



# 1 Millennium-length precipitation Reconstruction over South-eastern Asia: a 2 Pseudo-Proxy Approach

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## 13 14 Abstract

15  
16 Quantifying hydroclimate variability beyond the instrumental period is essential for putting current  
17 and future fluctuations into long-term perspective and to provide a test-bed for evaluating climate  
18 simulations. For South-eastern Asia such quantifications are scarce and millennium-long attempts  
19 are still missing. In this study we take a pseudo-proxy approach to evaluate the potential for  
20 generating summer precipitation reconstructions over South-eastern Asia during the past  
21 millennium. The ability of a series of novel Bayesian approaches to generate reconstructions at  
22 either annual or decadal resolutions and under diverse scenarios of pseudo-proxy records' noise is  
23 analysed and compared to the classic Analogue Method.

24  
25 We find that for all the algorithms and resolutions a high-density of pseudo-proxy information is a  
26 necessary but not sufficient condition for a successful reconstruction. Among the selected  
27 algorithms, the Bayesian techniques perform generally better than the Analogue Method, being the  
28 difference in abilities highest over the semi-arid areas and in the decadal-resolution framework. The  
29 superiority of the Bayesian schemes indicates that directly modelling the space and time  
30 precipitation field variability encapsulates more relevant value than just relying in similarities  
31 within a restricted pool of observational analogues, in which certain hydroclimatic regimes might be  
32 absent. Using a pseudo-proxy network with locations and noise-levels similar to the ones found in  
33 the real world, we conclude that performing a millennium-long precipitation reconstruction over  
34 South-eastern Asia is feasible as the Bayesian schemes provide skilful results over most of the  
35 target area.

## 36 1. Introduction

37  
38 Earth's climate varies in all spatial and temporal time-scales, as it is forced by either natural or



1 anthropic factors. To understand the dynamics of such variability, the analysis of the available  
2 instrumental information is an essential tool. However, the time-coverage of the instrumental  
3 records is rather short and, therefore, information from climate archives (natural and documentary)  
4 going back centuries is important to put current and future changes into a long-term perspective and  
5 to serve as a validation terrain for model simulations with the ultimate goal of understanding the  
6 underlying physical mechanisms.

7

8 South-eastern Asian societies and economies are heavily dependent on the summer rainfall  
9 (monsoon-dominated) as a fresh water resource, thus, it is important to investigate how these  
10 precipitation patterns have varied in the past to provide a useful guide for the climate response to  
11 future changes. Previous hydro Climate Field Reconstructions (CFRs) over Asia revealed a  
12 substantial mismatch between modelled and reconstructed precipitation patterns (Shi et al. 2017)  
13 and the spatial variability of large-scale droughts during the Little Ice Age (Cook et al. 2010, Feng  
14 et al. 2013). While these studies covered the last 500-700 years, a gridded hydroclimate product  
15 going beyond Medieval times on a spatio-temporal high resolution is yet missing. Whether such a  
16 long and highly resolved reconstruction is possible given nowadays available data and  
17 methodologies is the subject of this paper.

18

19 Reconstructing the temporal evolution of climatic variables in the space domain (Climate Field  
20 Reconstructions, CFR) based on the information from a sparse network of proxies and partially  
21 overlapping instrumental data is a complex mathematical problem. First of all, the proxy data used  
22 for generating reconstructions display a set of characteristics that make their use challenging: Their  
23 distribution in space and time is heterogeneous with decreasing numbers back in time; most  
24 archives vary with respect to their temporal resolutions and include dating uncertainties; proxy data  
25 might reflect different climate variables (temperature, precipitation, sea-level changes, pH, sea  
26 water temperature, water mass circulation, etc.), recording climate conditions at different times of  
27 the year, and this data contains non-climatic information (usually referred to as non-climatic noise).  
28 Second, the overlap with instrumental observations is commonly short, limiting opportunities for  
29 statistical learning and further validation. Third, and in contrast to average climate reconstructions,  
30 CFR require the spatial scale-up of the available information therefore implying the need for  
31 strategic inferring of the missing values in the target climate field, even in locations where no data  
32 might be input. Finally, as the number of paleo climatic information becomes smaller back in time it  
33 is virtually impossible to have an independent proxy data set to properly validate the output  
34 reconstruction. A common approach to overcome this shortcoming and have a proper validation  
35 stage is using a pseudo-reality. The process of using a Global Climate Model (GCM) simulation to  
36 assess the ability of a reconstruction technique is known as Pseudo Proxy Experiment (PPE;  
37 Smerdon, 2012; Mann and Rutherford, 2002). In a PPE, simulated data are modified to mimic real-  
38 world proxies and instrumental observations (called pseudo-proxy and pseudo-instrumental data  
39 sets) and the reconstruction algorithms are applied. The reconstruction results are then compared  
40 with the available simulated target field, giving an estimation of the skill of the method in real-



1 world applications.  
2  
3 There are several ways to perform a CFR (see Luterbacher and Zorita, 2018 for a review). The  
4 classical approach is through a multivariate regression perspective: a statistical relationship between  
5 proxy and instrumental data is inferred from the overlapping (calibration) period and then, assuming  
6 stationarity of this relationship, the missing instrumental values are predicted or reconstructed back  
7 through time. Some of the most common techniques for climate reconstructions included in this  
8 category are: Regularized Expectation-Maximization (RegEM, Schneider, 2001), Canonical  
9 Correlation Analysis (CCA; Smerdon et al., 2010), Markov Random Fields (Guillot et al., 2015)  
10 and the Analogue Method (Franke et al., 2011). The performance of these methods strongly depends  
11 on the length of the instrumental data. If the overlapping period between proxy and instrumental  
12 data is short, in comparison with the number of spatial locations considered, the estimation of the  
13 covariance matrix is uncertain and the matrix inversion process is numerically unstable, leading to  
14 poor performance when presented with new data out of the learning sample.  
15  
16 Another strategy to perform a CFR, more novel as it has only recently been applied in  
17 paleoclimatology, is the Bayesian approach (e.g. Tingley and Huybers, 2010, 2013; Werner et al.,  
18 2013; Luterbacher et al., 2016; Werner et al., 2018; Zhang et al., 2018). The Bayesian strategy is  
19 probabilistic, incorporates information about the climate–proxy connection as constraints on the  
20 reconstruction problem and has the benefit of providing more comprehensive uncertainty estimates  
21 for the derived reconstructions. Robust comparisons between established methods and the emerging  
22 efforts (Werner et al., 2013, Nilsen et al. 2018) underpin the benefits and justify further application  
23 of the computationally more expensive method. So far, most of the paleoclimatic applications of  
24 this methodology involve temperature reconstructions. Efforts to apply this probabilistic framework  
25 to the more complex and highly variable hydroclimate are only in the initial stages, but the  
26 advantages of the methodology over more classical approaches are auspicious.  
27  
28 Gómez-Navarro et al. (2015) used a pseudo-proxy experiment (PPE) approach to assess the skill of  
29 several statistical techniques (classical regression methods and Bayesian) in reconstructing the  
30 precipitation of the past two millennia over continental Europe. The authors find that none of the  
31 schemes shows better performance than the others and that precipitation reconstructions over  
32 Europe are only possible given a spatially dense and uniformly distributed network of proxies, as  
33 the accuracy strongly deteriorates with distance to the proxy sites.  
34  
35 In this study we propose to evaluate, via PPE, the potential to generate a last-millennium summer  
36 precipitation reconstruction for South-eastern Asia. We use four CFR techniques: Bayesian  
37 Hierarchical Modeling (BHM), BHM coupled with clustering processes (with two different  
38 numbers of clusters) and Analogue Method. For each of the schemes we perform two  
39 reconstructions: one at annual and one at decadal resolution. In addition, the influence of the noise



1 level in pseudo-proxies on the final reconstruction is evaluated.

2

3 This is the first time that a BHM approach is applied to the hydroclimate of Asia and its coupling  
4 with clustering techniques is a methodological advance, conforming an innovation in the field. The  
5 systematic evaluation of the skill of these probabilistic methods, and the comparison with the more  
6 classical and well established Analogue technique, is a necessary step into learning about the  
7 precipitation variability and the opportunities or obstacles to generate long-ranged informed guesses  
8 about it. The PPE exercise is a fundamental validation step, essential for selecting the most  
9 appropriate method to improve real-world reconstructions and, finally, derive a new and not  
10 previously attempted gridded product of South-eastern Asia precipitation during the last 1000 years.

11

12 The manuscript is organized as follows. In section 2 we present the data and methodology and  
13 describe in detail the four reconstruction techniques, as well as the skill scores used for quality  
14 evaluation. Section 3 is devoted to the results and discussions: we evaluate the skill of each of the  
15 reconstruction methods, at both annual and decadal resolution, and investigate the role of the  
16 pseudo-proxy noise. Finally, in section 4 we present conclusions and a short outlook.

17

## 18 2. Data and Methodology

19

### 20 2.1. Model

21

22 As a virtual reality setup for our study we use one full-forcing simulation (run 001) of the  
23 Community Earth System Model (CESM) from the Last Millennium Ensemble (LME) Project  
24 (Otto-Bliesner et al., 2016). The simulation is performed with horizontal resolution of  $\sim 2^\circ$  ( $\sim 1^\circ$ ) in  
25 the atmosphere and land (ocean and ice) components. The CESM is forced with reconstructions of  
26 the transient evolution of: solar intensity, volcanic emissions, greenhouse gases, aerosols, land use  
27 conditions and orbital parameters, all together, for the period 850-2005. The target variable to  
28 reconstruct is JJA precipitation over continental Southeast Asia, here defined as all continental grid  
29 points in the domain: Equator-50N, 72.5E-127.5E. Given the model resolution, this implies that the  
30 reconstruction is attempted over 366 grid points.

