



Process-based Estimate of Global-mean Sea-level Changes in the Common Era

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15 **Abstract.** Though the global-mean sea level (GMSL) rose over the twentieth century with a positive contribution from
thermsteric and barystatic (ice sheets and glaciers) sources, driving processes of GMSL changes during the pre-industrial
common era (PCE; 1 – 1850 CE) are largely unknown. Here, the contributions of glacier and ice sheet mass variations and
ocean thermal expansion to GMSL in the common era (1 – 2000 CE) are estimated based on simulations with different physical
models. Although the twentieth-century global-mean thermsteric sea level (GMTSL) is mainly associated with temperature
20 variations in the upper 700 meters (86% in reconstruction and 74±8% in model), GMTSL in the PCE is equally controlled by
temperature changes below 700 meters. GMTSL does not vary more than ± 2 cm during the PCE. GMSL contributions from
the Antarctic and Greenland ice sheets tend to cancel each other during the PCE owing to their differing response to
atmospheric conditions. The uncertainties of sea-level contribution from land-ice mass variations are large, especially over the
first millennium. Despite underestimating the twentieth-century model GMSL, there is a general agreement between the model
25 and reconstructed GMSL in the CE. Although the uncertainties remain large over the first millennium, model simulations point
to glaciers as the dominant source of GMSL changes during the PCE.



1 Introduction

Contemporary global-mean sea level (GMSL) rise is one of the key indicators of Earth's energy imbalance. For instance, the
30 GMSL rise ($1.2 - 1.5 \text{ mm yr}^{-1}$) in the twentieth century (e.g. Hay et al., 2015; Frederikse et al., 2020) is linked to the fact that
nearly 90% of the excessive radiative heating of the climate system, due to greenhouse gas emission, has been stored into the
oceans (e.g. von Schuckmann et al., 2016; Church et al., 2013; Zanna et al., 2019; Meyssignac et al., 2019). The remaining
heat also has an impact on GMSL via altering the mass balance of continental ice (Antarctic and Greenland ice sheets and
glaciers) and changing the global hydrological cycle (Rignot et al., 2011; Shepherd et al., 2012; Church et al., 2013). In addition
35 to those responses to anthropogenic forcing, the internal variability in the coupled climate system is also suggested to explain
a part of the recent GMSL rise, owing to the long memory of the oceans (Ocaña et al., 2016; Gebbie and Huybers 2019).
Hence, the GMSL is integral to changes happening in the climate system in response to both forced and internal variability.
Recent studies have shown that more than 90% of the observed change in GMSL during the last few decades can be explained
solely from ocean thermal expansion and changes in the mass balance of continental ice storage (Leuliette and Miller 2009;
40 Church et al., 2011, 2013; WCRP sea-level budget, 2018; Frederikse et al., 2020). Significant improvements in the
understanding of changes in ocean thermal structure as well as in the continental ice and water storage (e.g. Kjeldsen et al.,
2015; Marzeion et al., 2015; Zanna et al., 2019; Parkes & Marzeion 2018; Humphrey & Gudmundsson 2019) have indeed
resulted in the closure of GMSL budget for the entire twentieth century, pointing to the dominant role of those processes (e.g.
Frederikse et al., 2020).
45 GMSL was about 120 meters below the current level at the last glacial maximum (about 21 ka BP). The subsequent deglaciation
caused the sea level to rise until the mid-Holocene (from ~ 16.5 ka BP to ~ 6 ka BP), followed by smaller amplitude variations
(Lambeck et al., 2014). The centennial-scale GMSL changes seen in proxy-based sea-level reconstructions over the pre-
industrial common era (PCE; 1–1850 CE) do not exceed 10-15 centimeters (Kopp et al., 2016; Kemp et al., 2018; Walker et
al., 2020). For instance, the sea-level reconstructions indicate that the GMSL was in 600 CE ~ 5 -10 cm above the 1850 CE
50 level, and the multi-centennial rates do not exceed $\pm 0.2 \text{ mm yr}^{-1}$ during 1 – 1800 CE (Walker et al., 2020). The GMSL then
rose rapidly by ~ 15 cm after 1850 CE to reach its current level. The rate of GMSL change during the twentieth century is thus
an order of magnitude higher than the multi-centennial rate over the PCE. In this context, the steady and rapid rise in GMSL
since 1850 CE is unprecedented over the last two millennia and largely a result of anthropogenically-driven surface warming
(Kopp et al., 2016; Slangen et al., 2016), which is identified to be unique in terms of rate and spatial coherency (Neukom et
55 al., 2019).
The driving processes of GMSL changes during the PCE are likely the same as the ones responsible for the recent sea-level
rise (e.g. Gregory et al., 2006; Ortega et al., 2013), but their relative contributions are largely unknown. In particular,
considering PCE as a period with weak anthropogenic perturbations allows one to examine the processes controlling GMSL
arising from natural forcing and internal climate variability. In addition to that, the response time of the climate components
60 (ocean, glaciers and ice sheets) and the corresponding GMSL change can be of the order of several centuries (upper ocean and



glaciers) or even millennia (deeps oceans and ice sheets). Consequently, the understanding of current changes in GMSL calls for the analysis of past variability. For example, the cooling anomalies observed in the deep Pacific in the twentieth century were related to the Little Ice Age (LIA) cooling and shown to offset the recent global heat gain in the upper ocean in some regions (Gebbie and Huybers 2019).

65 This paper focuses on the GMSL changes in the PCE by analyzing contributions of major components (ocean thermal expansion and changes in continental ice-mass balance) derived from model experiments. A comparison of model-derived GMSL with proxy-based sea-level estimates (e.g. Kopp et al., 2016) is also provided. The importance of such an exercise is that estimates of different contributing processes to GMSL can provide insights into potential differences in the mechanisms controlling those GMSL changes between different periods in the PCE. Also, as the climate in the PCE is less impacted by the anthropogenic forcing and largely a result of natural variability, the findings place the current anthropogenic warming and sea-level rise in a broader context. Using model simulations, we mainly ask whether the GMSL changes over the CE can be explained within the uncertainty estimates, and what the major sources of uncertainty are? Also, which processes determine the centennial-scale variability seen in the GMSL reconstructions during the PCE?

2 Data and methods

75 GMSL varies either due to changes in the ocean mass (*barystatic* changes; Gregory et al., 2019) which primarily reflects changes in continental ice mass and terrestrial water storage, or by changing the density of the seawater (*steric* changes). The relative contribution of terrestrial water storage to twentieth-century GMSL change is not negligible but predominantly associated with water impoundment in dams (e.g. Frederikse et al., 2020). The contribution is likely much weaker during pre-industrial conditions, and considering the difficulties of estimating precisely the climate-driven terrestrial water storage changes in the past, we do not consider it in this study. Hence, our barystatic estimates are confined to mass balance changes of ice sheets (Antarctic and Greenland) and glaciers. The global-mean *halosteric* sea-level changes due to freshwater input to the ocean can be neglected, as the volume changes due to changes in the ambient salinity would be compensated by the salinity change of the added freshwater (Lowe and Gregory 2006; Gregory et al., 2019). Steric contribution to GMSL is hence reduced to global-mean thermosteric sea level (GMTSL).

85 2.1 Thermosteric sea level

GMTSL is estimated using the 3-D field of ocean temperature and salinity from *last millennium* simulations performed in the framework of the Paleoclimate (Coupled) Modelling Intercomparison Project (PMIP3/CMIP5; Taylor et al., 2012; Braconnot et al., 2011; 2012) and with the LOVECLIM (Goosse et al., 2010; Shi et al 2021) and CESM1 (Otto-Bliesner et al., 2016) models (List of models is given in Table S1). GMTSL is computed as the area-weighted mean of thermosteric levels over the entire ocean surface area (A):



$$GMTSL = \frac{1}{A} \iint_{z=-H}^0 \alpha \Delta\theta \Delta z dA$$

The thermal expansion coefficient (α) at each standard depth level is estimated as:

$$\alpha^\theta = \frac{1}{\vartheta} \left. \frac{\partial \vartheta}{\partial \theta} \right|^{s,p},$$

where ϑ , θ , s , and p are specific volume, potential temperature, absolute salinity and pressure, respectively.

- 95 Computations covered 1 – 2000 CE for LOVECLIM and 850 – 2005 CE for PMIP3/CMIP5 models and CESM1. We used the equation of sea-water state of Jackett and McDougall (1995) for the thermosteric sea-level computations rather than the recent equation (International thermodynamic equation of seawater – 2010) as most of the climate models considered in this study employ the former equation in their formulation. For GMTSL computations using simulations from the PMIP3 *last millennium* experiment (which covers 850 – 1850 CE), we considered mean ocean temperature for the period 1841-1850 CE as the
100 reference field, and for CMIP5 *historical* experiments (1851 – 2005 CE) the chosen reference period is 1851-1860 CE. This selection of consecutive reference periods allows the thermosteric levels from the two experiments, which are discontinuous for some models forbidding the definition of a common reference field for the two runs, to converge over 1841–1860 CE. Thus, all the GMTSL estimates presented in this paper (including LOVECLIM and CESM1) are referenced to 1841-1860 CE mean temperature field, and the computation is performed on the original ocean grid for each model (shown in Table S1).
105 Considering the deep ocean temperature drift and unavailability of control runs to correct it for the PMIP *last millennium* experiments, we restricted the GMTSL computations to the top 700 meters for the PMIP3/CMIP5 models. However, full-depth is considered for LOVECLIM (there is no such climate drift as a long spin-up is performed before starting the simulation in 1 CE) and CESM1 (corresponding control runs available). Since the *GISS-E2-R* simulation performed in PMIP3 showed a visually clear drift during the first 150 years (850 – 1000 CE), even for the top 700m, we have discarded that period for this
110 particular model from ensemble computations.

