

Relating Climate Sensitivity Indices to projection uncertainty

Benjamin Sanderson^{1,2}

¹CERFACS, Toulouse, France

²NCAR, Boulder CO, USA

Correspondence: Benjamin Sanderson (sanderson@cerfacs.fr)

Abstract. Can we summarize uncertainties in global response to greenhouse gas forcing with a single number? Here we assess the degree to which traditional metrics are related to future warming indices using an ensemble of simple climate models together with results from CMIP5 and CMIP6. We consider Effective Climate Sensitivity (EffCS), Transient Climate Response at CO₂ quadrupling (T140) and a proposed simple metric of temperature change 140 years after a quadrupling of carbon dioxide (A140). In a perfectly equilibrated model, future temperatures under RCP(Representative Concentration Pathway)8.5 are almost perfectly described by T140, whereas in a mitigation scenario such as RCP2.6, both ECS and T140 are found to be poor predictors of 21st century warming, and future temperatures are better correlated with A140. However, we show that T140 and EffCS calculated in full CMIP simulations are subject to errors arising from control model drift and internal variability. Simulating these factors in the simple model leads to greater error in the measured value of T140 than for EffCS. As such, if starting from a non-equilibrated state, measured values of Effective Climate Sensitivity can be better correlated with true TCR than measured values of TCR itself. We propose that this could be an explanatory factor in the previously noted surprising result that EffCS is a better predictor than TCR of future transient warming under RCP8.5.

Introduction

Summarizing the response of the Earth System to anthropogenic forcings with metrics has long been practised as a way to illustrate uncertainty in Earth system response to greenhouse gases. For example, the concept of the Equilibrium Climate Sensitivity (ECS), the equilibrium global mean temperature increase which would be observed in response to a doubling of atmospheric carbon dioxide concentrations (Hansen et al., 1984) has existed for over 50 years (Charney et al., 1979) and significant amount of literature has been devoted to constraining its value (Knutti et al., 2017).

The Earth system responds to a step-change in forcing on timescales ranging from days to millennia (Knutti and Rugenstein, 2015), so an ‘Effective Climate Sensitivity’ (EffCS hereon) is often used as a proxy for decadal to centennial feedbacks. EffCS is generally calculated in a coupled atmosphere-ocean model from the output of the ‘abrupt4xCO2’ simulation, a standard experiment in which CO₂ concentrations are quadrupled instantaneously from pre-industrial levels and the model is allowed to evolve (Gregory et al., 2004).

EffCS is calculated by assuming that a model is associated with a single feedback parameter (i.e. a rate of change of top of atmosphere radiative flux per unit surface temperature increase), allowing the equilibrium temperature response to a step change forcing to be predicted by linear extrapolation (we refer to this approach henceforth as the Constant Feedback (CF))

approximation, with EffCS referring to the estimate of ECS made using this approach). Another metric, the Transient Climate Response at CO₂ doubling (TCR) or quadrupling (T140) is calculated from an ‘1pctCO₂’ idealized experiment in which CO₂ concentrations are increased by 1 percent each year, starting from a pre-industrial state, resulting in linearly increasing forcing.

30 Although it was generally assumed that TCR would be a better predictor of transient warming under a high emissions scenario such as RCP8.5 (Riahi et al., 2011), a complication has arisen due to the fact that EffCS seems to be better correlated than TCR with 21st Century warming from present day levels under a business-as-usual scenario (Grose et al., 2018). The reason for this is not yet well understood given the radiative pathway in RCP8.5 leading up to 2100 is relatively similar to that of the 1 percent annual increase experiment used to measure T140. Furthermore, neither EffCS nor TCR is well correlated with
35 end of century temperatures in a mitigation scenario (Grose et al., 2018) such as RCP2.6 (Van Vuuren et al., 2011), which calls in to question the relevance of such summary metrics in the discussion of mitigation adaptations.

Similarly, a number of studies have shown that the EffCS approximation does not well describe the true equilibrium behaviour of most models (Knutti et al., 2017). When GCM abrupt-4xCO₂ simulations are continued for thousands of years, many are found to deviate significantly from the linear trend-line one would fit to a 150 year simulation (Andrews et al., 2015;
40 Knutti et al., 2017; Senior and Mitchell, 2000; Rugenstein et al., 2016).

The conceptual models representing the evolving feedbacks as a function of timescales vary slightly between studies - either modulating the efficacy of deep ocean heat uptake (Geoffroy et al., 2013; Winton et al., 2010; Held et al., 2010) or by representing the climate system as sum of warming patterns which emerge on different adjustment timescales (Armour et al., 2013; Rugenstein et al., 2016), each associated with their own feedback parameter. However, the analytical set of solutions
45 for the temperature response to a step change in forcing is the same in either case - a superposition of decaying exponential modes with different timescales varying between a few years and a few centuries (Proistosescu and Huybers, 2017). It has been shown that the implications of these additional degrees of freedom, and ambiguity over contributions from different timescales of response might imply that EffCS may not be strongly constrained by temperature change over the last century (Proistosescu and Huybers, 2017; Andrews et al., 2018), and that the Long Term Equilibrium (LTE) sensitivity may be greater than that
50 implied by estimates which use the CF framework (Otto et al., 2013; Lewis, 2013).

This state of understanding leads to a number of emerging critical questions which we discuss in this paper - can we explain the non-intuitive result that EffCS is a better predictor than T140 of end-of-century temperatures under RCP8.5? Which summary metrics of global sensitivity to greenhouse gas forcing are most useful for effective policy decisions? Finally, do the implicit structural assumptions underpinning the applicability of these metrics to the real world cause us to mis-categorize and
55 potentially underestimate future warming risk?

1 A simple model example

We begin by considering an idealized ensemble of climate model simulations. We use a two timescale thermal response model, conceptually representing the deep ocean (with a response timescale of a century or more) and shallow ocean response timescales (with a response timescale of 10 to 50 years). Such a model, although simple, is capable of resolving evolving

60 feedback amplitudes and can emulate the climatological responses of complex Earth System Models on two timescales. Such a model makes a structural assumption that the Earth can be modelled as a discrete sum of linear decaying exponential responses to forcing, but this model has been found to well describe GCM evolution on a century timescale (Proistosescu and Huybers, 2017; Geoffroy et al., 2013) and is sufficiently complex to illustrate the limitations of defining system sensitivity through TCR or EffCS.

65 To efficiently describe the response of the system to a generic forcing, this study employs a linear Green's function which describes the forcing by convolution with an impulse response Ruelle (1998) (in this case, the step change in CO2 forcing). This approach can be used to approximate and simplify global climate dynamics Ragone et al. (2016); Lucarini et al. (2017), and its computational efficiency allows Markov-Chain Monte Carlo parameter estimation for the physical parameters. Furthermore (and critically for this study), the pulse-response formulation can be used to self-consistently relate different metrics of climate
70 sensitivity on a range of timescales Lucarini et al. (2017).