31

32 Figure 1 depicts the JJA mean precipitation in the run used in this manuscript, considering only the  
33 last 100 years of simulation (period 1906-2005). Historical simulations with the CESM show a  
34 reasonable performance at reproducing summer precipitation over continental Asia: the simulated  
35 JJA precipitation is generally in agreement with observations, although a false rainfall center over  
36 the eastern Qinghai-Tibetan Plateau is generated in these simulations (Wang et al., 2015).



1

## 2 2.2. Proxy Data locations

3

4 For this study we select the locations of 47 real-world precipitation/drought sensitive proxies in the  
5 target domain, that span the last millennium. The locations of tree ring, speleothem, lake sediment  
6 and ice core sites as well as of some documentary data are mainly derived from the networks used  
7 in Chen et al. (2015) and Ljungqvist et al. (2016) (Table 1).

## 8 2.3. Design of the Pseudo Proxy Experiments (PPEs)

9

10 For the design of the PPE we build two data networks: a pseudo proxy and a pseudo instrumental.  
11 The pseudo proxy network is based on the locations of the real-world hydroclimate proxies listed in  
12 Table 1. As some of these 47 records are in close proximity, this translates into having 38 different  
13 model grid points (about 10% of the total grid points in the study region). The selected locations are  
14 not evenly distributed across South-eastern Asia: the highest concentrations are found over East  
15 China and over the dry lands in the northwest of the study region (Fig. 1). There are neither pseudo  
16 proxy sites southward of 20N, nor over Mongolia and the Himalayas. To emulate real proxies, we  
17 consider the modelled precipitation time-series spanning the complete period of the simulation  
18 (1156 years, either with annual or decadal resolution) at each of the 38 selected sites and  
19 contaminate them by the addition of noise. We select four different levels of additive Gaussian  
20 white noise, corresponding to null, low, medium, and high levels of noise. The selected noise levels  
21 are such that the correlation between the original and the contaminated time-series is: 1, 0.7, 0.5 and  
22 0.3, respectively. A correlation equal to 1 implies an idealised situation of perfect proxies to study  
23 the representativeness of our spatial sampling. A correlation of 0.7 represents an optimistic  
24 situation, but still realistic: for example, Shi et al. (2014) find correlations of up to 0.7 with a tree-  
25 based reconstruction of the South Asian Summer Monsoon Index. A correlation of 0.5 between the  
26 proxy series and precipitation corresponds to a medium-level noise, and could be regarded as the  
27 average situation with real proxies (examples for Asia: He et al., 2018; Liu et al., 2013). A  
28 correlation of 0.3 represents a high-noise setting, which is still rather common in real-world proxies  
29 (e.g. Jones et al. 1999).

30

31 For the pseudo instrumental network we consider all the locations for which a reconstruction is  
32 targeted: 366 model-grid points in South-eastern Asia. For each of these locations, we take the  
33 modelled precipitation time-series for the last 100 years of simulation (at either annual or decadal  
34 resolution) and add a small Gaussian-noise to represent the instrumental errors present in real  
35 precipitation measurements. The added noise is such that, at each location, the correlation between  
36 original and contaminated time-series is 0.95.

37



1 As an example, Figure 2 shows the simulated precipitation time-series at location [20N,82.5E] (east  
2 India) together with the associated pseudo proxy and instrumental time-series, both at annual and  
3 decadal resolution, for the case of medium-noise level (corresponding to a 0.5 correlation with the  
4 target precipitation). At annual resolution, the simulated mean JJA precipitation at this site is 241  
5 mm/month, with a standard deviation of 48 mm/month. The time-series shows a weak drying trend  
6 (-0.8 mm/month per decade) and decrease in variance, although none of these changes are  
7 statistically significant. The maximum (minimum) summer precipitation at this location is 423 (87)  
8 mm/month and occurred in the year 1022 (1208) of the simulation, respectively. At decadal  
9 resolution, the standard deviation is reduced to 14 mm/month and the maximum (minimum)  
10 precipitation value is 283 (208) mm/month, occurring at the period 1180-1189 (870-879).

## 11 2.4. Reconstruction Techniques

12

13 In the following subsections we describe in detail each of the four reconstruction techniques used in  
14 this manuscript.

### 15 2.4.1. Bayesian Hierarchical Modelling (BHM)

16

17 In the BHM technique a hierarchy of parametric stochastic models is used to describe the  
18 relationship between climate, instrumental and proxy data. The model parameters are estimated  
19 using the available data, through the Bayes's rule. The approach splits the complex relationship  
20 model into three basic components. First, in the process level, a stochastic model describing the  
21 time evolution of the climate variable is selected. Second, in the data level, stochastic relationships  
22 between the instrumental and proxy data and the climate variable are developed. Finally, a level of  
23 prior information about the parameters involved in the other two components of the hierarchy is  
24 coupled. Here we use the BHM algorithm named Bayesian Algorithm for Reconstructing Climate  
25 Anomalies in Space and Time (BARCAST), developed by Tingley and Huybers (2010). Following,  
26 we specify the assumptions and equations for each of the levels in the model hierarchy.

27

#### 28 **Process level:**

29 The process level describes the evolution of the true climatic field as a multivariate autoregressive  
30 process of order 1, AR(1), with spatially correlated innovations.

31

32 The evolution of the true precipitation, sampled at a finite number of spatial locations, is assumed to  
33 follow a first-order autoregressive process:

$$34 \quad Pr_{t+1} - \mu = \alpha (Pr_t - \mu) + \epsilon_{Pr,t} \quad (1)$$

35



1 where  $Pr_t$  is the vector consisting of the true precipitation values in all the locations at time step  $t$ ,  
2  $\mu$  is the mean of the process,  $\alpha$  the AR(1) coefficient. Note that the coefficient  $\alpha$  is the same  
3 for all the locations. The innovations  $\epsilon_{Pr,t}$ , accounting for the interannual or interdecadal  
4 variability, are assumed to be independent and identically distributed (iid) normal draws  
5  $\epsilon_{Pr,t} \sim N(0, \Sigma)$  with an exponentially-decaying spatial structure:

$$6 \quad \Sigma_{ij} = \sigma^2 e^{-\phi |x_i - x_j|} \quad (2)$$

7 where  $|x_i - x_j|$  is the distance between the locations  $i$ -th and  $j$ -th of the precipitation vector,  $\phi$  is  
8 the range parameter and  $\sigma$  is the partial sill of the spatial covariance matrix.

9  
10 The temporal model within BARCAST allows the estimations of the field at a certain temporal step  
11 to be influenced by the information in the previous time-step. The assumed covariance matrix  
12 structure is supposed constant in time and follows an exponentially decaying pattern with distance.  
13 Note that, by assuming this structure if two distant locations have well-correlated precipitation time-  
14 series this will not be well represented by the BARCAST model assumed. The method  
15 parameterizes the spatial covariance matrix with two unknown parameters: the covariance at null  
16 distance ( $\sigma$ ) and the exponential decay rate with distance ( $\phi$ ).

17  
18 The model assumes that the climatic variable, precipitation, follows a Gaussian distribution.  
19 Although this might not be the case, especially for arid regions, the simulated JJA precipitation in  
20 the area of study can be taken to reasonably follow this assumption: for the pseudo-proxy selected  
21 locations 63% of the time-series (considering the instrumental period) pass the Kolmogorov-Smirnov  
22 test for normality at a 95% confidence level (Figure A1).

23  
24 Figure 3 shows the correlation decay with distance for the simulated JJA precipitation for different  
25 latitudinal bands. For annual data (Figure 3a), the correlation between precipitation time-series in  
26 consecutive grid-points is usually high, around 0.8. With few exceptions, the simulated precipitation  
27 follows an exponentially-decaying pattern with distance, with points located further away than  
28 600km showing no significant correlation. Therefore, we take the exponentially-decaying spatial  
29 structure of the covariance matrix in BARCAST to be a reasonable assumption for the model. For  
30 decadal data (Figure 3b), the correlations behaviours are not uniform with respect to the latitudinal  
31 bands. While for some of the latitudes the plot follows an exponentially-decaying shape for others  
32 (notably the northern-most and southern-most latitude bands considered: 44N-48N and 10N-14N,  
33 respectively) this assumption is clearly flawed as it even evidences a teleconnection-pattern and not  
34 just a distance decaying behaviour.

35

### 36 **Data level:**

37 The data level specifies the relationship between the measurements (both proxy and instrumental)



1 and the true field values.

2

3 The instrumental observations at each time are assumed to be noisy variations of the true  
4 precipitation field:

$$5 \quad Inst_t = H_{Inst,t} (Pr_t + \epsilon_{Inst,t}) \quad (3)$$

6

7 the noise terms are assumed to be iid multivariate normal draws  $\epsilon_{Inst,t} \sim N(0, \tau_{Inst}^2)$ , while  
8  $H_{Inst,t}$  is a diagonal matrix with a one in position (i,i) if an instrumental observation is available  
9 at the i-th location, with a zero otherwise.

10

11 The proxy observations are assumed to follow an unknown statistically linear relationship with the  
12 true precipitation at each location:

$$13 \quad Proxy_t = H_{Proxy,t} (\beta_1 Proxy_t + \beta_0 + \epsilon_{Proxy,t}) \quad (4)$$

14

15 again, the  $H_{Proxy,t}$  is a diagonal matrix with ones only for the locations with proxy observations,  
16 and the noise terms are iid normal draws:  $\epsilon_{Proxy,t} \sim N(0, \tau_{Proxy}^2)$

17

#### 18 **Prior level:**

19 To close the scheme, prior distributions must be specified for the eight scalar parameters  
20  $(\alpha, \mu, \sigma, \phi, \beta_1, \beta_2, \tau_{Inst}^2, \tau_{Proxy}^2)$  and the initial climate field (i.e. at the first time-step). We follow the  
21 approach in Tingley and Huybers (2010) and select prior distributions that are sufficiently diffuse to  
22 not have any important influence on the posterior distributions.