2.2 Antarctic and Greenland ice sheets

- The contribution from ice sheet mass variations (Antarctic and Greenland) is estimated from the finite-difference ice sheet model *IMAUCE* (de Boer et al., 2014) that has recently contributed to several inter-comparison exercises for future projections of the Greenland ice sheet (Goelzer et al., 2018; 2020) and the Antarctic ice sheet (Seroussi et al., 2019; 2020, Sun et al., 2020; Levermann et al., 2020). For the present application and due to the absence of high-resolution forcing records over the common era, we force the models (configured for Greenland and Antarctica) with surface mass balance (SMB) calculated from a positive-degree-day model (PDDM, Huybrechts and De Wolde 1999) instead of prescribing SMB anomalies. The PDDM is
115 driven by spatially homogenous temperature anomalies relative to a 1960-1989 reference climate obtained either from climate model output or ice core-based temperature reconstructions.



120 **2.2.1 Greenland**

The model for Greenland is set up at 16 km horizontal resolution and uses the shallow ice approximation. Floating ice is not considered and removed when it occurs. In the absence of i) useful constraints on marine-terminating outlet glacier evolution over the common era, ii) applicable forcing and iii) sufficient process understanding, the model does not consider explicit ice-ocean interactions and is driven by SMB forcing alone. The model initialization builds on earlier work and starts from an existing thermodynamically coupled steady state with constant, present-day boundary conditions (IMAUICE1 in Goelzer et al., 2020). From here, the model is relaxed for 10 kyr with a fixed ice temperature to the PDDM SMB forcing with a surface temperature anomaly of zero degrees to produce a nominal initial state for CE simulations.

For simulations forced using PMIP3 GCM outputs, the initial state is assigned to the year 850 CE, and the model is run forward with GCM-derived spatially constant 2-m air temperature anomalies as input to the PDDM. Simulations using output from LOVECLIM are set up similarly but cover the entire CE, with the initial state assigned to CE 1. The same is the case for forcing derived from the last millennium reanalysis data version 2 (LMR; Tardif et al., 2019). The GCM-forced experiments are complemented by simulations driven with spatially constant temperature anomalies derived from an ice core record (Kobashi et al., 2011), spanning 1-2000 CE. To test uncertainty in the initial state, we have introduced two types of perturbations. In the first case, the initial state is perturbed for 500 years before the start of the simulations with a constant temperature offset between -0.5 K and +1.0 K. In the second set of experiments, the model is run to new steady states with temperature offsets between +0.4 K and +0.6 K. The design of these additional experiments implies that the forcing over the CE is identical for the ensemble of simulations, while the model responds differently to the initial perturbations. Note that, to avoid double counting, our simulations do not account for peripheral glaciers weakly connected to the Greenland ice sheet, which are then included in our glacier model (section 2.3).

140 **2.2.2 Antarctic**

The model for Antarctic simulations is run at a 32 km horizontal resolution and uses a combination of shallow ice and shallow shelf approximations, with velocities added over grounded ice to model basal sliding (Bueler and Brown, 2009). We use the Schoof flux boundary condition (Schoof, 2007) at the grounding line with a heuristic rule, following Pollard and DeConto (2012).

Model initialization again builds on an existing present-day ice sheet steady state (IMAUICE2 in Seroussi et al., 2020), which is first relaxed with fixed ice temperature for 10 kyr to the PDDM SMB and zero sub-shelf basal melting. We then continue for another 5 kyr with background sub-shelf basal melt rates estimated for the modelled ice draft using the shelf melt parameterization of Lazeroms et al., (2018) with a thermal forcing based on the World Ocean Atlas (WOA; Garcia et al., 2019) at 400 m depth. Assuming a colder ocean for the first millennium CE, and since we couldn't find stable, steady-state grounding line positions for the original thermal forcing, we introduced an offset of -0.5 degrees to the WOA thermal forcing. The



resulting melt rates are largest in the Amundsen sea embayment and have a maximum of 25 m yr^{-1} at the Pine Island glacier grounding line.

Sub-shelf basal melt rate anomalies for the transient GCM-forced experiments are derived using spatially uniform ocean temperature anomalies averaged over 400–600 meters from models in combination with a high sub-shelf melt sensitivity of $11 \text{ m a}^{-1} \text{ K}^{-1}$ (Jenkins, 1991; Payne et al., 2007; Levermann et al., 2020). An example of this ocean temperature extraction is shown for LOVECLIM (Figure S1). The ice sheet model is also forced with model air temperature anomalies driving the PDDM SMB calculations. Similar to the Greenland simulation, the experiments cover the period from 850 CE onwards, except for LOVECLIM- and LMR-based runs, which cover the entire CE. The GCM-based experiments are complemented by simulations forced with a spatially constant temperature anomaly from a reconstruction based on ice-core records (Stenni et al., 2017), spanning the entire CE. In the absence of a usable proxy record for sub-shelf ocean temperatures, the background sub-shelf basal melt rates are held constant in these experiments. Like Greenland's second set of initial state perturbations, we produce two alternative initial steady states using an air temperature offset of $\pm 0.5 \text{ K}$.

2.3 Glaciers

The glacier volume change estimates are made using the *Open Global Glacier Model* (OGGM, Maussion et al., 2019) version 1.4 (Maussion et al., 2021). OGGM is an open-source model which couples a surface mass balance model with a model of glacier dynamics. OGGM is used to model the annual rate of glacier mass change for 18 of the 19 glaciated regions defined in the Randolph Glacier Inventory (RGI; Pfeffer et al., 2014), with the Antarctic/sub-Antarctic region not modelled due to limitations of the baseline climatology dataset. We used gridded monthly temperature and total precipitation records from the last millennium reanalysis (LMR) data version 2 (Tardif et al., 2019) to drive the model. OGGM determines the temperature and precipitation at each specific glacier location by applying these as anomalies to a reference climate. We have not used PMIP climate model results because of the potential biases in those climate models that would require specific corrections before driving OGGM adequately, and deriving those corrections is out of the scope of the present study (Parkes and Goosse, 2020).

Runs with two different reference climatic conditions are performed: one using CRU TS 4.01 (Climatic Research Unit gridded Time Series 4.01; Harris et al., 2020) mean climate from 1951–1980 (simulation covers the period 1 – 2000 CE), and the other using ERA5 (covers 850 – 2000 CE), which is a recent update of the ERA-interim data as documented in Hersbach et al., (2020). Temperature and precipitation at the reference grid elevation for each of the two datasets are scaled to the glacier surface at each OGGM grid point using a default temperature lapse rate of $-6.5^\circ\text{C} / \text{km}$ between the reference elevation and the glacier surface elevation and a uniform precipitation multiplier of 2.5 (CRU) and 1.6 (ERA5) to account for enhanced precipitation and lateral transport of snow by wind and avalanches in mountainous topography. The model is calibrated to *in-situ* observations provided by the World Glacier Monitoring Service (WGMS, 2020) and then corrected to match regional mass-change estimates by (Hugonnet et al., 2021).



The contributions of positive degree-months for ablation and solid precipitation for accumulation are combined to calculate mass balance, which is used to update glacier geometry annually. In this study, frontal ice ablation of tidewater glaciers is not simulated explicitly. The initial state of mountain glaciers at the beginning of the millennial simulations is unknown: we therefore use the year ~ 2000 state (area from RGI and volume from Farinotti et al., 2019) as initial conditions. The first decades (most glaciers) to centuries (large, flat ice fields) of the simulations are therefore more uncertain and can be considered as a “spin up”. More details of OGGM workflow can be found in Maussion et al. (2019), and further background on the mass balance calculation is available in the precursor to OGGM described in Marzeion et al. (2012).

The simulated volume (V_{tot}) for each region is corrected to remove the below-sea-level component (V_{bsl}), using a fixed proportion by region from Farinotti et al. (2019), and the Sea-level Equivalent (SLE) of the final volume (contribution to GMSL) is calculated as:

$$SLE = \frac{V_{tot} - V_{bsl}}{A_{ocean}} \frac{\rho_{ice}}{\rho_{water}},$$

assuming bulk ice density, $\rho_{ice} = 900 \text{ kg m}^{-3}$, an ocean area of ($A_{ocean} = 3.625 \times 10^8 \text{ km}^2$) and density of freshwater, $\rho_{water} = 1,000 \text{ kg m}^{-3}$.

2.4 Sea-level Reconstruction

In addition to the estimates based on model simulations, proxy-based GMSL reconstructions for the common era from Kopp et al. (2016), Kemp et al. (2018) and Walker et al. (2021) are considered for comparison. As the Walker et al. (2021) reconstruction is the latest update of the proxy-based sea-level database, and the Kemp et al. (2018) and Kopp et al. (2016) curves do not differ much over the CE, we show GMSL from Walker et al. (2021) and Kemp et al. (2018) in our model comparison. We also compare our model GMTSL with the reconstructed GMTSL estimates from Zanna et al. (2019) over 1870 – 2018. Since the reconstructed GMSL from Walker et al. (2021) and Kemp et al. (2018) already incorporated the tide-gauge-based 20th-century GMSL, we do not show those available 20th-century GMSL reconstructions in this paper.