1.1 Model Formulation

The two-timescale impulse response model follows the thermal feedback-timescale implementation from the FAIR simple climate model (Smith et al., 2018; Millar et al., 2017), which follows Hasselmann et al. (1993):

$$\frac{dT_n}{dt} = \frac{q_n F - T_n}{d_n}; T = \sum_n T_n; n = 1, 2, \quad (1)$$

75 where T_n is global mean temperature and for each timescale n . T_n is the component of warming associated with that timescale, q_n is the feedback parameter and d_n is the response timescale. We consider the heat flux into the shallow and deep ocean to be functions of the same timescale:

$$R_n = r_n(F - T_n/q_n); R = \sum_n R_n; \sum_n r_n = 1; n = 1, 2 \quad (2)$$

80 where r_n is an efficacy factor for heat absorbed by the deep ($n = 1$) or shallow ($n = 2$) ocean, which sum to unity given the boundary condition that $R(0) = F(0) = F_{4xCO2}$ at $t = 0$ (allowing just one degree of freedom r_1 - the fraction of heat which is allocated to deep ocean storage).

The particular solutions for temperature and radiation response to a step change in forcing F_{4xCO2} at time $t = 0$ can be expressed as a sum of exponential decay functions:

$$T_p(t) = F_{4xCO2} \sum_{n=1}^2 q_n (1 - \exp(-t/d_n)) \quad (3)$$

$$85 \quad R_p(t) = F_{4xCO2} \sum_{n=1}^2 r_n (\exp(-t/d_n)), \quad (4)$$

where $T_p(t)$ is the annual global mean temperature and $R_p(t)$ is the net top-of atmosphere radiative imbalance at time t , and F_{4xCO_2} is the instantaneous global mean radiative forcing associated with a quadrupling of CO_2 , taken here to be $3.7Wm^{-2}$ (Myhre et al., 2013).

We define a historical forcing timeseries as a function of CO_2 concentrations $C(t)$ and a non- CO_2 forcing timeseries
90 $F_{nonCO_2}(t)$ (both taken from (Meinshausen et al., 2011)):

$$F(t) = \frac{F_{4xCO_2}}{\ln(4)} \ln\left(\frac{C(t)}{C_0}\right) + f_r F_{aer} + F_{other}, \quad (5)$$

where f_r is a free parameter to allow scaling of aerosol forcing (conceptually allowing for forcing uncertainty in the historical timeseries), and $F_{otherAnt}$ is all other anthropogenic and natural forcers (summed from (Meinshausen et al., 2011)). The thermal response is calculated by expressing the numerical time derivative of the forcing timeseries $F(t)$ where the change in
95 forcing in a given time-step in a given year $\Delta F(t')$ is $[F(t') - F(t' - 1)]$. The forcing timeseries can thus be expressed a series of step functions, and T_p from equation 3 can be used to calculate the integrated thermal response.

$$T(t) = \sum_{t'=0}^t \Delta F(t') \sum_{n=1}^2 q_n \left(1 - \exp\left(\frac{-(t-t')}{d_n}\right)\right), \quad (6)$$

Heat fluxes into the deep ($D(t)$) and shallow ($H(t)$) ocean components are represented by numerical integration of the slow (n=1) and fast (n=2) pulse response components of $R_p(t)$ in Equation 4:

$$100 \quad D(t) = r_1 \sum_{t'=0}^t \Delta F(t') \exp\left(\frac{-(t-t')}{d_1}\right), \quad (7)$$

$$H(t) = (1 - r_1) \sum_{t'=0}^t \Delta F(t') \exp\left(\frac{-(t-t')}{d_2}\right), \quad (8)$$

1.1.1 Model Optimization

The model input time-series for calibration are observed CO_2 concentrations, along with radiative estimates from Meinshausen et al. (2011) of non- CO_2 forcing agents. We optimize the thermal model parameters for 2 timescales and the non- CO_2 forcing
105 factor (see Table 1).

A Markov-Chain Monte-Carlo (MCMC) optimization procedure produces an ensemble of parameter configurations such that the density of the simulations in parameter space reflects the likelihood as reflected in a cost function (as represented by a number of pre-defined likelihood metrics). MCMC algorithms employ a random walk in parameter space which ultimately seeks to produce a representative sample of the distribution.

110 The classical approach to this random walk is the Metropolis Hastings algorithm MacKay and Mac Kay (2003), which iteratively moves a set of ‘walkers’ or sample points throughout the parameter space. This approach, however is computationally inefficient requires the specification of the transition distribution with a large number of degrees of freedom. Here, we follow the (Goodman and Weare, 2010) MCMC implementation which updates a walker position using a vector defined stochastically from the remaining ensemble of walkers. This approach has fewer degrees of freedom and is a well-tested approach for

115 multidimensional optimization problems Foreman-Mackey et al. (2013). We use flat initial parameter distributions as shown in
 Table 1, 200 walkers and 50,000 iterations for each optimization.

Cost functions are computed for global mean temperature, shallow and deep ocean content:

$$E_T = \sum_t \left(\frac{(T(t) - T_{obs}(t))}{\sqrt{2}\sigma_T} \right)^2 \quad (9)$$

$$E_H = \sum_t \left(\frac{(H(t) - H_{obs}(t))}{\sqrt{2}\sigma_H} \right)^2, \quad (10)$$

$$120 \quad E_D = \sum_t \left(\frac{(D(t) - D_{obs}(t))}{\sqrt{2}\sigma_D} \right)^2, \quad (11)$$

where T_{obs} are HadCRUT 4.6 ensemble median global mean temperature anomalies Morice et al. (2012) relative to a 1850-1900 baseline and σ_T is defined as the standard deviation of HadCRUT 1850-1900 values. Shallow and Deep Ocean heat fluxes are taken as the 0-300m and 300m+ heat content derivatives respectively in (Zanna et al., 2019), with σ_H and σ_D taken as 1850-1900 standard deviations from the same dataset.

125 Flat priors are used for all parameters, with an additional prior on true equilibrium climate sensitivity using the likely value and upper bound on Equilibrium Climate Sensitivity from Goodman and Weare (2010) to specify the median and 90th percentile of a gamma distribution for equilibrium sensitivity (i.e. warming as $t \rightarrow \infty$).

We demonstrate that this technique is able to capture the broad uncertainty associated with future projections of CMIP models by using pre-2020 temperatures in RCP8.5 to calibrate the simple model outlined above (Figure S4). In most cases,
 130 the future projection for each scenario falls within the distribution arising from the MCMC ensemble fit, with some specific exceptions - FIO-ESM, FGoals-G2, CCSM4 (which share some common heritage) and the GISS models. As such, the observationally fitted MCMC ensemble explores broadly comparable uncertainty to that seen in the bulk of the CMIP ensemble, with the caveat that the ensemble tends to under-sample cases where there is little or no long term warming response to emissions.