23

24 Using Bayes' rule the posterior distribution of each of the unknown variables can be calculated.  
25 Samples are drawn from this posterior distributions using a Gibbs sampler, with a Metropolis step  
26 (Gelman et al, 2003) to update  $\phi$ , the spatial range parameter. Before applying the BHM all the  
27 proxy time-series are standardized using the sample mean and standard deviation from the pseudo  
28 instrumental times-series at the same locations. The output of the Bayesian algorithm is not a  
29 unique reconstruction, but an ensemble of 1200 equally-probable draws all of them consistent with  
30 the model equations.

#### 31 2.4.2. Bayesian Hierarchical Modelling coupled to Clustering

32

33 Here we propose to couple the BHM with a clustering algorithm. The aim of the clustering step is to  
34 segregate South-eastern Asia into several clusters, according to similarities in the precipitation  
35 regimes during the pseudo-instrumental period. After the clustering, the BHM code is run within  
36 each cluster independently. Finally, all the results are merged together to produce the entire spatial





1 reconstruction over the post 850 period. The idea behind the clustering step is to reduce the  
2 complexity of the problem to be presented to the BHM algorithm, as after clustering the code does  
3 not have to deal with extreme differences in precipitation regimes (as dipole patterns at mountain  
4 ranges) and large number of grid cells.

5

6 We use a hierarchical agglomerative clustering technique. Each observation starts in its own cluster  
7 and pairs of clusters are agglomerated as one moves up in the hierarchy (Izenman, 2008). We select  
8 a complete-linking strategy: the distance between sets of observations is defined as the maximum of  
9 the pairwise distances between the observations in each of the sets. First, the method groups  
10 together the two closest observations, according to the selected distance, creating a cluster of two  
11 observations. Then, the sets whose distance is minimum are agglomerated together, iteratively  
12 repeating the process.

13

14 Here, the elements to cluster together are the different grid-points in South-eastern Asia. The input  
15 variables for the method are the pseudo-instrumental precipitation time-series at each of these  
16 locations. The distance between two points is defined as: One minus the correlation between the  
17 pseudo-instrumental precipitation time-series at these locations (points highly correlated display a  
18 small distance). In this way, the method groups together points whose pseudo-instrumental  
19 precipitation time-series are highly correlated.

20

21 For both, the annual and the decadal, reconstructions we select two cases: clustering into 5 and into  
22 10 groups (note that the clusters might be different when using the annual/decadal information, see  
23 Figure A2). We term the reconstructions in this category: BHM+5Clusters and BHM+10Clusters.

24

### 25 2.4.3. Analogue Method

26

27 The Analogue Method is a learning technique first introduced by Lorenz (1969) for weather  
28 forecasting. The technique uses predictors to determine the value of the target variable, based on the  
29 statistical relationship between them in a learning set: the so-called pool of possible analogues. The  
30 method can also be applied to produce a CFR. In our study and for each time step (year or decade),  
31 the predictor variables are the proxy records (38 predictors) and the target variable is the complete  
32 precipitation field at the given time-step. The learning set consists of all the time-steps in the  
33 instrumental period, i.e. all the time-steps in which we simultaneously have the information about  
34 proxy and target. The reconstruction of the precipitation field at time-step  $t$  is obtained as follows.  
35 First, a distance between time-steps is defined. Let  $t_i$  be a time-step included in the pool  
36 (instrumental period). Then, the distance between  $t$  and  $t_i$  is, in this paper, defined as the Euclidean  
37 distance between the vectors of proxy data at times  $t$  and  $t_i$ :



1 
$$d(t, t_i) = \sqrt{\sum_{j=1}^K (\text{Prox}(l_j, t) - \text{Prox}(l_j, t_i))^2} \quad (5)$$

2  
3 where  $\text{Prox}(l_j, t)$  is the value of the proxy at location  $l_j$  and time  $t$ . Locations  $l_1, \dots, l_K$  are all the  
4 proxy locations ( $K=38$ ). Second, the time-steps in the pool are ordered according to their distance  
5 from  $t$ . Third, the  $N$  closest time-steps are selected from the pool, and termed analogues:  $t_1, \dots, t_N$ .  
6 Finally, the precipitation reconstruction for time  $t$  is the mean of the precipitation field in the  $N$   
7 analogues:

8 
$$\text{Reconstruction}(t) = \frac{\text{Pr}(t_1) + \dots + \text{Pr}(t_N)}{N} \quad (6)$$

9  
10  $N$  can be any value between 1 and the total number of time-steps in the instrumental period (100 for  
11 yearly reconstruction, 14 for decadal reconstruction). On the one hand, using  $N=1$  will imply having  
12 a reconstruction identical to just 1 year of the instrumental period and, therefore, particularities of  
13 this year might be involved. On the other hand, using the maximal  $N$  implies just giving as  
14 reconstruction the mean during the instrumental period, which eliminates all the inter-annual or  
15 inter-decadal variability. In this paper we select as  $N$  intermediate values, considering  $N$   
16 approximately equal to 20% of the time-steps in the instrumental period: 20 for the annual  
17 reconstruction, 2 for the decadal reconstruction.

18

19 Note that in this manuscript we use the Analogue Method in its classical version (obtaining the pool  
20 of analogues from the observational data set) and not in combination with the use of an GCM to  
21 draw the Analogue cases from.

22

## 23 2.5. Skill Metrics

24

25 To evaluate the performance of the CFR methodologies we compare the reconstruction with the true  
26 precipitation field. We select three different skill metrics. The first skill metric, the Correlation  
27 Coefficient, evaluates the ability of the reconstruction to reproduce the temporal evolution of the  
28 target. At each grid point, we calculate the Pearson correlation between the reconstruction and the  
29 true precipitation time-series, considering the whole reconstruction period. As for the Bayesian  
30 algorithms we have an ensemble of reconstructions we first calculate the correlation of each of  
31 these ensembles with the true precipitation and, finally, we show the mean of these correlations.

32

33 The second skill metric quantifies the absolute biases of the reconstruction at each location. Instead  
34 of directly using the Root Mean Squared Error (RMSE), we compare the RMSE of the different  
35 reconstructions with the RMSE obtained with the simplest possible reconstruction: using the  
36 climatological mean during the instrumental period. In reconstruction studies, this is usually



1 referred to as the Reduction of Error (RE, Cook et al., 1994) and is defined, at each location  $l$ , as:

$$2 \quad RE(l) = 1 - \frac{\sum_t (Pr(l,t) - Reconstruction(l,t))^2}{\sum_t (Pr(l,t) - Climatology(l))^2} \quad (7)$$

3

4 where  $Reconstruction(l,t)$  is the reconstruction being evaluated at location  $l$  and time-step  $t$  and  
5  $Climatology(l)$  is the climatological mean at location  $l$ . The sum is done over all the time-steps  
6 within the reconstruction period. In this case for the Bayesian techniques, and to simplify the  
7 interpretation, we show this metric for the median reconstruction.

8

9 The last skill metric is especially designed to evaluate probabilistic ensemble forecasts of  
10 continuous predictands and is, therefore, particularly suitable for evaluating the Bayesian schemes.  
11 We use the Continuous Ranked Probability Score (Hersbach 2000; Wilks, 2011; Werner et al.,  
12 2018). The CRPS measures the difference between the accumulated probability density function  
13 and the step function that jumps from 0 to 1 at the observed value:

$$14 \quad CRPS = \int_{-\infty}^{\infty} (F(y) - F_0(y))^2 dy \quad (8)$$

$$15 \quad F_0(y) = \begin{cases} 0, & y < \text{observed value} \\ 1, & y \geq \text{observed value} \end{cases} \quad (9)$$

16 It has a negative orientation, meaning smaller values are better. This metric can only be provided  
17 for the Bayesian schemes and not for the Analogue reconstructions.

18

### 19 3. Results

20

21 In the following sub-sections we evaluate the ability of the different reconstruction techniques. In  
22 subsection 3.1 we select a pseudo-proxy scenario with medium noise-level (equivalent to a  
23 correlation with the target precipitation of 0.5) and evaluate the reconstruction schemes. In  
24 subsection 3.2, we assess the impact of the noise in the pseudo-proxies time-series on the quality of  
25 the reconstruction.

26

#### 27 3.1. Evaluation of Reconstruction Techniques: Medium-noise pseudo-proxy 28 case

29

30 As measures of performance we present the three selected skill metrics (see 2.3 for details), and in  
31 each case, we show the results at annual and at decadal resolution.



1

2 Figure 4 displays the Correlation Coefficient for the different reconstruction techniques. According  
3 to this skill measure, regardless of the method and resolution, proxy-rich East China (EChina, 20N-  
4 40N, 100E-120E) stands out as the best-reconstructed area. However, a fairly dense coverage by  
5 proxy records seems not to be a universal indicator of success, as North-Western Arid China  
6 (NWACHina, 40N-50N, 72.5E-90E) is highlighted as an area where the Bayesian algorithms are  
7 successful while the Analogue Method displays no ability. On the other hand, areas poorly covered  
8 by the pseudo-proxy network (south of 18N, North-Eastern Asia and South of Tibet at longitudes  
9 85E-95E) are the regions where the correlation coefficient is lowest.

10

11 For the annual-resolution reconstructions, the best performance is obtained by the BHM technique,  
12 showing a spatial mean correlation with the target of 0.4 (Fig. 4a). Coupling the BHM with  
13 clustering partially deteriorates the results, with the correlation coefficient severely dropping over  
14 the proxy-rich EChina region (Fig. 4b and 4c). Meanwhile, the performance of the Analogue  
15 Method is inferior: the Correlation Coefficient spatial mean is 0.25 and there is no skill in  
16 reconstructing precipitation north of 42N despite the fact that pseudo-proxies are located in that  
17 region (Fig. 4d).