2.5 Uncertainty estimates

As described in the previous sections, our model experiments span two distinct periods (either 1 – 2000 CE or 850 – 2000 CE) depending on the input fields used to run the ice-sheet model or the reference climate used in our glacier model. Our thermosteric estimates also cover these two periods depending on the model (1 – 2000 CE for LOVECLIM and 850 – 2000 for the rest of the models). Hence, we present our model-derived sea-level components and the final GMSL estimates as two groups, namely *EXP-I* (simulations covering 1 – 2000 CE) and *EXP-II* (850 – 2000 CE), primarily based on the period of model simulations. Table 1 summarises details of the input/reference fields used in these two groups. The two groups of simulations allow us to test the sensitivity of our model runs to different input fields and a different initial climate state. In addition to that, uncertainty derived from a “single-model large ensembles” (like the one performed with LOVECLIM GMTSL) provides an opportunity to isolate uncertainty arising solely from internal climate variability, while the uncertainty



from the PMIP models (or PMIP-based ice-sheet simulations; *EXP-II*) additionally represents differences in model physics.
215 Also, the simulations directly driven by reconstructions, like the ice-core based temperature estimates, provide alternative estimates not influenced by climate model potential biases.

2.5.1 glacier uncertainty

To generate an estimate of model uncertainty for the glacier contribution, we combined the impacts of intra-regional and inter-regional uncertainty. It should be noted that, since all samples (regional glacier volume simulations) are taken from a *single*
220 set of OGGM runs with a fixed set of parameters, this does not represent uncertainty in the model setup. It only represents uncertainty based on a) varying confidence in glacier inventory completeness or representativeness and b) OGGM's ability to effectively model ice masses by varying glacier-by-glacier and region-by-region using the applied forcing. Intra-regional uncertainty is estimated with a 'leave X out' method by creating a set of reconstructions of volume for each region using a random sample of 50% of glaciers in the region and scaling the volume time series for the sample to match the total regional
225 volume in 2001 as taken from Farinotti et al. (2019). A spread of 100 independently sampled volume time series is used to determine a time series for regional standard deviation, which is incorporated into the compound uncertainty estimates as described below.

Inter-regional uncertainty is also estimated with a 'leave X out' method by creating a set of global volume reconstructions, each leaving out 3 top-level RGI regions. The contribution of each region is then perturbed according to the regional standard
230 deviation calculated as above. For each region in the sample of regions, a single value is sampled from a normal distribution with mean 0 and standard deviation 1, then the standard deviation time series for the region is multiplied by that single value and added to the regional time series. Perturbing regional time series in this way results in a more realistic range than simply adding (a likely underestimate) or normalised multiplying (a likely overestimate) the independent uncertainty ranges from the intra-regional and inter-regional samples. The sample of perturbed regional time series (with the 3 top-level regions removed)
235 is then added together and scaled to match the total (including all modelled RGI regions) global volume in 2001. We did this for 1000 independently sampled leave-3-out sets of regions and formed the confidence interval for combined intra- and inter-regional uncertainty as the 1-standard deviation.

2.5.2 Uncertainty on rest of the processes

As shown in Table 1, our independent estimates of thermosteric and ice-sheet contributions are limited to less than ten cases
240 and not consistent for these two processes. On the other hand, we have generated 1,000 synthetic curves and derived confidence levels for the glacier sea-level simulations as described in the previous section. To have a consistent set of estimates for thermosteric and ice-sheet contribution, we employed a Monte Carlo method by generating 1,000 realizations of available estimates in each contributing process. Ensemble members are generated by randomly selecting and perturbing one of the available estimates at a time. Specifically, we perturbed the estimate by drawing random numbers (white noise) from a
245 Gaussian distribution using the *a priori* standard deviation (which is taken as the RMSE between the ensemble mean and the



randomly selected estimate) and adding those random numbers to the selected estimate. An additional remark here is that, for
thermsteric estimates from EXP-II for which the computation is restricted to the top 700 meters owing to the deep-layer
temperature drift, we added a *below-700-meter contribution* of 0.85 cm to the *a priori* standard deviation. This deep-layer
contribution is estimated as the mean RMSE between the *full-depth* and *top-700m* GMTSL estimates from the LOVECLIM
250 model over 850 – 2000 CE (see Figure 1). As the sea-level estimate varies over much lower frequencies (as seen in Figure 2,
for example), and the yearly white noise brings unrealistic high-frequency perturbations to the chosen sea-level estimate, we
converted the generated white noise (W) to a red noise (R) using the lag-1 autocorrelation (r) of the chosen estimate before
adding it to the chosen estimate, following Bretherton (2014):

$$R_t = rR_{t-1} + (1 - r^2)^{1/2} W_t$$

255 Since all the estimates are originally referenced to 1841 – 1860 CE, consistent with our thermsteric computations, we scaled
the generated red noise with a scale factor that varies between (0, 1) according to the time-varying difference between the
ensemble mean and the chosen estimate. This scaling ensures that we do not perturb the sea-level time series uniformly in time
but provide weightage for the chosen reference period. In other words, our uncertainty estimates are not *absolute* but relative
to the reference period chosen, being smaller for the reference period by construction. The entire process is repeated to yield
260 a thousand realizations of each contributing component and GMSL, for which all known sources of uncertainty and the spread
among different estimates have been propagated. 1-standard deviation of these large ensembles is shown as the uncertainty of
our central estimates. We compute the rate and budget of GMSL for each ensemble member and subsequently derive the mean
and confidence intervals from the large ensemble.

3 Results

265 3.1 Thermsteric sea level

Figure 1 shows the GMTSL computed over the entire depth (Fig. 1a) and the top 700 meters (Fig. 1b) from the LOVECLIM
model for the CE. Our primary goal here with Figure 1 is to illustrate the relative contribution of the *upper* (top 700 meters)
and *lower* (below 700 meters) layer temperature variations to the total (computed over the entire depth) GMTSL changes over
the last two millennia. As stated in section 2, nearly all of the PMIP simulations exhibit a strong deep-layer temperature drift,
270 and hence we confined our GMTSL computations to the upper layer for those models. Therefore, before describing the GMTSL
variability from PMIP and other models (shown in Fig. 2a), we will examine the extent of deep-layer contribution using
LOVECLIM and derive an uncertainty estimate for the PMIP upper-layer GMTSL, arising from that deep-layer variability.
The LOVECLIM GMTSL estimates, separately for the two layers, indeed show that the contribution of deep-layer variability
may have an equal role in determining the total variability during the PCE, as described below.

275 Over the 1900 – 2000 CE, 86% and 74±8% of the total GMTSL rise is associated with the thermal expansion in the upper 700
m layer of the world oceans as seen in Zanna et al., (2019) and LOVECLIM, respectively (Figure 1). These figures are
consistent with other studies that showed that the ocean heat content changes over the last fifty years are primarily contained



in the upper layers of the world ocean (e.g. Levitus et al., 2012; Church et al., 2013). For instance, total GMTSL rose about 5-6 cm since 1900 CE, and the upper-layer GMTSL shows ~ 4 - 5 cm contribution over the same period (Fig. 1b), as seen in
280 both Zanna et al., (2019) and LOVECLIM. The prominent role of the upper layer in shaping the 20th-century GMTSL change also indicates the absorption of anthropogenic heat in the oceanic upper layers.

However, the relative contribution of the oceanic upper and lower layers to the total GMTSL changes varies significantly over the PCE, as seen in Figure 1b. For instance, the upper layer cooling contributes only half of the total GMTSL decrease during 1500 – 1750 (LIA). A sharp increase in the upper layer GMTSL during 1250 – 1500 was offset by a deep-layer cooling (Fig.
285 1b) and resulted in a weak total GMTSL rise over that period (Fig. 1a). The contribution of the upper layer to the long-term GMTSL fall during 250 – 500 (500 - 750) is about 56% (59%), suggesting that the cooling below 700 meters has an equally important role over those periods (grey curve in Fig. 1b). Note that the uncertainty of lower-layer GMTSL contribution (grey shading in Fig. 1b) is comparatively larger than the uncertainty of upper-layer contribution throughout the last two millennia. The standard deviations of full-depth (Fig. 1a), upper-, and lower-layer (Fig. 1b) GMTSL during 1 – 1850 CE (PCE) are
290 0.62±0.05 cm, 0.42±0.02 cm, 0.57±0.08 cm respectively. All those figures indicate that the deep-layer temperature changes have an equally important role in shaping the total GMTSL variability in the PCE, compared to temperature changes in the upper 700 m of the ocean.

The GMTSL estimates from all the available simulations show that the amplitude of GMTSL changes in the PCE is small compared to the twentieth-century rise (Fig. 1 & 2a). GMTSL does not vary more than ± 2 cm during the PCE (valid for both
295 upper and lower layers). In general, GMTSL from PMIP/CMIP (EXP-II) shows a similar evolution since 850 CE compared to the LOVECLIM, except for a larger uncertainty and a slight underestimation of the twentieth-century rise in CMIP5. The 20th-century GMTSL rise is about 5 cm in reconstruction and LOVECLIM, but ~3 cm in CMIP models (Fig. 2a). Another interesting feature is the short-term episodic falls (notably in 1259, 1453, 1601, 1641, 1809, 1815, 1831) in GMTSL over the last millennium, evident in both LOVECLIM and PMIP simulations (Fig. 2a). These episodic falls in GMTSL result from the
300 reduction of the oceanic heat content due to anomalous radiative forcing triggered by strong volcanic eruptions reported at those times (e.g. Sigl et al., 2015; Ortega et al., 2013).