Long name	Symbol	Min	Max
Thermal equilibration of deep ocean Sensitivity (KWm^{-2})	q_1	0	10*
Thermal adjustment of upper ocean Sensitivity (KWm^{-2})	q_2	0	10
Thermal equilibration of deep ocean timescale (<i>years</i>)	d_1	100	4000
Thermal adjustment of upper ocean timescale (<i>years</i>)	d_2	10	100
Fraction of forcing in deep ocean response	r_1	0.	1
Non-CO2 Forcing ratio	f_r	.7	1.3

Table 1. A table showing model parameter values and minimum and maximum values allowed in model optimization.

The physical parameters of this simple model are constrained by historical carbon dioxide concentrations together with
 135 observed global mean temperatures from 1870 to present day (together with aggregate forcing estimates representing other

anthropogenic emissions (Meinshausen et al., 2011), which are not the focus of this study). The posterior parameter distribution for the model can then be used to project the corresponding range of response in probabilistic projections of the future scenarios or in idealized experiments which simulate a range of self-consistent values for various climate sensitivity metrics.

1.1.2 Idealized Simulations

140 Effective Climate Sensitivity is measured by implementing a step-change abrupt CO₂ quadrupling, and following (Gregory et al., 2004) to assess the linear extrapolation of warming at the point of net top of atmosphere energetic balance. A140 is calculated as the average of year 131-150 of the abrupt4xCO₂ simulation. TCR and T140 are calculated as the average of years 61-80 and 131-150 respectively of the 1pctCO₂ simulation (during which the CO₂ concentrations are doubled and quadrupled, respectively), where CO₂ concentrations are increased annually by 1pct resulting in a linear increase in climate
145 forcing. RCP scenario temperature trajectories are calculated for each parameter set using concentration and forcing timeseries from (Meinshausen et al., 2011) from 1850 until 2300.

Resulting EffCS values (to a doubling of CO₂) range from 2.4 to 4.6K (5th and 95th percentiles), and values of TCR from 1.6 to 2.2K (Figure 1(b,e)). This results in a range of 21st century warming under two scenarios considered, RCP2.6(RCP8.5) 2100 warming ranges from 1.4 to 2.4 K (3.8 to 5.1K) respectively (5th and 95th percentiles, see Figure 1(a)).

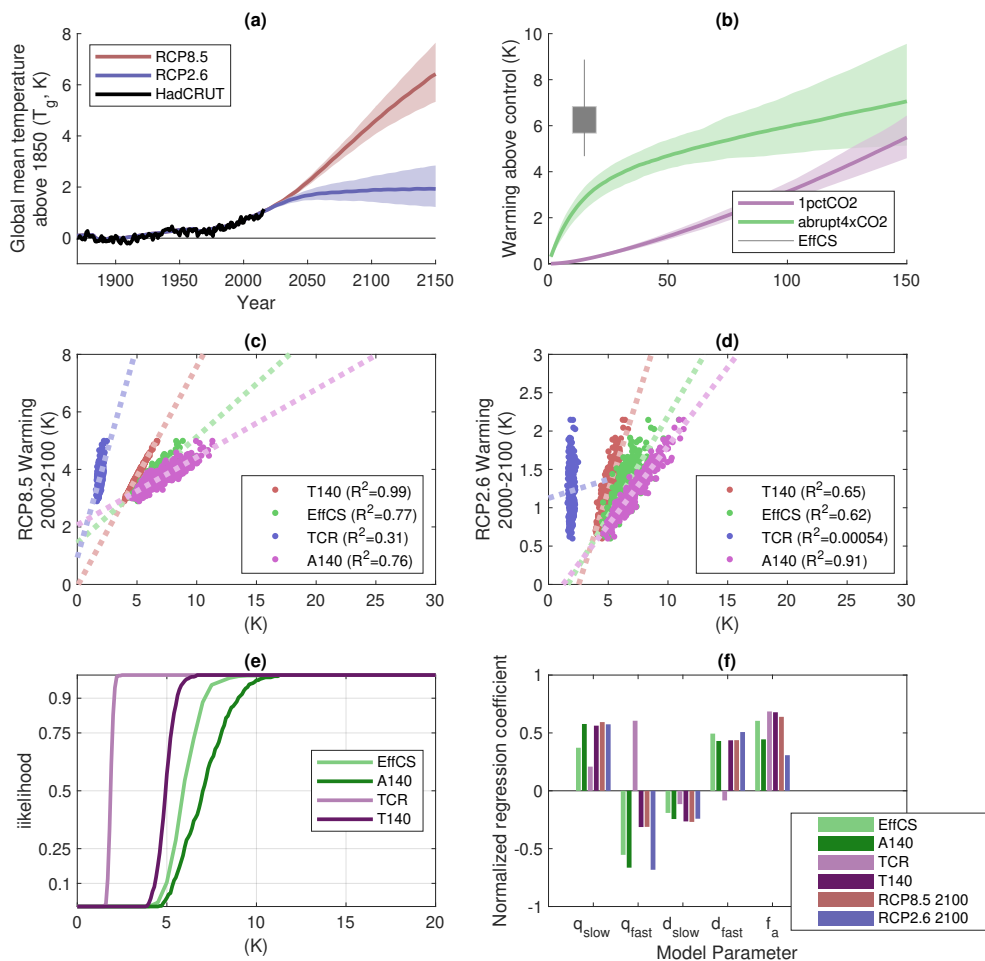
150 We then consider in the context of this observationally constrained ensemble of simple models, what idealized metrics of system response are most informative for describing 21st century warming. We consider four metrics: the EffCS, TCR/T140 (transient warming under an annual compounded 1 percent increase in CO₂ concentrations at time of CO₂ doubling/quadrupling, corresponding to years 70 and 140 of the simulation). We also introduce A140 as a possible metric for consideration, defined as the global mean warming above pre-emission levels in the abrupt4xCO₂ simulation calculated 140 years after time of CO₂
155 quadrupling (here and throughout estimated as the mean from years 131-150). Figure 2 illustrates how ensemble spread would be impacted for a set of different scenarios if each of these metrics were constrained to lie within a narrow range (nominally the 45-55th percentile range of values present in the entire observationally constrained ensemble).

In the high emissions, RCP8.5 scenario (Riahi et al., 2011), 2000-2100 warming is nearly perfectly described ($R^2 = 0.99$) by T140, the transient climate response after 140 years in a 1 percent CO₂ simulation (Figure 1(c) and Figure 2(k)). The
160 corresponding response after only 70 years, TCR, is a much poorer predictor at $R^2 = 0.31$).