18

19 For the decadal-resolved reconstructions the difference between the Bayesian methods and the  
20 Analogue is even larger. In terms of the Correlation Coefficient measure the BHM (Analogue  
21 Method) is the best (worst) performing with a spatial average of 0.37 (0.1). Among the Bayesian  
22 schemes, the cluster coupling maintains the skill levels in all regions except India, where lower  
23 correlation values are obtained. The Analogue Method shows a much constrained geographical  
24 skill, with correlation values above 0.2 only over EChina and central India.

25

26 In general, for each of the methods, the Correlation Coefficient is higher for the annually-resolved  
27 than for the decadal-resolved reconstruction. One exception to that is the BHM+5Clusters over  
28 EChina. This behaviour is probably derived from the clustering division (see Figure A2).

29

30 Figure 5 shows the results for the RE index. In most of the grid-points the RE index is positive,  
31 indicating a reduction of the error in comparison to forecasting the instrumental-period climatology  
32 as reconstruction. For all the Bayesian methods and both time-resolutions the highest skill is found  
33 in regions with high density of pseudo-proxy information. Again, the Analogue Method shows a  
34 clear inferior performance over NWACHina, in spite of the considerable number of pseudo-proxy  
35 locations present there.

36

37 For the annual reconstruction, improvements from climatology are found for the Bayesian  
38 approaches in EChina, NWACHina, Mongolia and, to a lesser extent, in central India (Fig. 5a, 5b



1 and 5c). For the Analogue Method, the improvement with respect to climatology is confined only to  
2 EChina and central India, and the improvement is weaker than with the Bayesian techniques (Fig.  
3 5d).

4

5 For the decadal data, similar results are obtained. However, the RE index is notably negative in  
6 some grid-points for the BHM+5clusters (mainly in the northern-most extent of the study region;  
7 Fig. 5f) and the Analogue cases (everywhere with exception of EChina; Fig. 5h).

8

9 Figure 6 displays the results for the CRPS metric, for the probabilistic methods (Bayesian schemes).  
10 For this metric, the annually-resolved (decadally-resolved) reconstructions have a CRPS of 190  
11 mm/month (22 mm/month), compared to the target precipitation spatially-averaged standard  
12 deviation of 34 mm/month (11 mm/month) for annual (decadal) data. This indicates that the  
13 methods have more problems in reproducing the expected probability distribution functions in the  
14 annual case.

15

16 For the annual resolution reconstructions there is almost no noticeable difference in the  
17 performance of the three Bayesian schemes. For this metric, the region of best performance is  
18 NWACHina. In this case, the performance over the proxy-rich EChina is intermediate (unlike with  
19 the Correlation Coefficient and RE Index metrics). For the decadal resolution reconstructions, the  
20 performance among the methods is quite different. While the spatial mean is in all the three cases  
21 similar (around 22 mm/month), the spread among grid points is much higher for the  
22 BHM+10Clusters scheme. In particular, for the 10 clusters scheme the skill over China and the  
23 South-East of the study region is much higher than in the other methods. In general, the regions  
24 with a dense proxy network display better performance levels and central India and the North-East  
25 of the study area stand out as low-performing areas for all the three methodologies.

26

27 Three main conclusions can be drawn from the experiments above: First, proxy-depleted areas can  
28 not be successfully reconstructed. Second, the Bayesian schemes are superior to the Analogue  
29 Method in all metrics (this difference is particularly acute over NWACHina where the Analogue  
30 fails despite the relatively good coverage by proxy data). Third, among the Bayesian algorithms  
31 there is no clear superiority.

### 32 3.2. Effect of noise in Pseudo-proxy records

33

34 Next, we evaluate the impact of noise in the pseudo-proxy time-series on the skill of the  
35 reconstruction techniques. We focus on two schemes: one Bayesian (BHM+5Clusters, selected for  
36 its balance between skill and computational requirements, as shown in subsection 3.1) and the  
37 Analogue Method. We work with four noise levels for the pseudo-proxy time-series: high-noise



1 (correlation with truth: 0.3), medium-noise (correlation with truth: 0.5), low-noise (correlation with  
2 truth: 0.7) and perfect-proxy (correlation with truth: 1). Note that the medium-noise proxies case  
3 corresponds to the level used through sub-section 3.1. To simplify and summarize the results, in this  
4 subsection we display the reconstructions performance in terms of only one skill measure: the  
5 Correlation Coefficient.

6

7 Figure 7 shows the dependency of the Correlation Coefficient, averaged in space, with noise levels  
8 in the pseudo-proxies records. At annual resolution, the skill of the methods increases in an almost  
9 linear way with the quality of the pseudo-proxies records, except for a drop in the Bayesian skill in  
10 the No-noise scenario. The BHM+5Clusters performance is better than the Analogue Method in all  
11 cases except the No-noise one. For high-noise proxies the skill of the BHM+5Clusters (Analogue  
12 Method) is 0.23 (0.18), while in the perfect-proxy scenario the BHM+5Clusters (Analogue Method)  
13 reaches 0.30 (0.42). For decadal-resolved reconstructions the picture is quite different. The  
14 Bayesian approaches show a quasi-constant skill for the medium, low and no noise examples  
15 (around 0.33) and the Analogue Method performs poorly showing for all the noise types a skill  
16 between 0.09 and 0.15. While for the Bayesian schemes the spatial average skill for the annual or  
17 decadal resolutions is similar, the difference between annual versus decadal is important in the  
18 Analogue case. To complement the spatially-averaged-information, Figures 8 and 9 show the  
19 sensitivity of the correlation skill measure field to the noise-levels in the pseudo-proxies for the  
20 BHM+5Clusters and the Analogue Method, respectively.

21

22 For the Bayesian algorithm (Fig. 8), the perfect-proxy case shows high performance over  
23 NWChina, EChina and North-East of the study area, at annual and decadal resolutions. For the  
24 annual reconstruction, the skill of the scheme is low southward of 25N and over some grid cells in  
25 the north of the area. For the decadal reconstruction, the same areas are also problematic and, in  
26 addition, most of India is not well reconstructed. In general, as the noise level in the input pseudo-  
27 proxies increases the performance of the method deteriorates and for the high-noise case only East  
28 China and the NW of the study region show a moderate success.

29

30 Figure 9 presents the Analogue Method performance. For annual resolution, in the case of perfect  
31 pseudo-proxies, the method is successful in the central part of the study area (between 15N and  
32 45N), while the northern and southern most extremes are not well reconstructed. However, the  
33 decadal counter-part is only skilful in EChina. In the high-noise end of the spectrum, the Analogue  
34 Method only shows a satisfactory performance in EChina, between 20N-40N (25N-35N) for the  
35 annually-resolved (decadally-resolved) reconstruction.

36

37 To summarize, as expected, the noise in the pseudo-proxy time-series is important for the quality of  
38 the reconstruction, as the latter rapidly decreases with the noise level. However, particularly for the  
39 decadal reconstructions, the reconstruction quality depends less on the noise level for the levels



1 medium, high and no noise, as only minor differences are noticed.

2

#### 3 4. Summary and Conclusions

4

5 This study evaluates the ability of several statistical techniques to reconstruct the precipitation field  
6 over South-eastern Asia in a PPE setting. The reconstructions are performed using 1156 years of  
7 model simulation (corresponding to the period 850–2005), at annual and at decadal resolution. The  
8 techniques used are: BHM, BHM coupled with clustering (dividing South-eastern Asia into 5 or 10  
9 clusters) and the Analogue Method. While the Analogue Method is a classical approach and has  
10 been widely used, the Bayesian variants are novel for the hydro-climatological reconstructions’  
11 field, being this the first time results are reported for the Asian continent. Moreover, the coupling of  
12 the Bayesian modelling with clustering algorithms is also an innovation that could potentially lead  
13 to a more wide-spread application of these computationally-intensive processes.

14

15 We find that for all the algorithms and resolutions a high-density of pseudo-proxy information is a  
16 necessary but not sufficient condition for a successful reconstruction. On one hand, the lack of  
17 proxy data over regions such as the NE of the study area, south of Tibet and south of 20N,  
18 determines that none of the methods is capable of delivering a skilful reconstruction. On the other  
19 hand, a good performance over the proxy-rich areas of EChina and NWChina is not guaranteed  
20 just by the amount of data present there: while all the methods are highly successful over EChina,  
21 only the Bayesian algorithms deliver quality reconstructions over NWChina.

22

23 We hypothesise a couple of reasons for the failure of the Analogue Method over NWChina: first,  
24 the semi-arid precipitation regime dominant in the area and second an insufficient number of  
25 analogues in the pool. However, as the method is unsuccessful both at annual and decadal  
26 resolutions we think that the number of elements in the pool of analogues is not an important  
27 variable and that the main cause for the failure resides in the fact that non-normal behaving time-  
28 series are more difficult to mimic by analogues than Gaussian-behaving ones. In general, for both  
29 the annual and the decadal reconstructions, while the Bayesian techniques are superior to the  
30 Analogue Method, among the three Bayesian schemes the differences in skill are not extremely  
31 notorious. Noting that the Bayesian technique without any form of pre-clustering of the area of  
32 interest (BHM) is extremely computationally expensive, coupling it with a clustering scheme  
33 (BHM+5Clusters or BHM+10Clusters) seems to be a good compromise between success of the  
34 reconstruction and computational demand.

35

36 We also find that the quality of the final reconstructions is highly sensitive to the noise levels  
37 included in the input pseudo-proxy data, being those variables negatively correlated. However, for



1 decadal resolutions the methods' performances are quite similar for levels of medium, low or no  
2 noise. Only under a perfect-proxy (no-noise) scenario and at annual-resolution is the Analogue  
3 Method capable of overperforming the Bayesian schemes over most areas. However, even in this  
4 ideal no-noise case NWACHina remains elusive for the Analogue methodology.

