1	Metrics for linking emissions of gases and aerosols to global precipitation changes
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Abstract

- 9 Recent advances in understanding have made it possible to relate global precipitation changes
- directly to emissions of particular gases and aerosols that influence climate. Using these
- advances, new indices are developed here called the Global Precipitation-change Potential for
- pulse (GPP_P) and sustained (GPP_S) emissions, which measure the precipitation change per
- unit mass of emissions.
- 14 The GPP can be used as a metric to compare the effects of emissions. This is akin to the
- 15 global warming potential (GWP) and the global temperature-change potential (GTP) which
- are used to place emissions on a common scale. Hence the GPP provides an additional
- perspective of the relative or absolute effects of emissions. It is however recognised that
- precipitation changes are predicted to be highly variable in size and sign between different
- regions and this limits the usefulness of a purely global metric.
- 20 The GPP_P and GPP_S formulation consists of two terms, one dependent on the surface
- 21 temperature change and the other dependent on the atmospheric component of the radiative
- 22 forcing. For some forcing agents, and notably for CO₂, these two terms oppose each other –
- as the forcing and temperature perturbations have different timescales, even the sign of the
- 24 absolute GPP_P and GPP_S varies with time, and the opposing terms can make values sensitive
- 25 to uncertainties in input parameters. This makes the choice of CO₂ as a reference gas
- problematic, especially for the GPP_S at time horizons less than about 60 years. In addition,
- 27 few studies have presented results for the surface/atmosphere partitioning of different
- 28 forcings, leading to more uncertainty in quantifying the GPP than the GWP or GTP.
- 29 Values of the GPP_P and GPP_S for five long- and short-lived forcing agents (CO₂, CH₄, N₂O,
- 30 sulphate and black carbon (BC)) are presented, using illustrative values of required
- 31 parameters. The resulting precipitation changes are given as the change at a specific time
- 32 horizon (and hence they are end-point metrics) but it is noted that the GPPs can also be
- interpreted as the time-integrated effect of a pulse emission. Using CO₂ as references gas, the
- 34 GPP_P and GPP_S for the non-CO₂ species are larger than the corresponding GTP values. For
- 35 BC emissions, the atmospheric forcing is sufficiently strong that the GPPs is opposite in sign
- 36 to the GTP_S. The sensitivity of these values to a number of input parameters is explored.
- 37 The GPP can also be used to evaluate the contribution of different emissions to precipitation
- 38 change during or after a period of emissions. As an illustration, the precipitation changes
- resulting from emissions in 2008 (using the GPP_P) and emissions sustained at 2008 levels
- 40 (using the GPPs) are presented. These indicate that for periods of 20 years (after the 2008
- 41 emissions) and 50 years (for sustained emissions at 2008 levels) methane is the dominant
- driver of positive precipitation changes due to those emissions. For sustained emissions, the
- sum of the effect of the 5 species included here does not become positive until after 50 years.
- by which time the global surface temperature increase exceeds 1 K.