Figure 2a shows that the GMTSL increased during the first three centuries of the CE (so-called *Roman Warm Period*) and then declined to 700 CE, a period characterized by cold and dry climate conditions, referred to as the *Late Antique Little Ice Age* (Helama et al., 2017). GMTSL further rose about 1 cm toward the *Medieval warm period* (MWP, ~1200 CE) before declining
305 again during the Little Ice Age (LIA). Those centennial-scale changes are also evident in the 250-year rate (*rate* here onwards) of GMTSL (Fig. 3a), as it exhibits positive and negative values over centennial periods, following the “climate epochs” mentioned above. The rate curves are nearly identical for EXP-I and EXP-II over the CE, except over the last two centuries where the rate is comparatively weak for EXP-II (this is expected because the twentieth-century rise is slightly underestimated in EXP-II shown in Fig. 2a). It is also interesting to note, in Figure 3a, that the global-mean surface temperature rate indeed
310 agrees with the GMTSL rate over certain periods (by “agreement” we mean the sign of the rate over multi-centennial periods, for instance, during 0 – 600 CE, 1200 CE – present), but also disagrees during 600 – 1200 CE. The GMTSL (global-mean



surface temperature) rate is well within $\pm 0.1 \text{ mm yr}^{-1}$ ($\pm 0.1 \text{ }^{\circ}\text{C century}^{-1}$) during the PCE, and the rate increases to $\sim 0.15 \text{ mm yr}^{-1}$ ($0.15 \text{ }^{\circ}\text{C century}^{-1}$) during the last two centuries (Fig. 3a).

3.2 Barystatic sea level

315 GMSL changes due to Antarctic mass balance variations over the instrumental period (Church et al., 2013; Frederikse et al.,
2020) and future projections (Moore et al., 2013; Palmer et al., 2020; Seroussi et al., 2020) are highly uncertain. The
uncertainties are also prominent over the PCE, with the uncertainty range (shading around the mean) of our estimate of the
Antarctic ice sheet contribution to sea-level changes (Fig. 2b) and its rate (Fig. 3b) including both positive and negative values
for the majority of the period. The range of probabilities at the beginning of the first millennium in EXP-I (Fig. 2b) indicates
320 either a sea-level fall or rise, depending on the initial state. The central estimate (ensemble mean) of the Antarctic sea-level
contribution, however, shows a long-term fall over the first millennium (1 – 1000 CE) and a reversal in sign further until the
early twentieth century (Fig. 2b). The positive sea-level contribution during the second half of the PCE (1000 – 1900 CE) is
further supported by the PMIP-based simulations (EXP-II). However, the uncertainty is even larger in this case (Fig. 2b). EXP-
II indicates a weak positive mass balance (negative sea-level contribution) during the twentieth century, while the twentieth-
325 century change is nearly zero in EXP-I (Figure 2b).

The inferred uncertainties are also evident in the rate of sea-level change, as seen in Figure 3b. The central estimate of the rate
(from EXP-I and EXP-II) over the entire period is in line with the sea-level or mass balance change described before. The rate
is negative during 1 – 1000 CE and then becomes positive for the rest of the period (Fig. 3b). The twentieth-century decline in
sea level is reflected in the sea-level rate, as the rate decreases towards the end of the period (the rate is still positive as our
330 window of rate computation is 250 years). The surface temperature over Antarctica in the past two millennia (Stenni et al.,
2017) exhibits an inverse relationship to sea level over multi-centennial periods (Fig. 2b). Our experimental design can explain
this relationship as a warmer climate generally enhances precipitation over Antarctica and decreases the GMSL (Frieler et al.,
2015; Medley and Thomas, 2019).

Greenland contribution to GMSL exhibits substantial centennial-scale variability with a positive long-term trend ($\sim 4 \text{ cm rise}$)
335 during 1 – 750 CE, probably in response to the large surface temperature variability over Greenland during this period (Figs.
2c & 3c). Despite considerable uncertainty, the contribution of Greenland ice-sheet mass changes to sea level was probably
well below the current level at the beginning of the common era (Fig. 1c). Figure 3c indeed shows that the sea-level variation
during the 1 - 750 CE (rate varies between $0 - 0.2 \text{ mm yr}^{-1}$) has substantial centennial-scale changes and follows the surface
temperature variations (varies between $\pm 1.5 \text{ }^{\circ}\text{C century}^{-1}$) over the same period. The sea-level decline during 750 – 1850 CE
340 ($\sim 2 \text{ cm}$) is also in line with the surface temperature fall in the same period in two experiments. In general, the sea-level rate is
positive (negative) during the first (second) millennium (Fig. 3c), opposite to those millennial-scale changes seen in Antarctic
contribution to sea level (Figs. 2b & 3b), suggesting a differing response of the two ice sheets to surface temperature changes.
Though the recent warming over Greenland started as early as 1800 CE and temperatures rose by approximately $1 - 2 \text{ }^{\circ}\text{C}$ to
the reference period (1841-1860), no clear sea-level response was observed during this period (Figs. 2c & 3c).



345 Results from OGGM (Fig. 2d) suggest that the GMSL, as a response to global glacier mass balance changes, rose gradually over 1-500 CE (with a sea-level equivalent of ~ 10 cm) and then exhibited a long-term fall until the early twentieth century (SLE ~ 6 cm). There is a positive sea-level contribution (~ 2 cm) during the subsequent decades (1920 – 2000). Note that, the large sea-level contribution over the first few centuries of the CE could be partly a model ‘spin-up’ response (as highlighted by red-dashed line in panel d). Figure 2d indicates that glaciers are the largest source of GMSL changes during the PCE, with an amplitude of associated sea-level variation much larger (2.65 cm standard deviation) over the PCE than contributions from the rest of the sources (Fig. 2). However, the uncertainty is very large over the first millennium. The large millennium-scale variability is also evident in the rate (Fig. 3d). The sea-level trend is positive during 1 – 800 CE (rate is gradually falling from ~ 0.3 mm yr⁻¹ at the beginning of the common era) and negative for the rest of the CE. The millennium-scale variability is robust across the ensemble members as inferred from the narrow uncertainty range enveloped around the ensemble-mean rate (Fig. 3d). As noted in section 2.5, the uncertainty estimate of the glacier contribution doesn’t account for the full range (for instance the single OGGM run restricts to integrate sensitivity of the model parameters and design into the uncertainty estimates), so that the actual uncertainties might be larger than the one shown in this paper. The glacier-driven GMSL changes are similar in both experiments (EXP-I and EXP-II) over their common period.

3.3 Combined estimate vs reconstruction

360 Figure 4a shows the comparison of our model-based GMSL (i.e. the sum of the contributing processes shown in Fig. 2) with the GMSL from reconstructions. An apparent difference between Kemp et al., (2018) and Walker et al., (2020) GMSL reconstructions at the beginning of the common era (green solid and dashed curves) is due to an imposed methodological constraint in the Kemp et al. (2018) reconstruction. In Kemp et al. (2018), the GMSL during -100 – 100 CE is made equal to GMSL over 1600 – 1800 CE to avoid a spurious regional sea-level trend component; however, such a constraint is not employed in Walker et al. (2020) reconstruction shown in Figure 4a. Model GMSL exhibits a broad agreement with reconstructions, despite a few inconsistencies and large uncertainty in the first millennium. Our model GMSL indicates a steady rise of about 5 – 10 cm during the first five centuries of the CE. This rise is in line with Kemp et al., (though the amplitude is smaller in reconstruction). However, Walker et al. (2021) reconstruction shows a nearly steady GMSL over the same period (Fig. 4a). Reconstructed sea level shows a PCE maximum ($\sim 6 - 12$ cm above the 1841 - 1860 CE level) during 370 500 - 700 CE, while the model GMSL shows a sea-level fall during this period, and the PCE maximum in model GMSL (~ 8 cm) appears around 800 CE (Fig. 4a). Both reconstructions and models indicate a long-term decrease in GMSL from 800 CE until the nineteenth century. There is, however, some multi-centennial variability within this long-term fall in reconstructions (for example, the GMSL fall during 1000 – 1250 and a subsequent rise during 1300 – 1500 CE), which is nearly absent in the modelled GMSL. Note that, this multi-centennial variability is prominent in the Kemp et al. (2018) reconstruction but weaker in Walker et al. (2021), who used an expanded set of proxy data in their reconstructions. Additionally, the model GMSL shows $\sim 5-8$ cm GMSL rise in the twentieth century. This is only about half of what is seen in reconstructions and reported elsewhere



(e.g. Church et al., 2013; Hay et al., 2015). Our GMSL estimate from EXP-II shows similar evolution to that from EXP-I from 850 CE onwards (Fig. 4a).