5

6 As a summary, we find that for millennium-length precipitation reconstructions over South-eastern  
7 Asia a dense network of proxy information is mandatory for success, highlighting the complex  
8 nature of the precipitation field in the area of study. Among the selected algorithms, the Bayesian  
9 techniques perform generally better than the Analogue Method, being the difference in abilities  
10 highest over the semi-arid Northwest and in the decadal-resolution framework. The superiority of  
11 the Bayesian approach indicates that directly modelling the space and time precipitation field  
12 variability encapsulates more added value than just relying in similarities within a restricted pool of  
13 observational analogues, in which certain regimes might not be present.

14

15 A natural next step is to implement real-world reconstructions of precipitation in the region of  
16 continental South-eastern Asia. These PPE are auspicious for such a future endeavour, as some  
17 moderate skill can be expected in most of the region. Nevertheless, it is important to acknowledge  
18 that these experiments are highly idealised and that real-world data might incorporate additional  
19 constraints and challenges. Additionally, more PPE could be also designed lifting some of the  
20 simplifications assumed here. For example, while here we only took proxy time-series that cover  
21 the whole period of interest, with the same temporal resolution, same signal to noise relation and  
22 same relationship with the underlying hydroclimatic variable of interest, some of these constrains  
23 could be modified to better resemble reality.

24

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29

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1 Table 1: List of the real-world Proxy records used to select the locations of the pseudo-proxy  
 2 network.  
 3

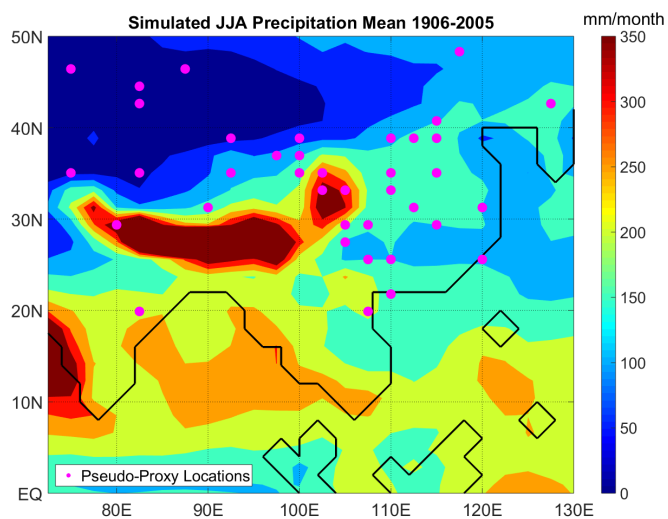
	Site	Longitude	Latitude	Archive	Target Season	Reference
1	Anyemaqen Mountains	99.5	34.5	Tree	Annual	Gou et al, 2010
2	Balkhash Basin	75	46.9	Pollen	Annual	Feng et al., 2013
3	Buddha Cave	109.5	33.4	Speleothem	Annual	Paulsen et al., 2003
4	Central India Composite	82	19	Speleothem	Summer	Sinha et al., 2011
5	Delingha	97.38	37.38	Tree	Annual	Yang et al., 2014
6	Dharamjali Cave	80.21	29.52	Speleothem	Annual	Sanwal et al., 2013
7	Dongge Cave	108.8	25.28	Speleothem	Annual	Wang et al., 2005
8	Eastern Tibetan Plateau	102.52	32.77	Lake	Annual	Yu et al., 2006
9	Furong Cave	107.9	29.29	Speleothem	Summer	Li et al, 2011
10	Gonghai Lakee	112.23	38.9	Lake	Summer	Liu et al, 2011
11	Great Bend of the Yellow River	115	35	Documentary	Annual	Gong and Hamed 1991
12	Guliya	81.48	35.28	Ice	Annual	Yao et al., 1996
13	Haihe River Basin	116	40	Documentary	Annual	Yan et al., 1993
14	Hani	126.51	42.21	Lake	Annual	Hong et al., 2005
15	Heihe River Basin	100	38.2	Tree	Annual	Yang et al., 2012
16	Heshang Cave	109.36	19.41	Speleothem	Annual	Hu et al., 2008
17	Huangye Cave	105.12	33.92	Speleothem	Annual	Tan et al., 2011
18	Huguangyan Lakee	110.28	21.15	Lake	Annual	Zeng et al., 2012
19	Jianghuai	113.5	31.5	Documentary	Annual	Zheng et al., 2006
20	Jiangnan	115	30	Documentary	Annual	Zheng et al., 2006
21	Jiuxian Cave	109.1	33.57	Speleothem	Summer	Cai et al., 2010
22	Karakorum Mountains	74.93	35.9	Tree	Annual	Treydte et al., 2006
23	Kesang Cave	81.75	42.87	Speleothem	Annual	Zheng et al., 2012



24	Kusai Lake	93.25	35.4	Lake	Summer	Liu et al., 2009
25	Lake Aibi	82.84	44.9	Lake	Annual	Wang et al., 2013
26	Lake Gahai	102.33	34.24	Lake	Annual	He et al., 2013
27	Lake Hulun	117.5	49	Lake	Annual	Zhai et al., 2011
28	Lake Nam Co	90.78	30.73	Lake	Summer	Kasper et al., 2012
29	Lake Xiaolongwan	126.35	42.3	Lake	Annual	Chu et al., 2009
30	Lonxi Area	105	30	Documentary	Annual	Tan et al., 2008
31	North China Plains	115	38	Documentary	Annual	Zheng et al., 2006
32	North-eastern Tibetan Plateau	98	37	Tree	Annual	Yang et al., 2014
33	Qaidam Basin	97.5	37.2	Tree	Annual	Yin et al., 2008
34	Qaidam Basin	97.5	37.2	Tree	Annual	Wang et al., 2013
35	Qigai Nuur	109.5	39.5	Pollen	Annual	Sun et al., 2013
36	Qilian Mountains	99.5	38.5	Tree	Annual	Zhang et al., 2011
37	Qinghai Province	99	37	Tree	Annual	Sheppard et al., 2004
38	Southern China	110	25	Documentary	Annual	Qian et al., 2003
39	Sugan Lake	93.9	38.85	Lake	Annual	He et al., 2013
40	Tsuifong Lake	121.6	24.5	Lake	Annual	Wang et al., 2013
41	Wanxiang Cave	105	33.19	Speleothem	Annual	Zhang et al., 2008
42	Wulungu Lake	87.15	47.15	Pollen	Annual	Liu et al., 2008
43	Yangtze Delta	121	32	Documentary	Annual	Zhang et al., 2008
44	Yangtze Delta	120	32	Documentary	Annual	Jiang et al., 2005
45	Yangtze Delta	115	30	Documentary	Annual	Qian et al., 2003
46	Yellow River	110	35	Documentary	Annual	Qian et al., 2003
47	Zhijin Cave	105.84	26.73	Speleothem	Summer	Kuo et al., 2011



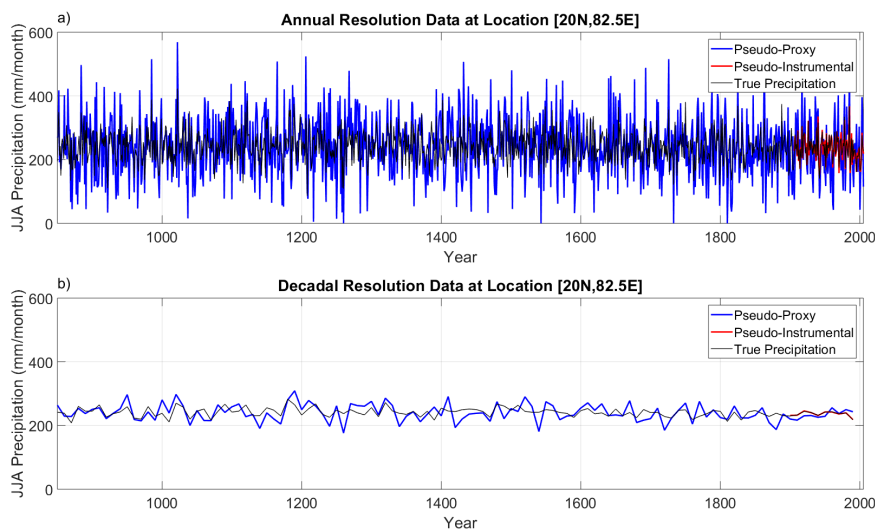
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2 **Figure 1: Simulated mean JJA precipitation (mm/month) during the instrumental period**  
3 **(years 1906-2005) in Asia. Magenta dots: Pseudo-Proxy network.**