1. Introduction

- 47 A broad range of emissions of gases and aerosols influence climate, either directly or
- indirectly. That influence depends on the characteristics of the gases and aerosols, such as
- 49 their lifetime, and their ability to influence the radiation budget. The conventional cause-and-
- effect chain links emissions to changes in concentrations, which then cause a radiative
- forcing with subsequent downstream effects on, for example, temperature, precipitation and
- sea level. By exploiting understanding of the characteristics of the gases and aerosol, in
- 53 concert with simplified descriptions of the climate system, it is possible to develop simple
- methodologies that relate emissions directly to climate impacts, rather than having to
- explicitly account for the intermediate steps. Such methodologies have pedagogic value in
- making clearer the link between emissions (rather than, for example, concentration changes)
- and climate response and they also have potential applications. The purpose of this paper is to
- present a methodology that links global-mean precipitation directly to emissions of different
- 59 gases and aerosols. This exploits recent advances in understanding of how radiative forcing
- 60 (RF) and temperature change influence precipitation change. The methodology presented
- here yields what we call the Global Precipitation-change Potential (GPP), which is the global-
- mean precipitation change per unit mass of emission. The GPP is presented for both pulse
- and sustained emissions.
- The impact of climate change depends on more than just global temperature change. Hence
- 65 the development of a methodology linking emissions directly to precipitation is attractive.
- However, precipitation change is much less amenable to a global representation than
- 67 temperature change. Average surface temperature response to increased concentrations of
- greenhouse gases is largely the same sign over the whole planet, the temperature changes are
- 69 coherent on large spatial scales, and climate models largely agree on the pattern of
- temperature change, if not the absolute size (e.g. Knutti and Sendláček 2012). By contrast,
- 71 precipitation changes vary regionally in sign, are spatially much more variable and there is
- much less agreement between climate models on the patterns of response (e.g. Knutti and
- 73 Sendláček 2012).
- Part of the spatial variability in precipitation response is due to changes in atmospheric
- 75 circulation in response to forcing, and also due to model internal variability. Nevertheless, for
- increased temperatures, there is a component of the precipitation response which has a
- 77 regionally coherent pattern. Increases and decreases in precipitation are largely reflective of
- an amplification of precipitation minus evaporation fields, primarily explained by increasing
- 79 concentrations of water vapour with warming (as expected from the Clausius-Clapeyron
- 80 equation); this leads to systematic increases and decreases in precipitation depending on the
- 81 region (e.g. Held and Soden, 2006, Liu and Allan 2013). These changes are superimposed on
- a global-average increase in precipitation. Hence, when coupled with changes in temperature,
- 83 changes in global-mean precipitation can be taken as being a useful an indicator of the size of
- 84 disturbance of the global hydrological cycle. In more idealised experiments with one climate
- model, Shindell et al. (2012) have demonstrated a link between radiative forcing (due to a
- variety of forcing mechanisms) in specific latitude bands to precipitation change in a number
- of selected regions; their precipitation change per unit radiative forcing was called a

- 88 "Regional Precipitation Potential", which is distinct from the framework here, where the
- 89 precipitation change is directly related to emissions.
- One potential application of the GPP is to place emissions of different species on a common
- scale, in a similar way to the GWP. The 100-year time-horizon GWP (GWP(100)) is used by
- 92 the Kyoto Protocol to the United Nations' Framework Convention on Climate Change to
- place emissions of many relatively well-mixed non-CO₂ greenhouse gases on a so-called
- 94 "CO₂-equivalent scale"; this is necessary for the type of multi-gas treaty that the Kyoto
- 95 Protocol represents. Metrics such as the GWP can also be used in life-cycle assessment and
- carbon footprint studies, for assessing possible mitigation strategies, for example in particular
- 97 economic sectors, and can extend beyond the gases included in the Kyoto Protocol (see e.g.,
- 98 Fuglestvedt et al. 2010, Deuber et al. 2014).
- 99 The GWP characterises the RF in response to a pulse emission of a substance, integrated over
- some specified time horizon. It is normally expressed relative to the same quantity for an
- equal-mass emission of CO₂. The GWP has enabled the multi-gas operation of the Kyoto
- 102 Protocol but has also been the subject of criticism for some applications (e.g., Myhre et al.
- 103 (2013), Pierrehumbert (2014) and references therein). This is partly because the use of time-
- integrated RF does not clearly relate to an impact of climate change (such as temperature
- 105 change) and also because it contains value judgements (particularly the choice of time
- horizon) that cannot be rigorously justified for any particular application (Myhre et al., 2013).
- Metrics that extend beyond time-integrated forcing have also been proposed. The GTP (e.g.,
- Shine et al. 2007; Myhre et al. 2013) characterises the global-mean surface temperature
- 109 change at some time after an emission. It may be more applicable to policies that aim to
- restrict temperature change below a given target level. The GTP is also subject to criticism
- and the need for value judgements when choosing time horizons (Myhre et al. 2013).
- Nevertheless the GTP (and its variants, such as the mean global temperature-change potential
- (e.g., Gillett and Matthews 2010, Deuber et al. 2014)) and integrated temperature potential
- (e.g., Peters et al. 2011, Azar and Johansson, 2012) do at least extend to a parameter
- 115 (temperature change) more obviously related to a climate change impact. Metrics can also be
- derived numerically on the basis of the contribution of an emission of a component at a given
- time, to temperature change during some future period, as simulated by a simple climate
- model driven by a specific emissions scenario (e.g. Tanaka et al. 2009). Sterner et al. (2014)
- recently presented a metric for sea-level rise. Metrics can be extended to the economic effects
- of an emission (for example the Global Cost Potential and Global Damage Potential), by
- relating the metrics to costs and damages (e.g., Johansson 2012) and in certain restrictive
- cases these can be shown to have equivalence to physically-based metrics such as the GWP
- and GTP (e.g., Tol et al. 2012). One difficulty in such approaches is that the economic
- damage has to be represented in a highly-idealised form, as some simple function of, for
- example, temperature change. Conventional physical metrics can also be judged in an
- economic context (e.g., Reisinger et al. 2013, Strefler et al. 2014).