Those salient features of GMSL evolution over the CE are also evident in Figure 4b, which shows a moving 250-year rate for
380 GMSL (model and reconstructions) and global-mean surface temperature. The GMSL trend is positive during 1-500 CE in
both model and reconstructions, and the rate varies between ~ 0.3 and 0 mm yr⁻¹. The model GMSL rate is below zero after
850 CE, ranging between $-0.2 - 0$ mm yr⁻¹. This negative rate corresponds to the long-term GMSL fall during the first part of
the last millennium (Fig. 4a). The rate then becomes slightly positive by the end of the nineteenth century. The sea-level rate
from reconstructions (either Walker et al., 2021 or Kemp et al., 2018) lies within the uncertainty of the model rate over 1 –
385 600 and 850 – 1800 CE. However, the rate is clearly out of the model uncertainty range during 600 – 800 and post 1800 CE.
The disagreement over 600 – 800 CE between the model and reconstruction results from inconsistent GMSL variability
between the model and reconstruction during 500 – 700 CE, as seen in Figure 4a. Compared to reconstructions, the weak
twentieth-century GMSL rise in the model is consistent with a too weak model GMSL rate (0.1 mm yr⁻¹ compared to 0.6 mm
yr⁻¹ in reconstruction by the end of the nineteenth century; Fig. 4b).

390 The ensemble-mean thermosteric and barystatic (sum of ice-sheet and glacier contribution) sea level over the CE is separately
shown in Figure 5a. In general, the thermosteric changes are weaker than barystatic changes during the PCE. However, the
twentieth-century model GMSL change is mostly contributed by thermosteric sea level rise. Also, while the barystatic changes
happens mostly over millennial time scales, multi-decadal-to-centennial changes are seen in thermosteric variability (Fig. 5a).
As noted in section 3.1, the multi-centennial GMTSL changes are linked to those regional climate epochs during the PCE. For
395 example, the GMTSL was down to the reference level (1840-1860 CE level) during 600 CE (Late Antique Little Ice Age –
LALIA) and then rose by $\sim 1-2$ cm to Medieval Warm Period (MWP). GMTSL fell further during the Little Ice Age (LIA)
and rebound quickly during the Current Warm Period (CWP; post-1800). The respective contribution of different processes in
shaping the GMSL (known as *GMSL budget*) during those climate epochs are shown in Figure 5b (1 – 600 CE), 5c (600 –
1200 CE), 5d (1200 – 1800 CE) and 5e (1800 – 2000 CE). Note that, as our GMSL estimates from EXP-II agrees well with
400 EXP-I over their overlapping period (850 - 2000 CE), we show this analysis only for EXP-I.

Figures 5b-e illustrate that different processes contribute variable amounts (in terms of both rate and sign) to GMSL change in
different periods with glaciers as the dominant source throughout the PCE. For instance, the GMSL rise during the first 600
years and GMSL fall during 1200 – 1800 CE are mostly driven by glacier mass-balance changes (Figs. 5b&5d). Figure 5c also
shows that the weak GMSL change during 600 – 1200 CE (Fig. 4a) is a result of opposing contributions from its components.
405 While the thermosteric and Greenland ice sheet exhibit a positive contribution (i.e. GMSL rise), the GMSL associated with
changes in glaciers and Antarctic ice sheet show a negative contribution (Figure 5c), and resulting a net GMSL change which
is nearly zero over this period (Fig. 4a). Note that the uncertainties are very large for all the components except the glacier
contribution during this period. All the GMSL components except Antarctic ice sheet have a positive contribution to net GMSL
fall during 1200-1800 CE. As we have seen in Figure 5a, the model GMSL rise since 1800 CE is mostly linked to thermosteric



410 rise with very weak contribution from barystatic sea-level components (Fig. 5e). Figures 5b-e indicates that the changes in
GMSL centennial rate (Fig. 4b) could be due to the fact that the respective contributions to GMSL vary over such time scales.

4 Discussion and conclusions

4.1 GMSL in the last two centuries

From instrumental records and models, it is virtually certain that the GMSL rose during the twentieth century with a mean rate
415 of $\sim 1.2 - 1.5 \text{ mm yr}^{-1}$ (e.g. Hay et al., 2015; Frederikse et al., 2020). The barystatic rise (about 1 mm yr^{-1} including the terrestrial
water storage contribution, which is $\sim -0.21 \text{ mm yr}^{-1}$) is about twice the thermosteric contribution ($\sim -0.52 \text{ mm yr}^{-1}$) during 1900
– 2018 CE (Frederikse et al., 2020; Zanna et al., 2019). Though our model-based GMTSL estimates over the twentieth century
are consistent with those observation-based estimates (Fig. 1), there is an apparent underestimation of twentieth-century
barystatic changes in our model simulations. For instance, a recent GMSL closure analysis by Frederikse et al., (2020) showed
420 that glaciers are the largest source of the twentieth-century GMSL rise (contributing about 70% of the net barystatic rise and
 $\sim 46\%$ of the GMSL rise). Similar rates of glacier mass loss over the last century are also reported in earlier studies (e.g.
Leclercq et al., 2011; Marzeion et al., 2015; Malles and Marzeion 2021).

There are some notable differences between the formulation of our model-based estimates covering the entire CE and other
estimates (some of which are mentioned above) focussed on the 20thC barystatic GMSL rise. For example, Frederikse et al.,
425 (2020) accounted for the GMSL contribution from missing and disappeared glaciers (Parkes & Marzeion, 2018) and assumed
a constant positive rate of Antarctic mass loss ($0.05 \pm 0.04 \text{ mm yr}^{-1}$) before the satellite era. Such inputs are absent in our
model simulations. Additionally, our glacier model (OGGM) has been initialized using 20thC global glacier geometry with
climate variables extracted from LMR. Assuming that the glacier geometry at the beginning of the CE is similar to the recent
geometry may not be optimal, but we have no estimate at that time, and the drift from those initial conditions may affect the
430 simulated 20thC glacier volumes. This is particularly an issue owing to the sizeable long-term glacier mass loss during the first
millennium, as seen in Figure 2d. So, attaining the right volume at the end of the PCE could be challenging if the presumed
initial volumes were originally much different than the prescribed volume. Large uncertainties remain about the configuration
and mass trend of both ice sheets at the onset of the PCE and their subsequent climate forcing and evolution. We have
characterised this uncertainty using a wide range of initial conditions and climate forcing options in our modelling (section
435 2.2). The resulting ice-sheet simulations over the PCE represent an attempt to provide physically based ice sheet changes,
complementing the other sea-level components. Further work should focus on better constraining the climate forcing
specifically important for ice-sheet changes and developing paleo data that can inform about ice sheet evolution over the PCE.
Despite those limitations, our model-based estimates provide some insights on the GMSL variability in the PCE, as discussed
below.



440 4.2 Barystatic and thermosteric GMSL in the PCE

The GMTSL rise as a response to industrial climate warming started in the mid-nineteenth century in LOVECLIM (Fig. 1, 2a), following the global-mean surface temperature curve, but there is indeed a lag of nearly half of a century in the PMIP ensemble mean (Fig. 2a) and probably in reconstruction (Zanna et al., 2019; Fig. 1). This lag could be one of the reasons for a relatively weak 20thC GMTSL rise in PMIP models. The relatively weak ocean thermal expansion in PMIP could have a link
445 with the strong volcanic eruption of Krakatoa in 1883, as reported before in Gleckler et al., (2006), and possibly those eruptions earlier in the nineteenth century (See S2). LOVECLIM is able to capture those episodic GMTSL falls in response to strong volcanic eruptions over the last millennium. However, it seems that the impact of the 19th-century volcanos is weaker than some earlier ones in LOVECLIM (Fig. 1). LOVECLIM is a model of intermediate complexity, and the ocean's response to volcanically-induced aerosol cooling in the background of anthropogenically-induced warming might be more complex, and
450 a correct representation of ocean thermal response would have a strong dependency on model physics and experimental design. Though the GMSL rose over the 20thC with positive contributions from major sources, as shown in this study (except a weak negative sea-level contribution of Antarctic in EXP-II) and elsewhere, the individual contributions to GMSL in the PCE varied in sign and magnitude depending on the period considered (Fig. 4c). Barystatic sea level dominates the GMSL variations throughout the PCE, with the largest (least) contribution from glaciers (Antarctica). This result is, in fact, identical to the
455 relative contributions over the 20thC (e.g. Frederikse et al., 2020). The amplitude of sea-level change due to glacier mass balance changes in the PCE (2.8 ± 0.3 cm standard deviation; Fig. 2d) is indeed remarkable. Despite considerable uncertainty, the change is larger during the first millennium, which probably indicates relatively high glacier surface mass balance sensitivity to initial glacier size and surface temperature changes.

The glacier contributions to sea-level change have a broad association with the long-term global-mean surface temperature
460 evolution, as seen in Figure 2 (although glacier SMB is locally-driven, global-mean surface temperature can be an indicator of changes happening on a global scale for longer time scales). For example, the global-mean surface temperature cooling during 1000 – 1800 CE is associated with a worldwide net glacier advance and a corresponding GMSL decrease (Figs. 2d & 3d). A similar association of GMSL and regional surface temperature is also evident for Greenland and Antarctica (Fig. 2b, c & Fig. 3b, c). In the context of semi-empirical sea-level models (e.g. Oerlemans, 1989; Grinsted et al., 2010; Jevrejeva et al., 2009;
465 Kemp et al., 2011), those millennium-scale GMSL components presented in this paper, combined with regional and global surface temperature, may potentially be helpful to resolve semi-empirical constants and response periods in a better way and can lead to useful hindcasts and projections.