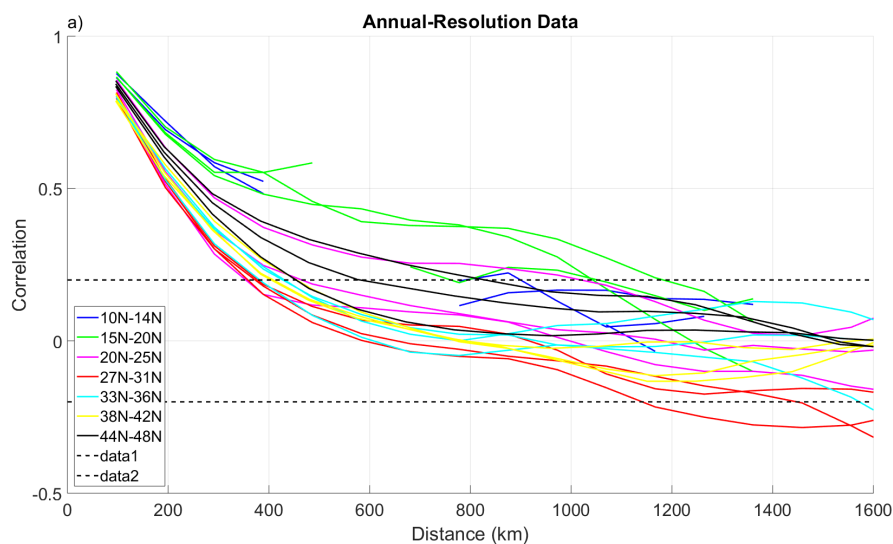
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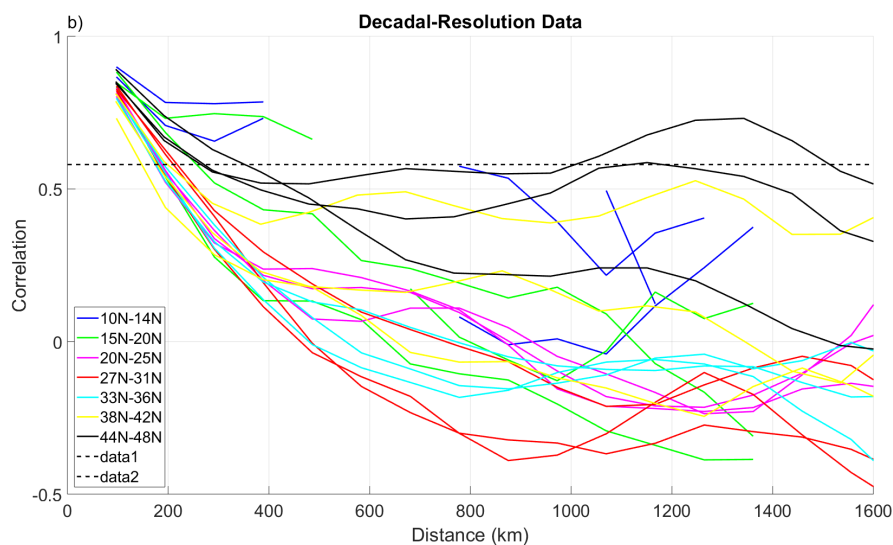
2 **Figure 2: Example of Pseudo-Proxy, Pseudo-Instrumental and True precipitation time-series**  
3 **at location [20N,82.5E]. a) Annually-resolved data b) Decadally-resolved data.**



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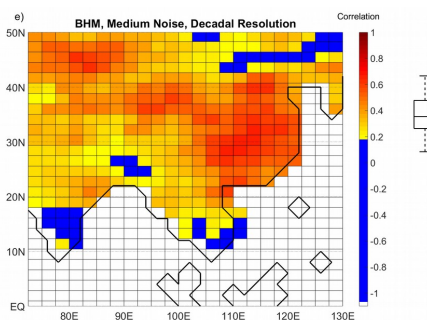
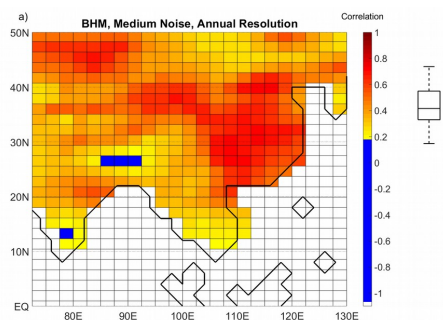
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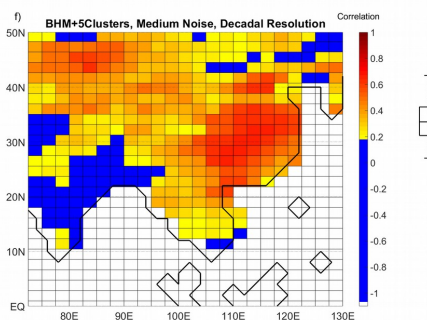
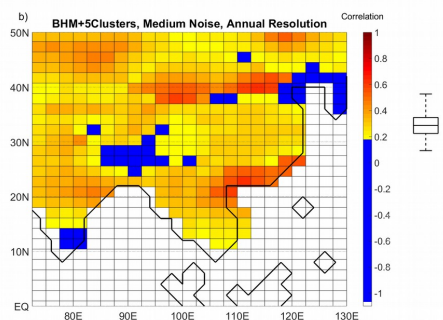
3 **Figure 3: Correlation of Simulated JJA precipitation time-series across different latitudinal**  
4 **bands, versus distance. Only the instrumental period (years 1906-2005) and the grid-points in**  
5 **continental Asia are considered for the calculation. a) Annual-resolution Data, b) Decadal-**  
6 **resolution Data. Dashed horizontal lines indicate the thresholds of statistical significance at a**  
7 **95% confidence level according to the t-student test.**



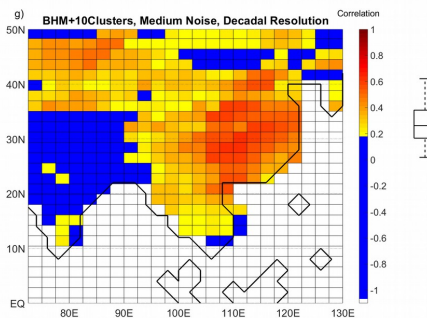
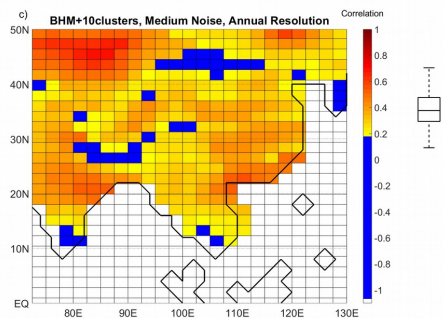
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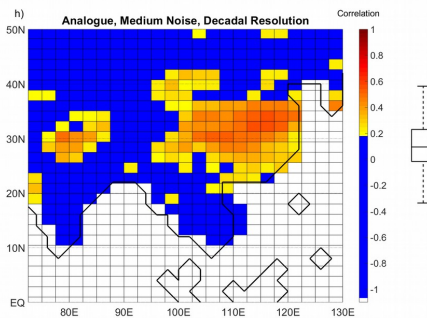
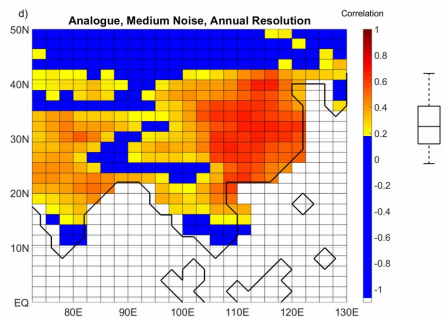
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**Figure 4: Correlation between Target Precipitation and different Reconstructions, at each grid point. Left: Annually-resolved data. Right: Decadally-resolved data. a and e: BHM. b and f: BHM + 5Clusters. c and g: BHM + 10 Clusters. d and h: Analogue Method. The boxplots (indicating median, 25% and 75% percentiles and non-outlier limits) to the right of the colour bars show the distribution of the grid point Correlation Coefficients.**

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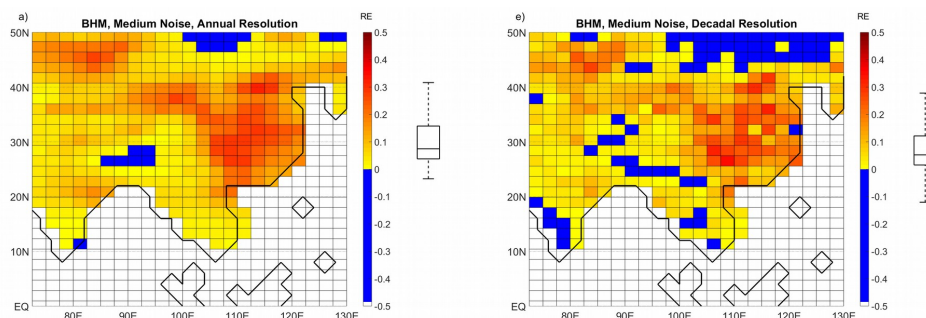
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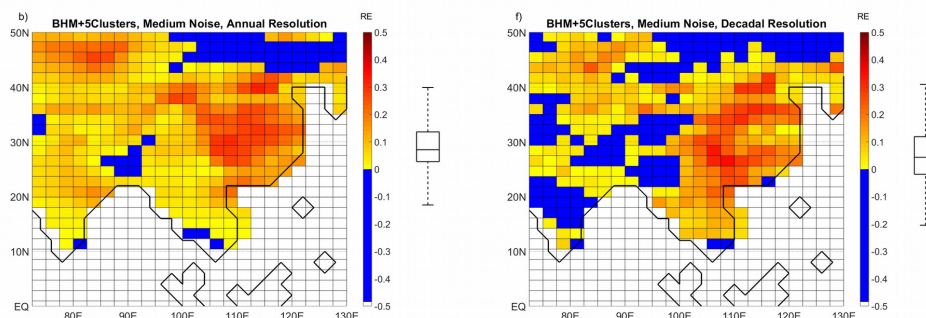
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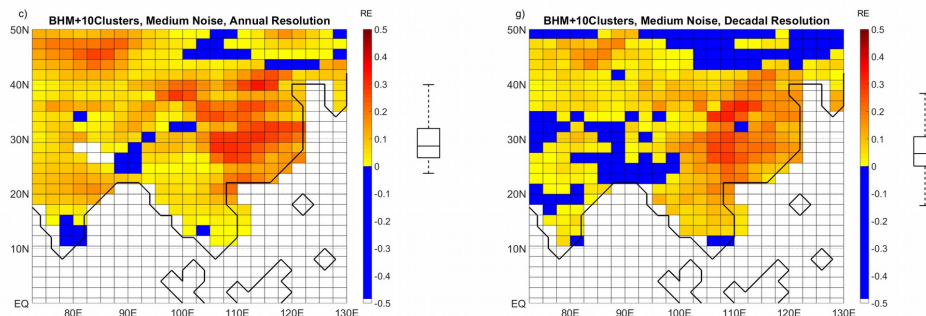
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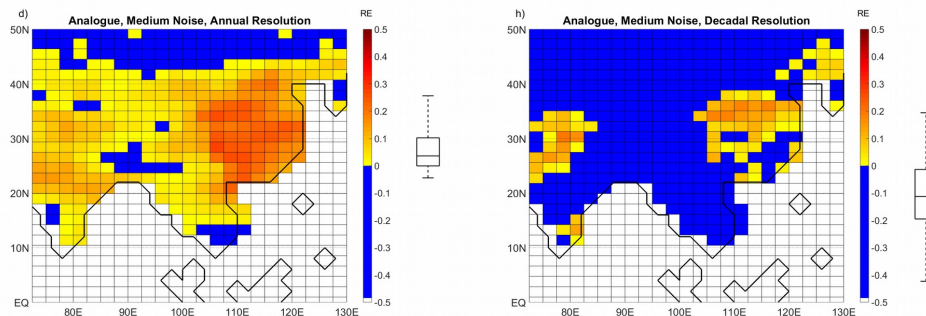
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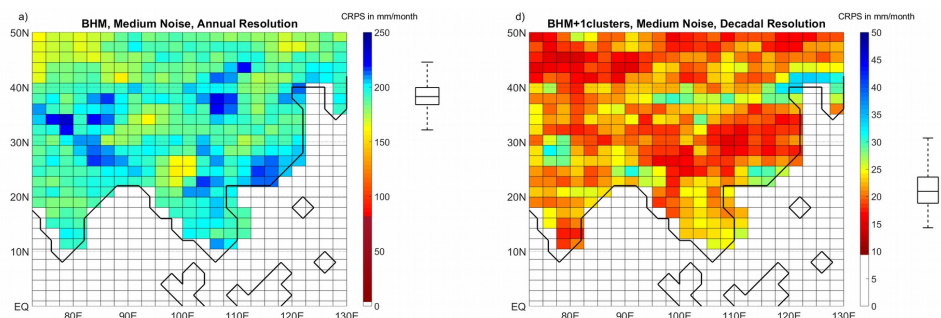


