quality indices for scalar variables can be used for ranking the climate model simulations and as an evaluation measure. For example, the climate simulation NorESM2-LM seems to underperform all other models (Mean JS=0.137) whereas other models have higher values. Such diagnostic is a useful complement for model evaluation: poor quality scores from evaluation
- 870 of synoptic patterns should be seen as warning prior to analysing scalar variables.

# 7 Conclusions

We presented a new two-stage classification method that uses the Structural Similarity Index Measure (SSIM) for building classifications of synoptic circulation patterns, which are described by geopotential anomaly at the level of 500hPa. This classification method produces a set of well separated, consistent, and representative classes. The algorithm demonstrated its

- 875 robustness against temporal variability and to the spatial resolution of the data. It classifies all input data fields without prefiltering and pre-initialization of classes, it builds structurally different classes with inter-class homogeneity. While explaining the procedure of developing the two-stage classification algorithm, we demonstrated the disadvantage of using the classical clustering algorithm k-means and the MSE as distance measure for cluster building when classifying meteorological fields such as geopotential. We hope this demonstration helps users and developers of classification methods to be careful with
- 880 interpreting their results and to be conscious that some problems (such as "snowballing") may be avoided by simple modifications of the clustering algorithm as illustrated in this paper.

The important strength of the new classification method - its applicability to any region on the globe with no requirements on prior knowledge about weather types at that region. The applicability of our classification method to any region allows evaluation of models quasi-globally as it is done by Cannon (2020) for evaluation of CMIP5 and CMIP6 models: in 6 continental-scale regions (or more).

885

In this paper we describe the method - the recipe - to build a set of synoptic classes. We do not propose an "optimal classification" of synoptic patterns for all purposes. Depending on the purpose of classification, the presented classification method can be extended (from the single variable - geopotential anomaly at 500 hPa) to multiple variables by either targeting the optimization algorithm on a vector of similarity values, or defining the SSIM for vector-valued variables.

890 We apply the new method on the reanalysis data ERA-Interim and built a set of synoptic classes (application of the classification method on other data sets may build other sets of synoptic classes). We demonstrate that separating rare classes may be useful for diagnostics of extreme weather events affiliated with these classes. Here we clearly make use of multiple synoptic classes as only few of them would hamper such attribution.

As an example, we use this set of classes to evaluate the performance of 32 global CMIP6 climate models in the CORDEX-895 EU domain. Model data were attributed to the reference set of classes and statistical parameters (frequency of occurrence of each pattern, frequency of transitions from one pattern to another, persistence of each pattern) were computed for these models. We compared these statistical parameters to the parameters computed on the reference data, calculating the Jensen-Shannon distance metric, and suggest using it for computing a Quality Index (Sanderson et al., 2015) in evaluation routines for climate

- models as an additional diagnostic measure. Using the distance metric proposed in this study would help to avoid 900 misinterpretations in model evaluation such as "right results for wrong reasons" - when a good match of scalar variables (temperature, precipitation etc.) between a model and the reference is achieved but the distance metric for synoptic patterns alerts about poor model performance. We believe, the use of such distance metric for synoptic patterns as proposed in this study would improve evaluating routines currently used for climate models and may give valuable feedback for model developers. We emphasize readers' attention here: the evaluation of model dynamics performed using synoptic classifications
- 905 should not replace but complement (!) existing evaluation routines that use scalar variables and other metrics. Another application of the synoptic classes in the evaluation of climate models is the so-called "weather-pattern-based model evaluation" (Nigro et al., 2011). Surface climate model data are analysed conditionally on each class: this allows for the determination of model errors as a function of synoptic class and can highlight if certain errors occur under some synoptic situation and not others. Alternatively to evaluation, other applications of the two-stage classification are possible. A linkage
- 910 of synoptic classes to extreme weather could be used in improving predictability of the numerical models as it was done by Nguyen-Le and Yamada (2019) who classified anomalous weather patterns associated with heavy rainfall in Thailand and implemented classification results into a Global Spectral Model (GSM) of the Japan Meteorological Agency improving the forecast skill with the lead time up to 3 days. However, we doubt that using synoptic classes in a form of "precursor" for particular weather events would be the best-suited instrument for improving weather forecasts beyond 3 days lead-time.

#### 915 Code and data availability

The ERA-Interim reanalysis data are available <u>https://www.ecmwf.int/en/forecasts/dataset/ecmwf-reanalysis-interim</u>. The NCEP1 reanalysis data are available at <u>https://psl.noaa.gov/data/gridded/data.ncep.reanalysis.html.</u>

The Global Climate Model data used in this study are part of the World Climate Research Programme's (WCRP) 6th Coupled Model Intercomparison Project (CMIP6) open-access data. It was accessed through the Earth System Grid 920 Federation (ESGF; https://esgf-node.llnl.gov/search/cmip6/.

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#### **Competing interests**

925 The authors declare that they have no conflict of interest."

#### **Author Contributions**

KW and CD designed the methods. CD modified the structural similarity index metric SSIM to be applicable to mixed-sign data as presented in this study. KW developed the code in FORTRAN and performed classifications, prepared the manuscript with contributions from all co-authors.

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