On the other hand, thermosteric sea level varies not more than ± 2 cm during the entire PCE (0.62 ± 0.05 cm standard deviation; Fig. 1 & 2a). Then, the GMTSL rose by $\sim 4 - 6$ cm during 1850 – 2000 CE which is clearly an unprecedented rate of ocean
470 heat content increase over the last two millennia. A weak GMTSL variability over the PCE seen in our experiments also provides an internal consistency, i.e. it supports our finding that barystatic changes contribute a large part of the GMSL variability in the PCE. Considering PCE as a period free from major anthropogenic emission and the corresponding weak



475 GMTSL (and global-mean surface temperature) variability in this period (compared to post-1850 warming) suggests that centennial-scale ocean heat-content changes during the PCE, as a response to natural climate variability, are small. It also further supports the notions that recent changes are exceptional in the context of the past centuries and that the oceans have absorbed over 90% of the anthropogenic heat during the current climate warming (e.g. Church et al., 2011b).

4.3 GMSL centennial changes in the PCE and implications

480 However, the model and reconstruction show some centennial-scale GMSL variability in the PCE (Fig. 4a). For example, GMSL varies up to 5 - 10 cm during 1 – 500 CE or 1300 – 1800 CE, and those figures are nearly half of the observed GMSL change over the twentieth century. Those GMSL centennial changes over the PCE could primarily result from the slow and integrated response of sea-level components to surface perturbations and reflect the long-term persistence of oceanic thermal field and long response periods of barystatic components. Our results also suggest that some of those centennial-scale variabilities are comparable to the 20thC GMSL rise, for example, the sea-level change associated with Greenland variability during 1 – 500 CE (Fig. 2c). Hence, it indicates that the twentieth-century GMSL rise may include response to such natural variations. The offset of recent anthropogenic ocean warming by deep-layer cooling originated from LIA in the Pacific, as reported by Gebbie and Huybers (2019), is an example. We suggest that a similar influence of past variability can also be expected for barystatic sea level owing to its long response time scales, so recent GMSL change might be linked to variability in the past. The integration of climate forcing can be manifested as lower-frequency change in the ocean, which can partly be misinterpreted as trends associated with deterministic forcing as reported earlier in Ocaña et al. (2016). However, with the current set of simulations and analyses, it is hard to make firm conclusions on these aspects. Resolving the response time scales empirically and dedicated sensitivity experiments can provide more insights.

490 Although some earlier studies have discussed GMSL changes in the common era, either based on proxy-based reconstructions or semi-empirical methods (Kemp et al., 2011, 2018; Kopp et al., 2016; Grinstead et al., 2010; Walker et al., 2021), no attempt has been made to describe it using process-based modelling. Our model-based estimates are broadly consistent with the GMSL reconstruction from earlier studies, despite a few disagreements combined with large uncertainties in the first millennium. For example, our results suggest that the GMSL doesn't vary more than ± 0.1 m during the PCE, a result consistent with Kopp et al., (2016), Kemp et al., (2018) and Walker et al., (2021) GMSL reconstructions. Our results also suggest that the GMSL generally rose over 1 – 500 CE, and there has been a long-term decline during 1000 – 1800 CE, an evolution consistent with the long-term global-mean surface temperature cooling in the PCE (Fig. 4b), as noted earlier by Kemp et al. (2011) and Kopp et al. (2016). However, as seen in our model, a pause in the generally rising GMSL around 600 CE is inconsistent with the GMSL reconstructions (see Figs. 4a, b). This inconsistency can be traced to the centennial-scale sea-level drop associated with thermosteric and Greenland contributions over the same period, as seen in Figure 2. Though both the global and Greenland surface temperature variability seem to control it (Figs. 2a&2c), it is difficult to make definitive conclusions due to the large uncertainty during the first millennium (especially for sea level associated with Greenland and glaciers). Our results also quantify the current state of uncertainties in the individual contributions which are particularly large for barystatic components



over the first millennium. Challenges in incorporating the impact of the ocean on marine ice sheets (both because of incomplete knowledge of ocean changes and of ice sheet dynamical response to those changes) are a serious limitation and a potentially major source of uncertainty. Additionally, the challenges in initializing the model with the right climate conditions at the beginning of the common era and reconciling the inherent uncertainties in the model input fields also remain to be addressed in detail.

510



Code and Data availability: All model outputs discussed in this paper and analysis scripts are available on request from the corresponding author.

515 **Author contribution:** GN and HG¹ designed the study. GN analysed the data and prepared the manuscript. Ice sheet simulations were performed by HG³. Glacier simulations were performed by DP and FM. All authors contributed to discussions and writing of the manuscript.



Acknowledgements. This work was supported by Fonds National de la Recherche Scientifique (F.R.S.-FNRS-Belgium) in the framework of the project “Evaluating simulated centennial climate variability over the past millennium using global glacier
520 modelling” (grant agreement PDR T.0028.18). Hugues Goosse is Research Director within the F.R.S.-FNRS. We acknowledge the World Climate Research Programme’s Working Group on Coupled Modelling, which is responsible for CMIP, and we thank the climate modelling groups for producing and making available their model output. For CMIP, the US Department of Energy’s Program for Climate Model Diagnosis and Intercomparison provides coordinating support and led the development of software infrastructure in partnership with the Global Organization for Earth System Science Portals. We thank Dr Jennifer
525 Walker for providing reconstructed sea-level data on request. Computational resources have been provided by the supercomputing facilities of the Université catholique de Louvain (CISM/UCL) and the Consortium des Equipements de Calcul Intensif en Fédération Wallonie Bruxelles (CECI) funded by the Fond de la Recherche Scientifique de Belgique (F.R.S.-FNRS) under convention 2.5020.11. Ice sheet simulations were performed on resources provided by UNINETT Sigma2 - the
530 National Infrastructure for High Performance Computing and Data Storage in Norway through projects NN8006K, NN9560K, NS5011K, NS8006K and NS9560K. Heiko Goelzer acknowledges support from the Research Council of Norway through projects 270061, 295046 and 324639. FM acknowledges support from the Austrian Science Fund (FWF) grant P30256.



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Experiment	Thermosteric	Antarctic	Greenland	Glacier
EXP-I (1-2000 CE)	LOVECLIM (Goosse et al., 2010)	IMAUICE (de Boer et al., 2014)	IMAUICE	OGGM (Maussion et al., 2019)
	10 members (T_o, S)	Stenni '17 (1) LMR (1) LOVECLIM (1) (T_s)	Kobashi '11 (1) LMR (1) LOVECLIM (1) (T_s)	LMR, CRU (1) (T_s, P)
EXP-II (850-2000 CE)	PMIP3/CMIP5 (7) CESM1 (1) (T_o, S)	IMAUICE	IMAUICE	OGGM
		PMIP3/CMIP5 (7) LOVECLIM (1) CESM1 (1) (T_o, T_s)	PMIP3/CMIP5 (7) LOVECLIM (1) CESM1 (1) (T_s)	LMR, ERA5 (1) (T_s, P)

Table 1: Details of the two groups of model experiments presented in this study. The columns are split into two rows for the barystatic components for EXP-I and EXP-II, highlighting the physical model used (top row) and the input used to run the model (bottom row). The numbers in brackets show the number of independent simulations made either using different models (e.g. PMIP model simulations) or based on the input field given to the physical model (ice-sheet/glacier model run with different input fields) for each component. Abbreviations are: T_o - Ocean Temperature, S - Ocean salinity, T_s - Surface Temperature, P - Precipitation, Stenni '17 - Stenni et al., 2017, LMR - Last Millennium Reanalysis, Tardif et al., 2019, Kobashi '11 - Kobashi et al., 2011, CRU - Climatic Research Unit gridded Time Series v-4.01 (Harris et al., 2020), PMIP3/CMIP5 - Paleoclimate/Coupled Model Intercomparison Project (Taylor et al., 2012; Braconnot et al., 2012), CESM1 - Community Earth System Model (Otto-Bliesner et al., 2016), ERA5 - ECMWF atmospheric reanalysis - v5 (Hersbach et al., 2020).