These results are physically intuitive. The climate forcing and rate of change of forcing in RCP8.5 at the end of the 21st century are of similar magnitude to those in year 140 of the 1 percent CO₂ simulation, and so it is unsurprising that T140 is an efficient predictor for RCP8.5. TCR is a poor predictor in the simple model ensemble largely because TCR itself is already highly constrained by historical warming (Figure 1(e)), and thus the ensemble is effectively conditioned on a value of TCR and
165 it has little additional explanatory value in explaining the ensemble variance in the RCP projections (Figure 2(f,g)).

EffCS and A140 are also well correlated with the RCP8.5 warming ($R^2 = 0.77$ and 0.76 respectively), but less so than T140. For the mitigation scenario RCP2.6, the most effective predictor of 2000-2100 warming is A140 ($R^2 = 0.91$). Both EffCS and T140 are weakly correlated ($R^2 = 0.62$ and 0.65 respectively), and TCR shows no significant correlation.

Figure 1. An observationally constrained ensemble of simple models. (a) shows the global mean temperature both historically and under the RCP2.6 and RCP8.5 scenarios. Black lines show the HadCRUT data used in calibration, whereas shaded regions show the 10-90% range of scenario projections in the posterior simple model ensemble distribution. (b) shows the corresponding time-series posterior distributions for the abrupt4xCO₂ and 1pctCO₂ simulated experiments, with grey errorbars showing range of EffCS for CO₂ quadrupling (boxes and whiskers show 25-75th and 1-99th percentiles respectively). (c/d) show relationships between different sensitivity indicators and 2000-2100 temperature changes under RCP8.5/RCP2.6 respectively (e) shows the posterior cumulative probability density functions for the 4 sensitivity variables considered and (f) shows the parameter regression coefficients relating the 5 normalized model input parameters to the 4 normalized sensitivity metrics.



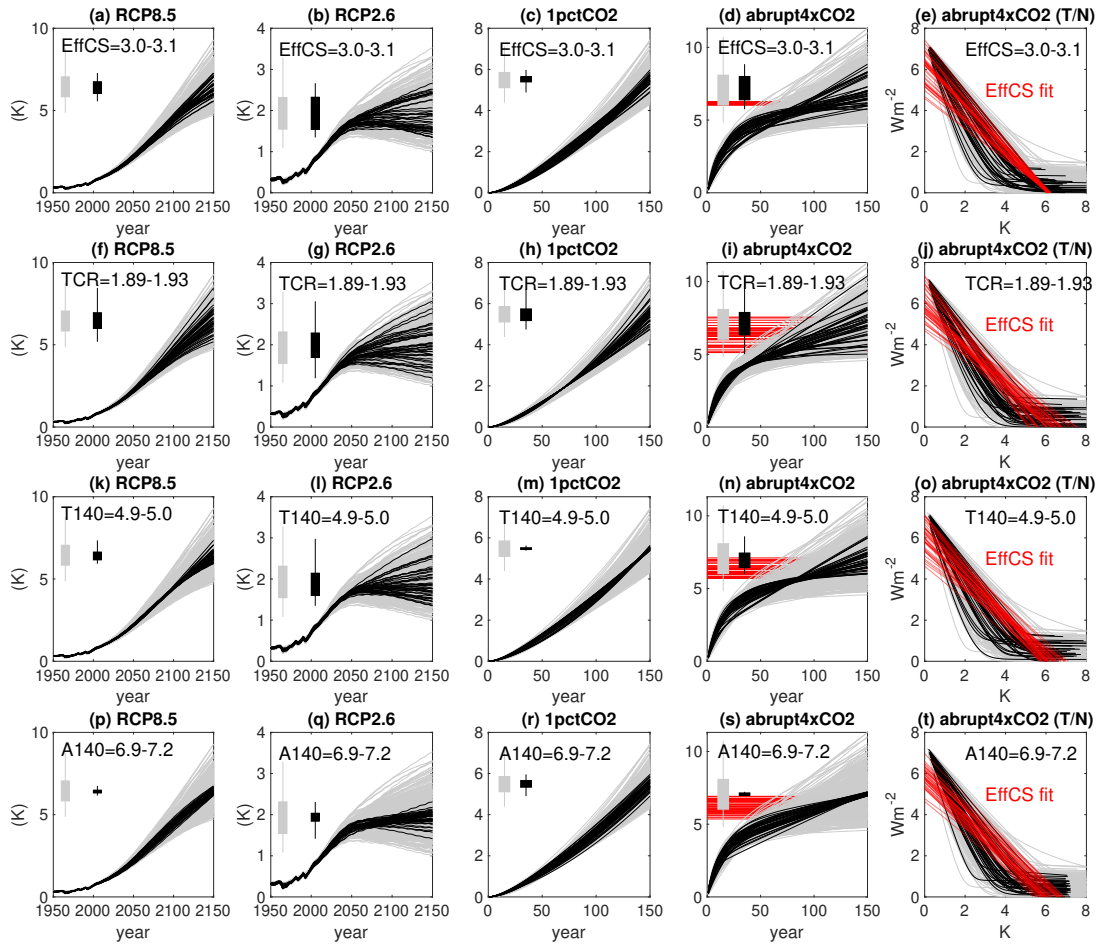


Figure 2. An illustration of how constraining different types of global sensitivity metric impact the idealized spread of global mean temperature evolution under different scenarios. Each row illustrates one constraint, Effective Climate Sensitivity to CO₂ doubling (EffCS), TCR (70 year, CO₂ doubling), T140 (140 year, CO₂ quadrupling) and A140. Lines in grey show the entire posterior distribution of models from Figure 1, while lines in black show the 45-55th percentiles of the distribution of the respective quantity. The first four columns show global mean temperature time-series of a scenario or idealized experiment - RCP8.5, RCP2.6, 1 percent ramping CO₂, abrupt CO₂ quadrupling (the 5th column shows energetic imbalance as a function of surface temperature in the abrupt4xCO₂ experiment). Histograms show the resulting distribution of temperature in 2150 (RCP8.5/2.6) or year 140 (1pctCO₂, abrupt4xCO₂) for the complete distribution (grey) and 45-55th percentile range (black). Red lines show the distribution of values of effective climate sensitivity (4th column) and the trend lines used to compute it (5th column).

To help understand these relationships, we can perform a regression analysis of the metrics as a function of model ensemble parameters (Figure 1(f)) which suggests A140 and RCP2.6 warming from 2000 to 2100, are controlled by the *difference* between the slow and fast components of sensitivity. We can understand this in the context of the way the model is constrained by historical temperatures.