- Section 2 presents the simple conceptual model that is used to relate precipitation change to
- RF and temperature change, which are themselves related to emissions. Section 3 presents
- some illustrative examples of the GPP drawing values of key parameters from the literature.
- 131 Section 4 then uses the methodology in the context of climate metrics, and compares it with
- more conventional metrics (the Global Warming Potential (GWP) and Global Temperature-
- change Potential (GTP)). Section 5 presents an illustration of the use of the methodology for
- understanding the effects of emissions in an individual year (or sustained emissions from that
- 135 year) on precipitation changes in or after that year this illustrates the principle drivers of the
- precipitation change, given present-day emissions. Section 6 explores some aspects of the
- uncertainty in characterising the GPP and Section 7 discusses prospects for further
- developing the GPP.

2. Simple conceptual model

- 140 The simple conceptual model presented here originates from the analysis of simulated
- precipitation changes in response to increases in CO₂ presented by Mitchell et al. (1987). This
- analysis was based around the fundamental controls on the energy balance of the troposphere,
- in which, to first order, the latent heating resulting from the net rate of condensation of water
- vapour (and hence precipitation) is balanced by net radiative cooling. The conceptual model
- has been further developed more recently, and extended to both multi-model assessments and
- other climate forcing (and feedback) mechanisms (e.g., Allen and Ingram, 2002, Takahashi
- 147 2009, Andrews et al. 2010, Kvalevåg et al. 2013, Allan et al. 2014).
- 148 The framework starts with an expression of the global-mean atmospheric energy budget,
- whereby the net emission of radiation by the atmosphere (i.e. the atmospheric radiative
- divergence (R_d) , which is the sum of the emission of longwave radiation by the atmosphere
- minus the atmospheric absorption of longwave and shortwave radiation) is balanced by the
- input of surface sensible (SH) and latent (LH) heat fluxes so that

$$R_d = LH + SH. (1)$$

- 154 *LH* is directly related to the precipitation as, at the global-mean level, evaporation (and hence
- 155 *LH* fluxes) and precipitation approximately balance.
- 156 In response to the imposition of an RF and subsequent changes in temperature, humidity and
- clouds, R_d will change. The latent heat change ΔLH can then be written

$$\Delta LH = \Delta R_d - \Delta SH. \tag{2}$$

- 159 ΔLH in W m⁻² can be converted to precipitation units of mm day⁻¹ by multiplication by 0.034
- 160 (86400 seconds in a day divided by the latent heat of vaporisation, L (2.5 x 10^6 J kg⁻¹ at
- 161 273.15 K)). There is some level of approximation in this conversion, as L is temperature
- dependent and some precipitation falls as snow rather than rain, and hence the latent heat of
- sublimation would be more appropriate. The precipitation change could also be quoted in %
- of total global-mean precipitation (about 2.68 mm day⁻¹ (e.g., Huffman et al., 2009)).