5 **Figure 5: RE Index for different Reconstructions, at each grid point. Left: Annually-resolved**  
 6 **data. Right: Decadally-resolved data. a and e: BHM. b and f: BHM + 5Clusters. c and g:**  
 7 **BHM + 10 Clusters. d and h: Analogue Method. The boxplots (indicating median, 25% and**  
 8 **75% percentiles and non-outlier limits) to the right of the colour bars show the distribution**  
 9 **of the grid point RE Index.**

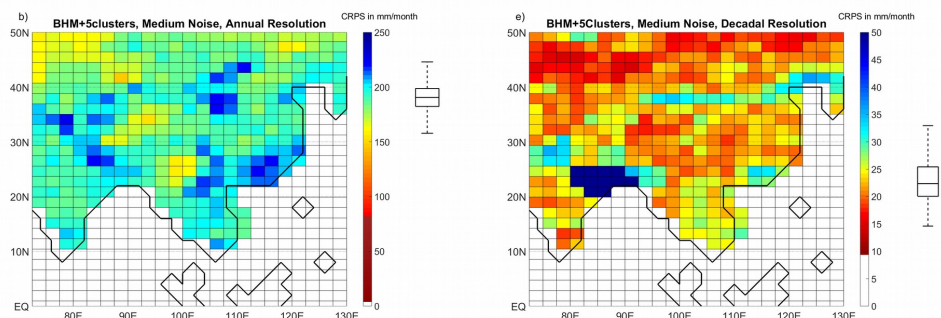




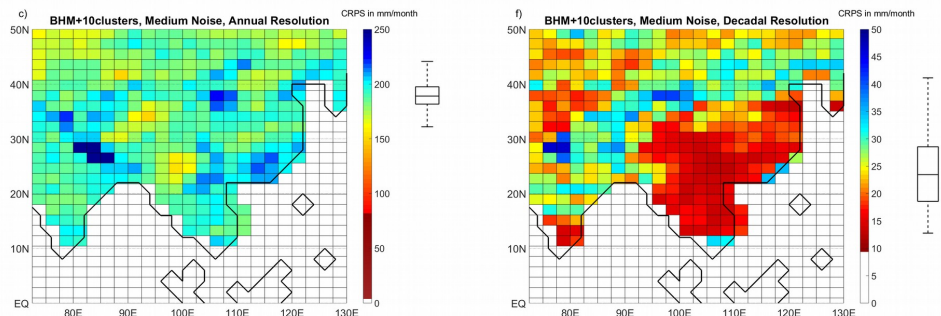
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**Figure 6: CRPS for different Reconstructions, at each grid point. Left: Annually-resolved data. Right: Decadally-resolved data. a) and d): BHM Reconstruction. b) and e): BHM+5Clusters. c) and f): BHM + 10 Clusters. The boxplots (indicating median, 25% and 75% percentiles and non-outlier limits) to the right of the colour bars show the distribution of the grid point CRPS.**

5

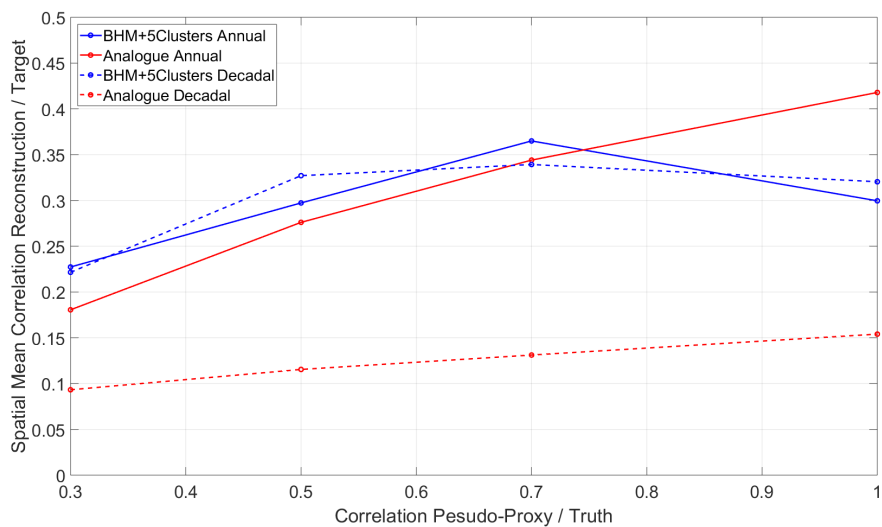
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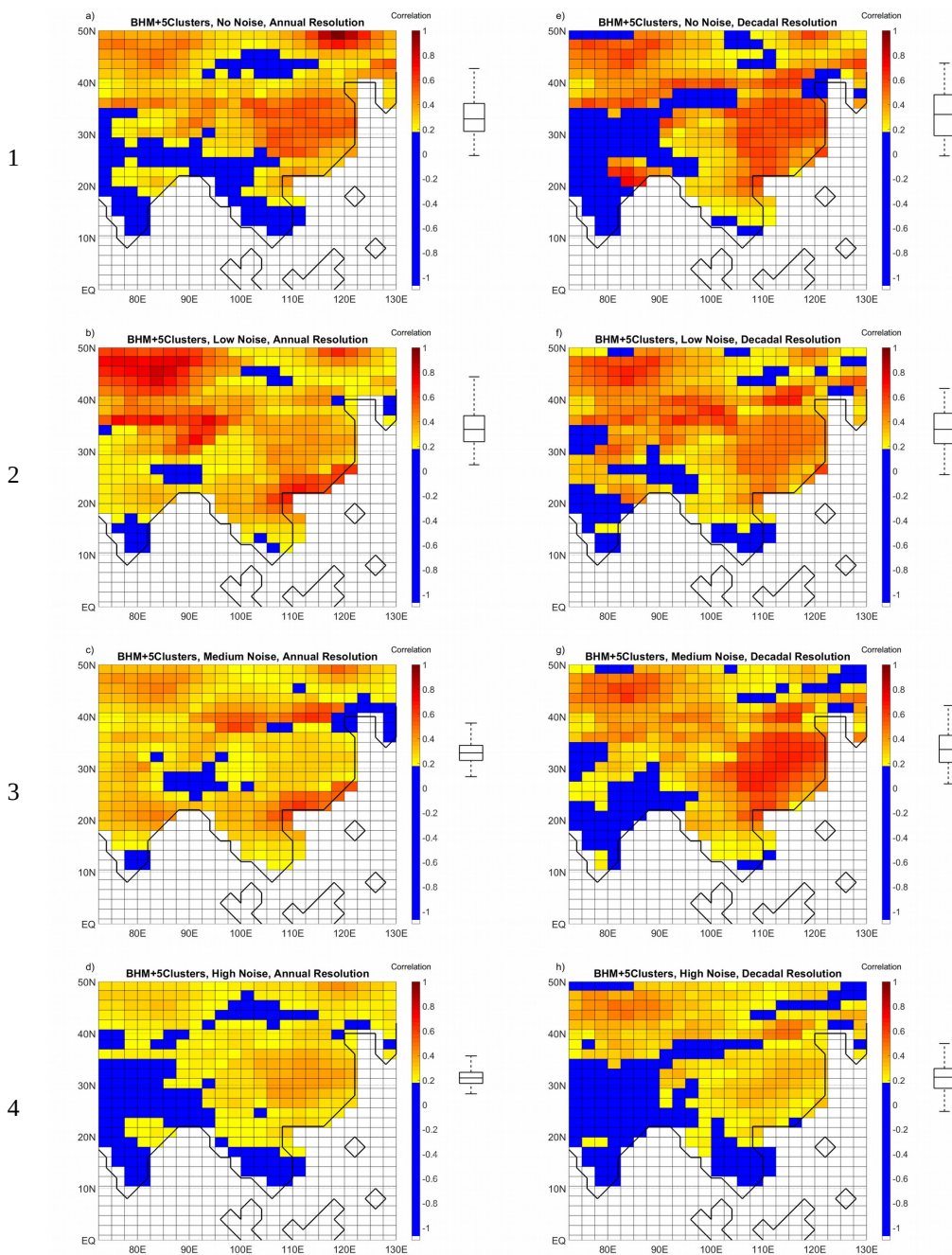
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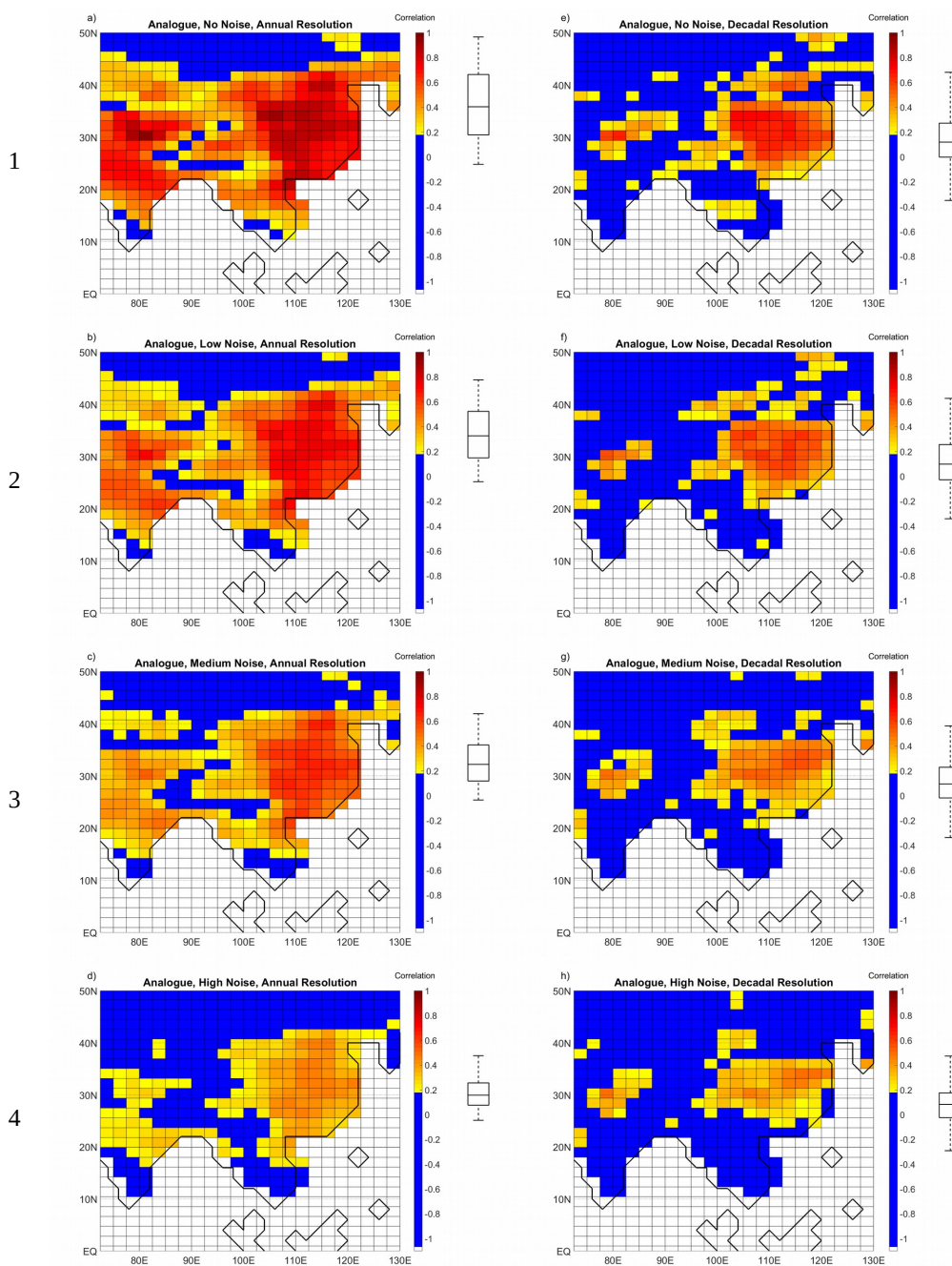
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2 **Figure 7: Spatial Mean Correlation Skill of Reconstruction techniques for different noise**  
3 **levels (expressed here in terms of the correlation between the pseudo-proxy and truth).**