There is a weak trade-off between fast and slow components of climate sensitivity in the posterior parameter distribution of the ensemble (see supplementary figure S3), which broadly determines the fraction of equilibrium warming associated with current forcing levels that has already been experienced. If a greater fraction of today's observed warming is explained with the faster component of model response, there is less unrealized warming in a mitigation scenario later in the century. This causes large uncertainties in RCP2.6 evolution, even if EffCS, TCR or T140 are known (Figure 2b,g,l).

The constrained distribution for fast-timescale sensitivity is near-Gaussian, and non-zero in all ensemble members, whereas slow-timescale sensitivity is more weakly constrained by the observations ranging from near-zero to large (20K/Wm^{-2}) long term equilibrium responses. The slow feedback component strongly controls A140 and RCP2.6 warming (Figure 1(d,f), Figure 2q).

RCP8.5 warming and T140, however are associated with a near-linear increase in forcing throughout the simulation which results in a near-linear temperature increase. The relative fraction of warming associated with fast- and slow-timescale feedbacks remains constant over time, and thus warming to date (effectively fixing TCR, subject to aerosol forcing uncertainty) better constrains relative error in future response in a non-mitigation scenario (Figure 2f).

2 Considering the multi-model ensemble

But how do the findings in the simple model framework reconcile with findings in the CMIP5 and CMIP6 multi-model ensembles? Firstly, it is plausible that there is some commonality in the lack of skill of TCR (the transient response after 70 years) in our simple model ensemble and in the CMIP ensembles. In our simple model case, the ensemble members were explicitly calibrated to reproduce the 20th and early 21st century warming - which is a very strong constraint on the value of TCR in this idealized setup.

Earth System Model calibration is conducted in a much larger parameter space by groups with a wide range of objectives which complicate interpretation (Mauritsen et al., 2012; Sanderson and Knutti, 2012), but simulations are generally only published using models which are able to adequately describe the 20th century and thus might be subject to a similar effective constraint on TCR which renders the metric ineffective for describing variance in the future evolution of the model. But there remains a direct contradiction for T140, where the simple model suggests T140 should be a better predictor than EffCS for non-mitigation warming in the 21st century whereas the opposite was found in the CMIP correlations (see Supplementary material, Figure S2 and (Grose et al., 2018)).

To understand this, we need to consider how the properties of the simple model ensemble differ from the CMIP archive. Although the thermal response of the simple model is broadly able to represent the climatological response of CMIP models to step forcing and transient forcing in CO_2 over a century timescale ((Geoffroy et al., 2013; Proistosescu and Huybers, 2017)),

it contains no internal climate variability and all experiments in Section 1 are conducted from an idealized, perfectly spun up state.

Both of these assumptions are not true for CMIP5 or CMIP6. Measurement of EffCS and TCR are complicated by internal variability (Knutti and Rugenstein, 2015), and many models still exhibit some temperature drift in the control simulation from which the ‘1pctCO2’ simulations and ‘abrupt4xCO2’ simulations are branched (Figure 3). This creates uncertainty from two sources - firstly, it is not always apparent at what point during the control simulations the 1pctCO2 simulation has been branched, thus there is uncertainty in how the anomaly should be measured. Secondly, there is the potential for an unknown contribution of control drift to be erroneously included in the temperature evolution of the 1pctCO2 and abrupt4xCO2 simulations.

To assess the contribution of control drift bias in sensitivity metrics, we implement idealized representations of non-equilibration into our simple model from Section 1. We then create an idealized distribution of drift similar to that seen in the CMIP ensembles in the simple model ensemble by initializing the model 500 years before the experiment begins, defining an effective ‘baseline’ period from which anomalies are measured to be the average temperature between years 400 and 500. Climate internal variability is represented by a 2nd order autoregressive model, which is fitted to each CMIP model in turn. The ensemble-mean autoregressive parameters are used to create artificial ‘noisy’ simulations by linearly adding noise generated from the autoregressive model to the output of the simple model.

We consider the range of control drifts observed in the CMIP5 and CMIP6 ensembles (illustrated in Figure 3(L)) which range from -0.3 to $+0.6$ K/century in the CMIP5 and CMIP6 models considered in this study. An idealized distribution of drift in the simple model ensemble is created by initializing the model 500 years before the abrupt4xCO2 or 1pctCO2 simulation with a non-zero, constant forcing drawn from a flat distribution ranging from -1 to $+1$ Wm^{-2} , which results in a distribution of control drift of -0.4 K to $+0.4$ K per century (i.e. broadly comparable to the CMIP case). For each simulation we consider a baseline for temperature to be defined by the average global mean temperature in years 400-500.

To represent the first order effect of climate noise, we fit a 2nd order autoregressive model to the detrended global mean temperature timeseries in each available model in the CMIP5/6 ensemble. Taking CMIP mean parameters for the variance and autoregressive parameters, we generate noise for each realization of the simple model (though we note, in practise that the noise characteristics vary by CMIP model).

The results are illustrated in Figure 4(a), where the simple model ensemble is initialized in a non-equilibrium state with additive Gaussian noise. With these additional sources of error, both EffCS and A140 are not strongly impacted when measured in the noisy/unequilibrated model variants (Figure 4(b,c)), but the T140 measurement is strongly degraded (Figure 4(d)). Indeed, in this ensemble the biased measurements of EffCS or A140 are slightly better correlated with true T140 than the biased measurement of T140 itself. This provides a possible explanation for why T140 may be a poor predictor of RCP8.5 warming in CMIP.

In our simple framework, the reasons for the more accurate measurement of EffCS are primarily associated with the lack of equilibration. Simply adding noise from the autoregressive model has little effect on the accuracy of EffCS, T140 or A140 (where both T140 and A140 are estimated using the average of years 131 to 150 in the simulation, see Table 2).