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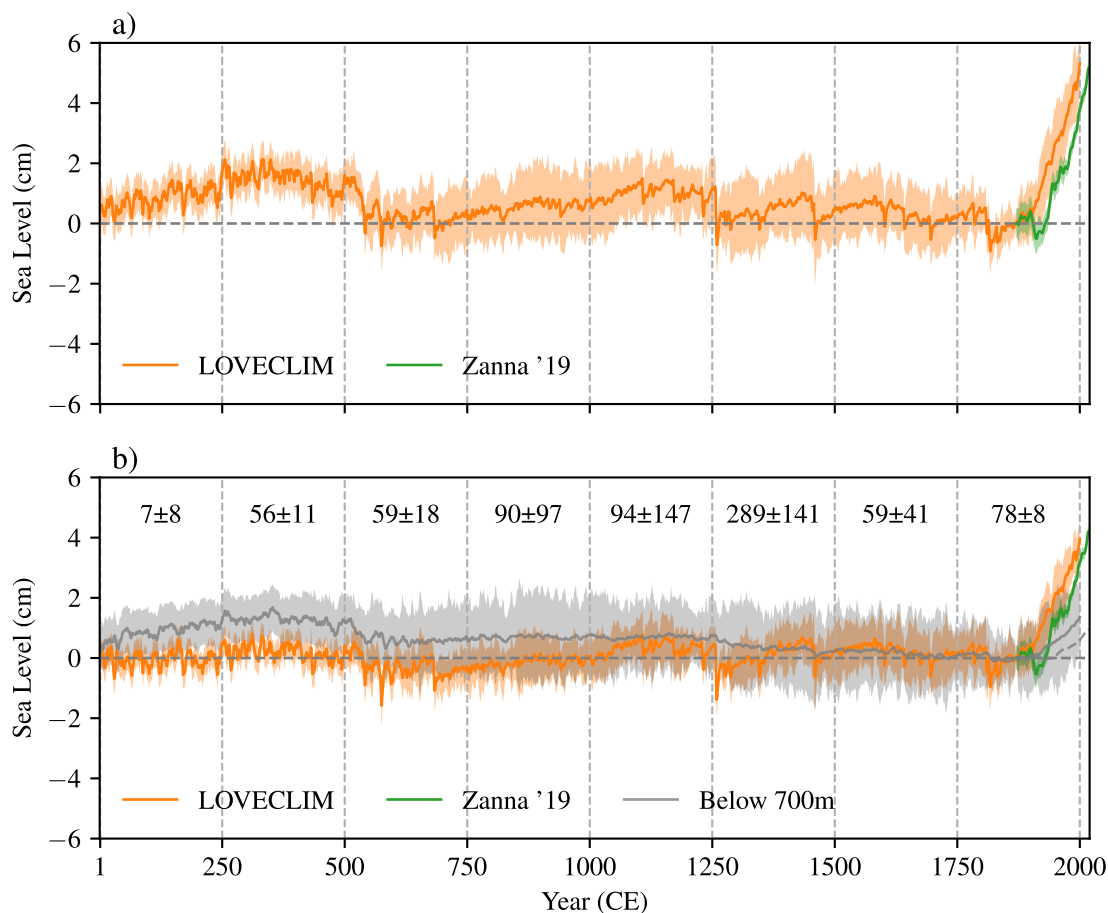
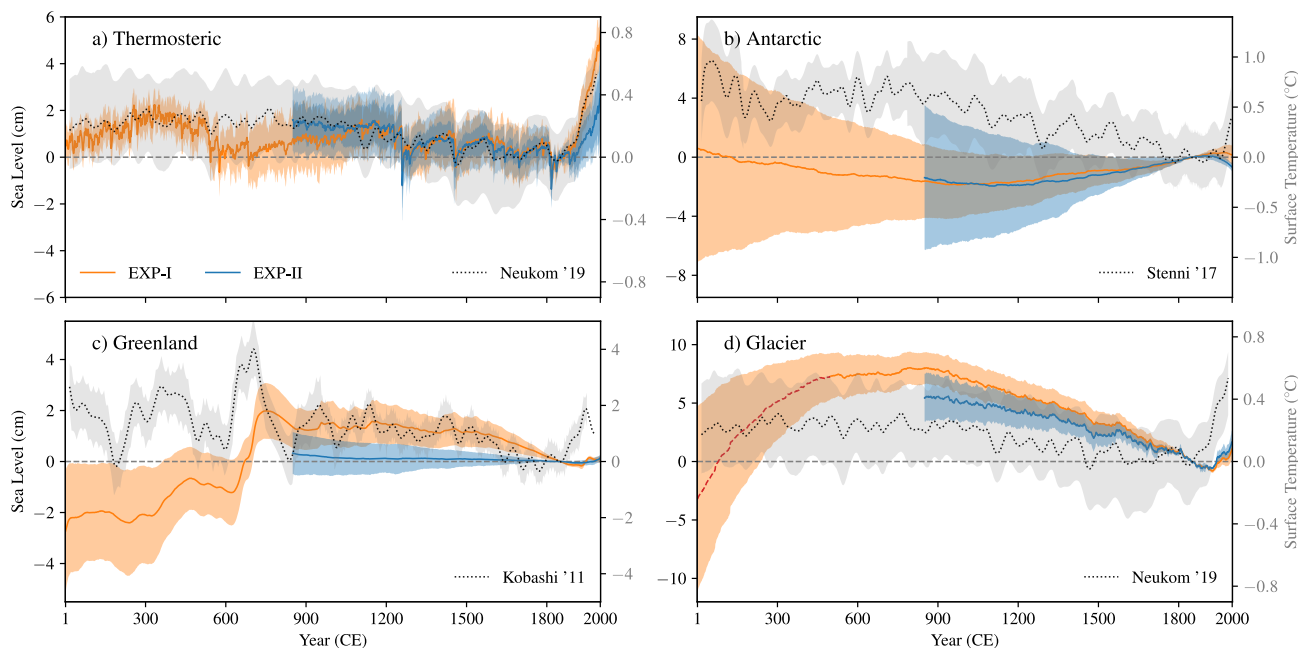


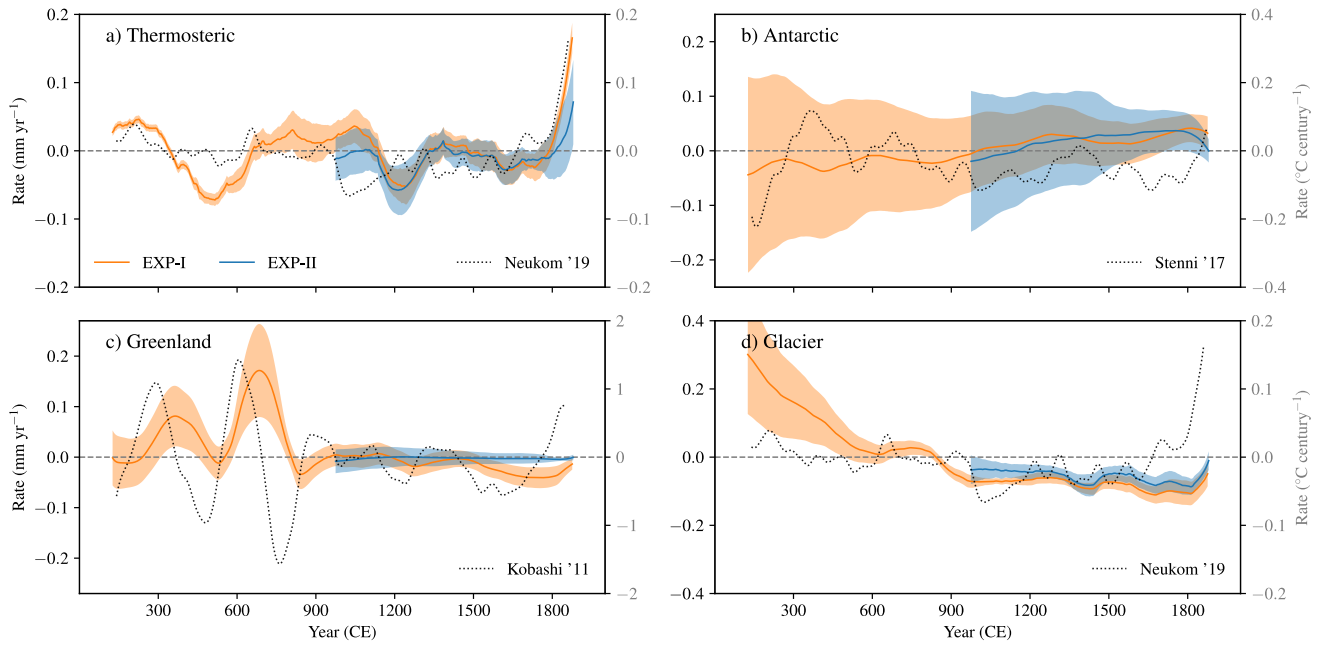
Figure 1: Ensemble-mean global thermosteric sea level estimated using LOVECLIM climate model simulations (orange; 1-2000 CE) and Zanna et al., (2019) reconstruction (blue; 1870 - 2018) for full depth (a) and top 700m (b). Grey curves in the lower panel show the thermosteric level associated with variability below 700 meters (i.e. the difference between “full depth” and “top 700 m” thermosteric sea level) for both LOVECLIM (solid) and Zanna et al. (dashed). All curves are referenced to 1870 CE (when the reconstruction begins), and the shading indicates the 1- σ confidence level of the ensemble-mean curve. The percentage contribution of change in the top 700 meters thermosteric level to that of the full depth, estimated over chunks of 250-year periods (vertical dashed lines), is shown on the bottom panel. The estimated 1900 – 2000 CE contribution of the upper 700 m for Zanna et al. (LOVECLIM) is 86% (74 \pm 8%).