5 **Figure 8: BHM+5Clusters performance in terms of Correlation with target for different levels**  
 6 **of noise at annual (left column) or decadal (right column) resolution. A and b) No noise. C and**  
 7 **d) low noise. E and f) Medium-level noise. G and h) High noise.**  
 8 **The boxplots (indicating median, 25% and 75% percentiles and non-outlier limits) to the**  
 9 **right of the colour bars show the distribution of the grid point Correlation Coefficients.**



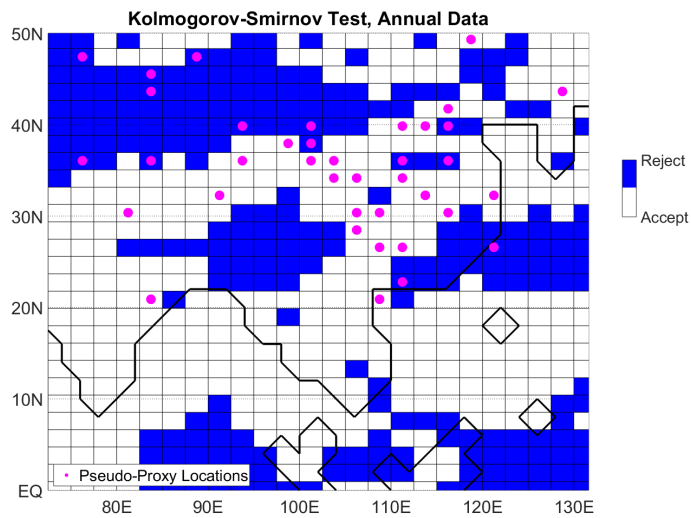
5 **Figure 9: Analogue Method performance in terms of Correlation with target for different**  
 6 **levels of noise at annual (left column) or decadal (right column) resolution. A and b) No noise.**  
 7 **C and d) low noise. E and f) Medium-level noise. G and h) High noise.**  
 8 **The boxplots (indicating median, 25% and 75% percentiles and non-outlier limits) to the**  
 9 **right of the colour bars show the distribution of the grid point Correlation Coefficients.**



1 **Appendix A**

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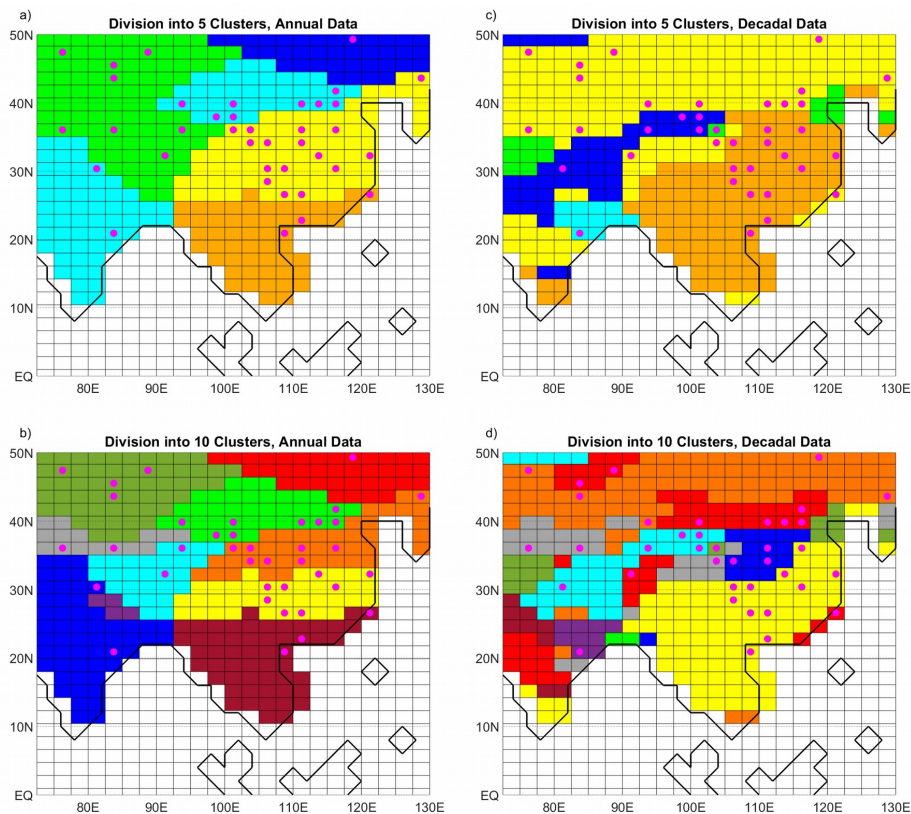
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6 **Figure A1: Kolmogorov-Smirnov Normality test on the Simulated JJA Precipitation during**  
7 **instrumental period (years 1906-2005, at annual resolution): Blue: The Normality hypothesis**  
8 **is rejected, White: the Normality hypothesis is not be rejected, at a 95% confidence level.**  
9 **Magenta dots: Pseudo-Proxy network.**



1



3

4 **Figure A2: Divisions into Clusters (in each plot different colors indicate different Clusters),**  
5 **using the simulated JJA precipitation in the instrumental period (years 1996-2005) as input. a)**  
6 **Annual Data, division into 5 Clusters, b) Annual Data, division into 10 Clusters, c) Decadal**  
7 **Data, division into 5 Clusters, d) Decadal Data, division into 10 Clusters. Magenta dots:**  
8 **Pseudo-Proxy network.**