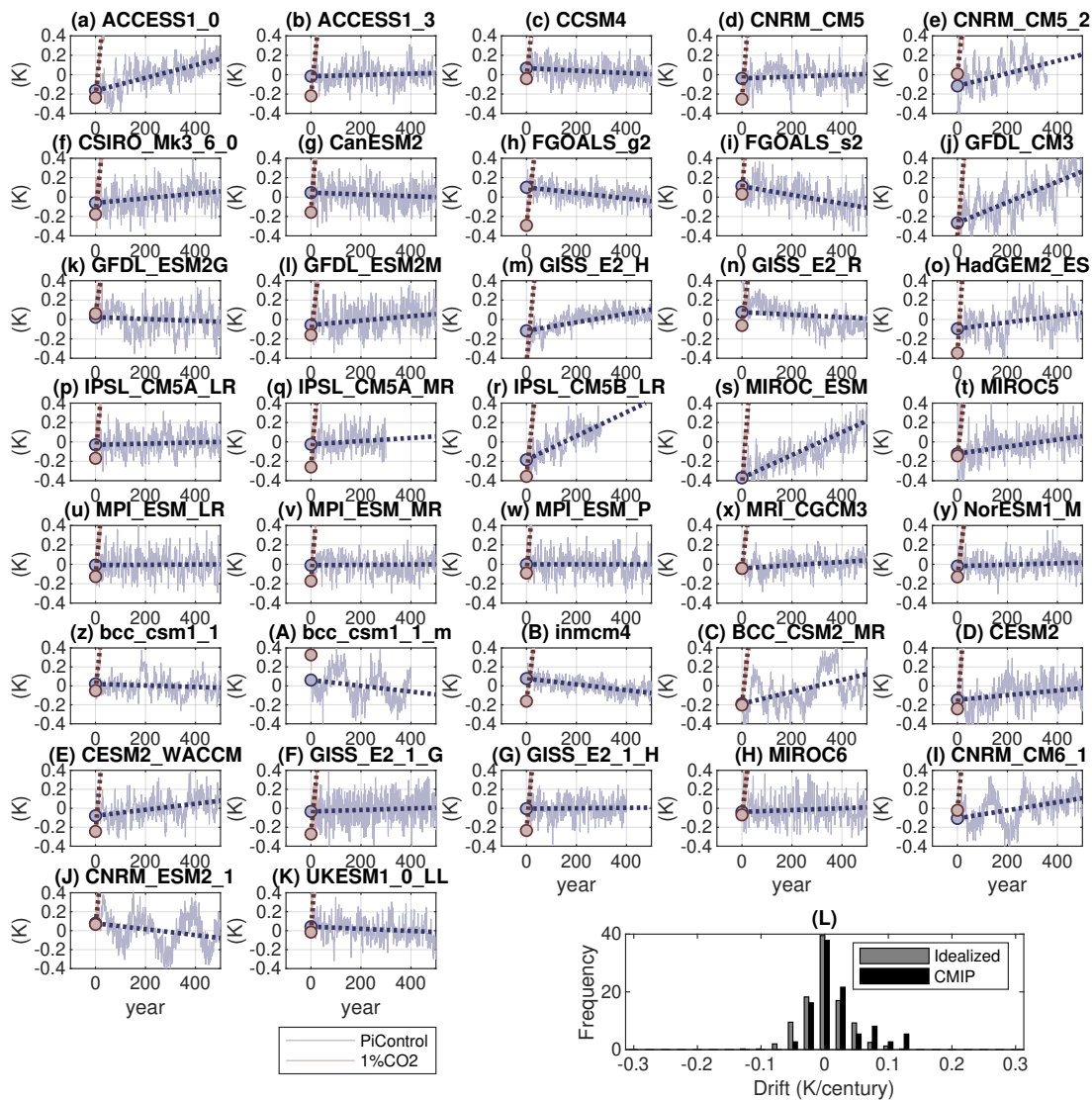


Figure 3. (a-K) Control simulation global mean temperatures from a selection of models in the CMIP5 and CMIP6 ensembles. Control simulations (blue) and initial years of 1pctCO2 simulations (pink) are plotted. Dotted lines show linear fit to the available timeseries. Blue and pink circles show the intersection of the linear temperature fit at the start of the simulation. (L) histogram showing the distribution of control model trend in CMIP (black) and in idealized ensemble of non-equilibrated simple models considered in Figure 4 (grey).

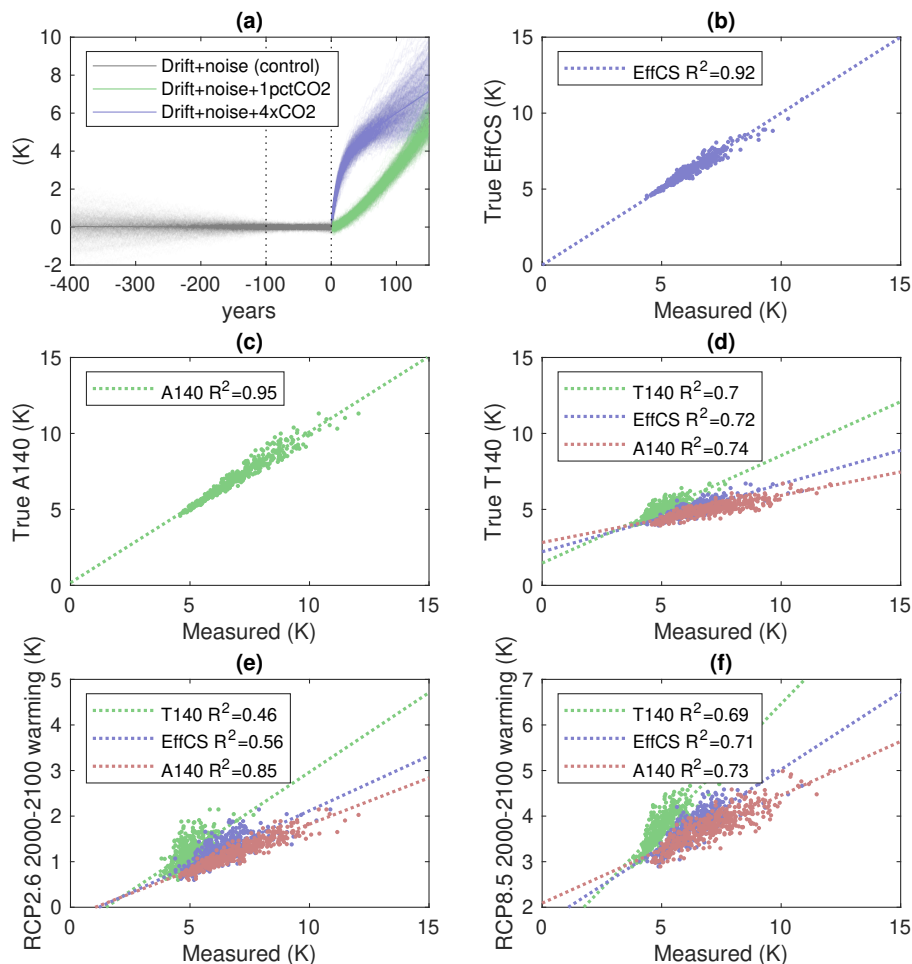


Figure 4. An idealized ensemble of simple models, where model parameters are identical to those considered in Figure 1(b), but models are initialized in a non-equilibrium state such that the baseline period is subject to some control drift, and model output is also subject to interannual variability of a similar magnitude to models in the CMIP archive. (a) shows global mean temperature evolution for the control period (gray), abrupt4xCO₂ simulation (blue) and 1pctCO₂ simulation (green). (b,c) show the true value of (EffCS,A140) as calculated in the noise-free, equilibrated simulations, plotted as a function of the measured value of (EffCS,A140) in a noisy, non-equilibrated simulations. (d,f,g) shows the true value of (T140,RCP2.6,RCP8.5 2000-2100 warming) plotted as a function of the measured values of T140, EffCS and A140 respectively.