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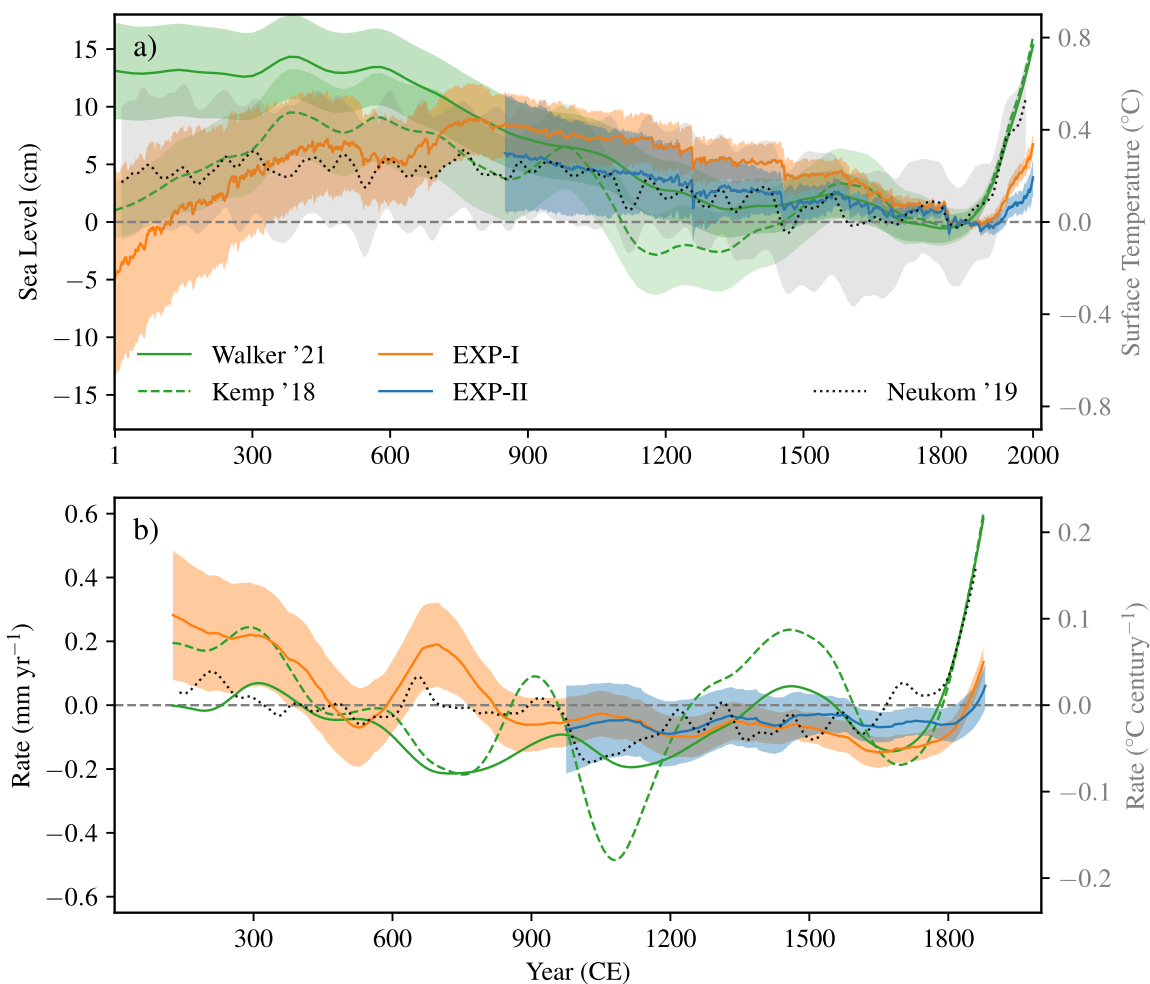
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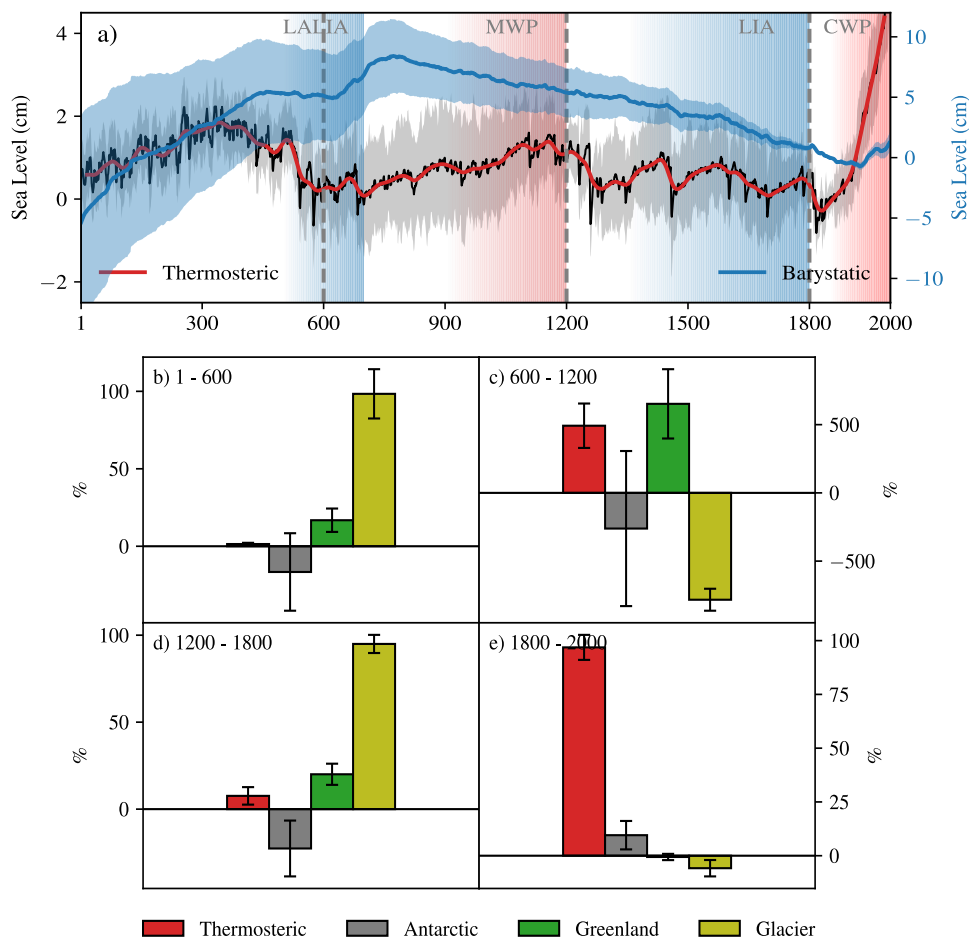
725 **Figure 2: Contributing components to GMSL. a) thermosteric b) Antarctic ice sheet mass changes c) Greenland ice sheet mass**
changes, and d) Glaciers mass changes. Orange (EXP-I) and blue (EXP-II) curves represent the two sets of model simulations used
in this study (see table 1). Global-mean surface temperature from Neukom et al., 2019 (a, d) and regional surface temperature over
Antarctica (b; Stenni et al., 2017) and Greenland (c; Kobashi et al., 2011) are shown as dotted grey lines. Shading around sea-level
curves and Greenland surface temperature indicates 1- σ confidence level of the ensemble mean, and the shading of global-mean
surface temperature (Antarctic surface temperature) shows a 95% confidence level (2RMSE of the ensemble mean). Light blue
shading of EXP-II thermosteric sea level (panel a) indicates additional source of uncertainty arising from temperature changes below
730 **700 meters (see text and Figure 1). Glacier contribution during 1 – 500 CE (EXP-I) is shown with dotted line to indicate the**
uncertainty related to model initialisation (see section 2.3). All the curves are anomalies to 1841-1860 mean.



735 **Figure 3: 250-year rate of sea level for each of the components shown in Figure 2. a) thermosteric b) Antarctic ice sheet mass balance c) Greenland ice sheet mass balance and d) Glaciers mass balance. 250-year rate of global (a, d) and regional surface temperature is also shown (dotted grey lines). Shading around sea-level rates indicates 1- σ confidence level of the ensemble mean curve.**



740 **Figure 4: a) Ensemble mean GMSL curve estimated as the sum of the contributing processes, from EXP-I (orange) and EXP-II (blue). Proxy-based GMSL reconstruction from Walker et al. (2021; solid green), Kemp et al. (2018; dashed green), and global-mean surface temperature from Neukom et al. (2019; dotted grey) are also shown. b) 250-year rate of GMSL and global-mean surface temperature curves shown in (a). Shading in (a) and (b) indicates 1- σ confidence level of the ensemble mean curve except for global-mean surface temperature, for which the 95% confidence level is shown.**



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Figure 5: a) Ensemble-mean global-mean thermosteric (black) and barystatic (i.e. the sum of Antarctic, Greenland and glacier contribution; blue) sea level with their 1-sigma uncertainty level. A 31-year smoothed thermosteric sea level is also shown (red). Note that the scale of the thermosteric sea level is adjusted (compared to Figure 2a) to more visualize the changes during the PCE. Since the amplitude of barystatic changes are typically two-to-three times larger than thermosteric changes over the PCE, the barystatic levels is shown in a different scale (right). We defined four time-periods in the CE (1 – 600, 600 – 1200, 1200 – 1800 and 1800 – 2000) based on major shifts seen in the global-mean thermosteric sea level. Those periods also mark the major sub-millennial climate epochs reported in the CE (The Late Antique Little Ice Age: LALIA (~ 600-700), The medieval warm period: MWP (~ 900 – 1300), The little ice age: LIA (~ 1300 – 1800) and the current warming period: CWP (post-1800)). The respective contribution of thermosteric, ice-sheet and glacier mass-balance changes to model GMSL is estimated for these four periods and shown in panel b (1 – 600), c (600 – 1200), d (1200 – 1800) and e (1800 – 2000). Percentage contribution is calculated by a linear regression method and the error bar represents the 1- σ standard deviation of the contribution across the large ensemble.