Predictor	T140	EffCS	A140	RCP8.5 2000-2100	RCP2.6 2000-2100
T140 (true)	1.00	0.78	0.77	0.99	0.65
EffCS (true)	0.78	1.00	0.70	0.77	0.62
A140 (true)	0.77	0.70	1.00	0.76	0.91
T140 (drift)	0.74	0.58	0.59	0.73	0.50
EffCS (drift)	0.73	0.94	0.67	0.73	0.59
A140 (drift)	0.74	0.67	0.95	0.73	0.86
T140 (noise)	0.99	0.77	0.76	0.98	0.65
EffCS (noise)	0.78	1.00	0.69	0.77	0.61
A140 (noise)	0.78	0.70	1.00	0.77	0.91
T140 (drift+noise)	0.70	0.55	0.55	0.69	0.47
EffCS (drift+noise)	0.72	0.93	0.65	0.71	0.58
A140 (drift+noise)	0.73	0.66	0.94	0.72	0.85

Table 2. A table showing R^2 regression statistics relating a set of predictors to a set of unbiased model properties. Predictors are Transient Climate Sensitivity at quadrupling of CO₂ (T140), Effective Climate Sensitivity (EffCS) and warming 140 years after a quadrupling of CO₂ (A140), additional rows show these values measured experiments conducted with unequilibrated base climates (drift), additive autoregressive noise (noise) and a combination of both factors (drift+noise). 'True' output model properties (T140, EffCS, A140, RCP8.5 and RCP2.6 warming from 2000 to 2100) are derived from the equilibrated model without noise.

Both A140 and EffCS are less sensitive to non-equilibrated initial states than T140. The former experiences the same variance due to the uncertain climate drift, but the absolute value of A140 tends to be larger than T140, thus there is less relative error in its estimation. The effect on the drift on EffCS is muted because the near-linear climate drift primarily biases the estimation of slow rather than fast feedbacks (see Supplementary Figure S1). Because EffCS is primarily a measure of fast-mode feedback strength (see Figure 1(f)), its value is less impacted if experiments are started from a non-equilibrium state.

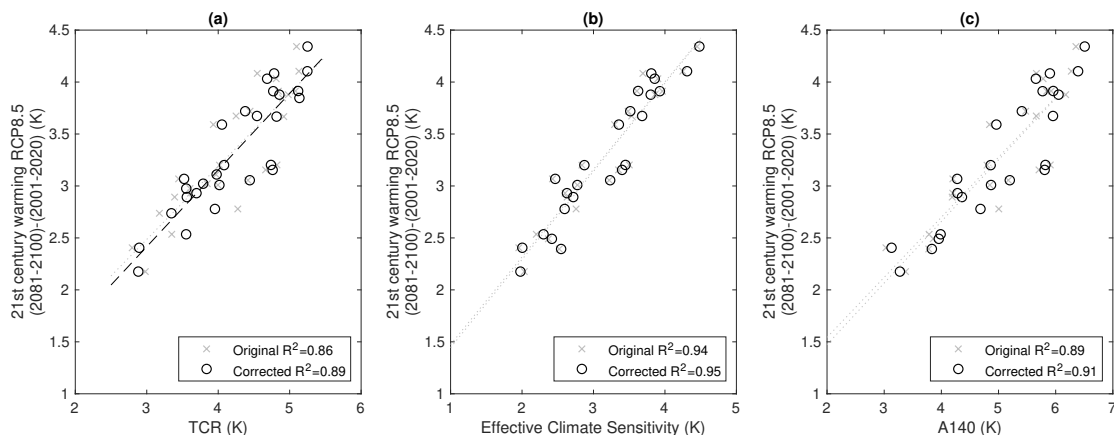
There is some evidence that the lack of equilibration has an outsized effect on the estimation of TCR in the CMIP models. In Figure 5, we attempt to unbias the estimate of TCR in two ways. Firstly, we estimate the baseline temperature by regressing the temperatures in the first 20 years of the 1 percent CO₂ ramp experiment as a function of time (see Supplementary Figure S5). Anomalies in temperature (and TOA fluxes for ECS) are measured relative to the corrected baselines derived from the 1pctCO₂ simulation, and estimated linear pre-industrial trends are subtracted from the 1pctCO₂ and abrupt4xCO₂ timeseries. This pre-processing of the temperature timeseries improves the correlation between TCR and 21st century warming under RCP8.5 from 0.86 to 0.89. It also improves the correlation between EffCS and 21st century warming slightly from 0.94 to 0.95 (and A140 from 0.89 to 0.91).

These 'corrected' values (listed in Table 3) are estimates only, given we would expect the regression estimate based on a short 20 year period to be itself subject to internal variability noise, and we are assuming that the abrupt4xCO₂ simulation and 1pctCO₂ simulation have the same baselines. However, the improvement in correlation with future warming seen over the

Model	EffCS (org)	EffCS (corr)	A140 (org)	A140 (corr)	T140 (org)	T140 (corr)	RCP8.5 2000- 2100	RCP2.6 2000- 2100
ACCESS1_0	3.48	3.53	5.48	5.60	4.45	4.57	3.72	-
ACCESS1_3	3.30	3.38	4.84	5.02	3.93	4.11	3.59	-
BNU_ESM	3.86	3.80	6.17	6.05	4.98	4.86	3.88	0.63
CCSM4	2.84	2.87	4.80	4.86	4.02	4.08	3.20	0.44
CESM1_CAM5_1_FV2	3.31	2.89	5.29	4.44	-	-	-	-
CNRM_CM5	3.22	3.28	5.17	5.30	4.42	4.54	3.06	0.68
CNRM_CM5_2	3.37	3.37	5.11	5.12	4.29	4.29	-	-
CSIRO_Mk3_6_0	3.53	3.63	5.66	5.86	4.25	4.45	3.67	1.09
CanESM2	3.61	3.59	5.92	5.89	5.08	5.05	3.91	0.92
FGOALS_s2	3.85	3.78	5.90	5.76	4.76	4.62	-	-
GFDL_CM3	3.69	3.87	5.66	6.02	4.55	4.90	4.08	1.25
GFDL_ESM2G	2.37	2.34	3.86	3.80	-	-	2.49	-0.08
GFDL_ESM2M	2.52	2.60	3.78	3.93	-	-	2.39	0.32
GISS_E2_H	2.20	2.42	3.79	4.23	3.35	3.79	2.53	0.36
GISS_E2_R	2.03	2.01	3.37	3.34	2.98	2.94	2.18	0.09
HadGEM2_ES	4.25	4.34	6.27	6.45	5.13	5.30	4.10	0.87
IPSL_CM5A_LR	3.90	3.92	5.78	5.78	4.81	4.81	4.03	0.80
IPSL_CM5A_MR	3.96	4.01	5.84	5.93	4.84	4.93	3.91	0.59
IPSL_CM5B_LR	2.43	2.54	4.20	4.43	3.45	3.67	3.07	-
MIROC_ESM	4.45	4.51	6.35	6.56	5.10	5.30	4.34	1.26
MIROC5	2.60	2.62	4.20	4.27	3.61	3.68	2.93	0.62
MPI_ESM_LR	3.50	3.45	5.91	5.82	4.82	4.74	3.20	0.43
MPI_ESM_MR	3.35	3.42	5.71	5.84	4.66	4.80	3.15	0.36
MPI_ESM_P	3.34	3.31	5.71	5.64	4.57	4.49	-	-
NorESM1_M	2.63	2.68	4.19	4.29	3.39	3.49	2.89	0.55
bcc_csm1_1	2.77	2.77	4.85	4.87	4.00	4.02	3.01	0.52
bcc_csm1_1_m	2.76	2.68	5.00	4.84	4.27	4.11	2.78	0.30
inmcm4	1.96	2.00	3.03	3.13	2.80	2.89	2.41	-
BCC_CSM2_MR	2.87	2.91	4.75	4.89	3.88	4.02	-	-
CESM2	4.70	4.80	7.20	7.40	5.01	5.20	-	-
CESM2_WACCM	4.32	4.43	6.51	6.74	4.68	4.91	-	-
GISS_E2_1_G	2.61	2.66	4.18	4.27	1.95	2.04	-	-
GISS_E2_1_H	2.99	3.09	4.94	5.13	4.11	4.31	-	-
MIROC6	2.40	2.40	3.96	3.98	3.47	3.49	-	-
CNRM_CM6_1	4.69	4.67	6.75	6.71	5.49	5.46	-	-
CNRM_ESM2_1	4.35	4.30	6.16	6.07	5.12	5.02	-	-
UKESM1_0_LL	5.26	5.14	7.66	7.41	6.36	6.11	-	-
E3SM_1_0	5.26	4.68	-	-	-	-	-	-

Table 3. A table showing various sensitivity metrics estimated from the CMIP5 and CMIP6 ensembles (in K), using both pre-industrial average baseline temperatures (org) and baseline temperatures estimated from a regression fit to the first 20 years of the 1pctCO2 simulation (corr), where the linear fit is used to estimate temperatures and radiative fluxes at t=0. Warming is shown (where available) for corresponding RCP2.6 and RCP8.5 simulations, where the difference between 2001-2020 and 2081-2100 in the first ensemble member for the corresponding model is used to assess 21st century warming.

Figure 5. Plots showing the correlation between TCR (a), EffCS (b) and A140 (c) with 21st century warming, here represented by the difference between 2001-2020 and 2081-2100 global mean temperatures in the 1st ensemble member for each model in the CMIP5 archive for the RCP8.5 scenario. Each plot shows the 'original' calculation, where the baseline temperatures (and TOA fluxes for EffCS) are taken as the PControl mean. In the 'corrected' calculation, a correction term for the baseline temperature and control drift is applied. Correlation coefficients are shown for the original and corrected cases.



case with the pre-industrial average baseline supports the hypothesis that control drift adds uncertainty to the estimation of all quantities (and particularly TCR). However, it is not a complete explanation - and even after this adjustment, EffCS remains better correlated to RCP8.5 transient warming than TCR in the multi-model ensemble.

3 Conclusions

The question of which metric of climate sensitivity is most useful for summarizing uncertainty in future projections is conditional on a number of factors. Any single metric of sensitivity, even if known perfectly, cannot constrain Earth System response on all timescales and scenarios. We have shown here that one can produce a number of model variants which can exhibit the same value of EffCS or TCR, but with a range of responses, especially in a mitigation scenario such as RCP2.6.

In an idealized environment where models can be brought to a complete equilibrium control state, and ensemble sizes for '1pctCO₂' simulations are large enough to avoid the effects of internal variability, the T140 metric would be the best idealized warming measure for century-scale warming under a high emissions scenario. However, the presence of even moderate control drift can act as a significant source of error in the measurement of T140, and so here we find that EffCS is likely to be a more accurate practical sensitivity metric in Earth System Model applications where full equilibration is difficult to achieve.

EffCS itself has limitations, it is relatively insensitive to slow timescale feedbacks, which means that it poorly correlated with century-scale warming under RCP2.6 (where a large fraction of warming occurs due to slow feedback response to historical emissions), and for warming on multi-century timescales under a high emissions scenario (where concentrations stabilize post-2100). We find that a simple, but useful alternative is to simply use the mean warming from years 131-150 of the abrupt-

270 4xCO₂ simulation - which is comparably skilled to EffCS in predicting RCP8.5 warming in 2100, but more sensitive to century timescale feedbacks than EffCS - so therefore it is better correlated with RCP2.6 end of century warming.

It is notable that the most common metrics of sensitivity, EffCS, T140 and TCR, provide very little guidance on peak warming expected under climate mitigation. The focus on these metrics has also given rise to the issue that slow feedbacks in Earth System Models are not well constrained by the set of experiments currently conducted by default in CMIP. The standard
275 150 year simulation used to calculate Effective Climate Sensitivity does not constrain true Equilibrium Climate Sensitivity, and only a limited set of CMIP-class models have run models for long enough to be informative about equilibrium response (Rugenstein et al., 2019).

It should be noted that these conclusions are derived from the consideration of a relatively simple two-timescale pulse response model. In this model, we can show that certain sensitivity metrics are insufficient to constrain future projections, and
280 that non-equilibration may confound measurement. However, the constrained distributions for the metrics are subject to the structural assumptions of the model. The real world may have more than two response timescales Aengenheyster et al. (2018), or may be better described as a continuous sum Ragone et al. (2016); Lembo et al. (2019). Further work should identify how such complexity impacts uncertainty in relevant climate metrics.

The diversity of simulated global mean dynamical response to greenhouse gas forcing over the coming centuries can be
285 represented in simple models with a relatively small number of parameters (Smith et al., 2018; Meinshausen et al., 2011), but we cannot reduce uncertainty in climate projections on all timescales to a single degree of freedom. Summary metrics of climate response have value if the context of those metrics (and their range of applicability in relation to projection uncertainty) is well understood, but their limitations should be kept in mind.

Data availability. CMIP5 and CMIP6 data are available through a distributed data archive developed and operated by the Earth System Grid
290 Federation (ESGF).

Code and data availability. Code for this study is available on Github at https://github.com/benmsanderson/matlab_pulse

Author contributions. The author performed all analysis and writing for this project

Competing interests. The author declares no competing interests

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