- 165 ΔR_d has two components. The first component is due directly to the RF mechanism which can
- 166 change the absorption of shortwave radiation and/or the emission and absorption of longwave
- radiation. The conventional top-of-atmosphere radiative forcing (RF) can be written as the
- sum of a surface component (RF_a) and an atmospheric component (RF_a) , and it is RF_a that
- directly influences ΔR_d . Because values of RF are more readily available than RF_a for a wide
- range of constituents, it is convenient to relate RF_a to RF and so, following Allan et al.
- 171 (2014), we define a parameter f such that $RF_a = fRF$. The parameter f could be estimated
- directly from RF calculations using a radiative transfer code. However, here results from
- 173 fixed-sea-surface-temperature climate model simulations (e.g. Andrews et al. 2010, Kvalevåg
- et al. 2013) are used; these have the advantage that they include the impact on f of rapid
- adjustments of, for example, clouds. A disadvantage is that the results of such experiments
- are noisier, because of model internal variability, which can be particularly important for
- small forcings. Note that a fully consistent approach would adopt effective radiative forcings
- 178 (ERF see Myhre et al. (2013)) rather than RF, and values of f derived using ERFs.
- However, assessed values of ERFs are not available for many species and so, in common
- with Myhre et al., (2013), the metric values calculated here use RFs, but including a number
- of indirect chemical effects and some cloud effects, as noted in Section 3. The values of f are
- based on one method of deriving ERFs and a possible reason for differences between f values
- in Andrews et al. (2010) and Kvalevåg et al. (2013) is that the fast tropospheric responses that
- distinguish RF from ERF differ between the models used in their study.
- The second component of ΔR_d is due to the temperature change resulting from the RF, which
- leads to an increased emission of longwave radiation. This increase in emission is modified
- by feedbacks involving other radiatively-important components such as water vapour and
- clouds (e.g. Takahashi, 2009, Previdi 2010) which can additionally influence ΔR_d via the
- absorption of shortwave radiation. Climate model simulations indicate that this component of
- 190 ΔR_d varies approximately linearly with changes in global-mean surface temperature ΔT_s (e.g.,
- Lambert and Webb, 2008, Previdi 2010, O'Gorman et al. 2012).
- 192 $\triangle SH$ in Eq. (2) is less well constrained. It also has two components, one due to the fast
- response to RF, which is independent of surface temperature change, and one due to surface
- temperature change. The fast response has been shown to be small for greenhouse gas
- forcings; Andrews et al. (2010) and Kvalevåg et al 2103 show it to be typically less than 10%
- of $\triangle LH$ for a doubling of CO₂, although the size and sign varies can vary amongst models
- 197 (Andrews et al. (2009)). However, it can be much larger for other forcings (of order 50% of
- 198 $\triangle LH$ in the case of black carbon (Andrews et al. (2010) and Kvalevåg et al 2013)). As noted
- by Takahashi (2009) and O'Gorman et al. (2012) an improved conceptual model could
- distinguish between ΔR_d for the whole atmosphere and ΔR_d for the atmosphere above the
- surface boundary layer, as changes in ΔR_d within the boundary layer seem more effective at
- 202 changing SH (e.g. Ming et al. (2010)) and hence less effective at changing LH. Here,
- following Thorpe and Andrews (2014), we assume the fast component ΔSH to be small and
- 204 neglect it, but more work in this area is clearly needed.
- Lambert and Webb (2008), Previdi (2010), O'Gorman et al. (2012) and others show that
- while generally a smaller term, the surface temperature dependent part ΔSH has a similar

- dependency on ΔT_s (at least in the multi-model mean). Hence it is convenient to combine the
- feedback-related changes in R_d and this component of SH in Equation (2) into a single term
- dependent on ΔT_s and separate out the RF term. Equation (2) then becomes, in precipitation
- 210 units of mm day⁻¹,

$$\Delta P = 0.034(k\Delta T_s - fRF). \tag{3}$$

- Despite its apparent simplicity, Eq. (3) has been shown by Thorpe and Andrews (2014) to
- simulate reasonably well future projections of precipitation change from a range of
- atmosphere-ocean general circulation models, albeit with a tendency to underestimate the
- 215 multi-model mean. Uncertainty in the value of f for all forcing agents (and possible inter-
- 216 model variations in f see section 6) inhibit a full assessment.
- We will refer to the $k\Delta T_s$ term as the "T-term" and the -fRF term as the "RF-term" although
- 218 they could also be termed the "slow" and "fast" responses, respectively, which relates to the
- 219 contrasting heat capacities and associated response time-scales of the ocean and atmosphere.
- The balance between these two terms varies between climate forcing agents; as will be
- shown, they can act to either reinforce or oppose each other. Hence the same ΔT_s from two
- 222 different forcing agents can result in a different ΔP .
- Note the sign convention here. For the case of a positive RF, since k is positive, the effect of
- 224 the T-term is to increase R_d as temperature increases the increased radiative divergence then
- leads to a requirement for a greater latent heat flux (and hence an increase in precipitation) to
- 226 maintain the tropospheric energy balance; this term provides the direct link between surface
- temperature change and precipitation change. If in this same case f (and hence RF_a) is
- 228 positive, then the RF-term would oppose the T-term (as it would decrease rather than increase
- 229 the radiative divergence) and act to suppress precipitation. Physically, in this case, there is
- less "demand" for latent heating to balance the tropospheric energy budget.
- 231 As a simple example of the processes, consider the equilibrium response to a doubling of
- carbon dioxide, and take $k = 2.2 \text{ W m}^{-2} \text{ K}^{-1}$ (consistent with the multi-model means in Previdi
- 233 (2010) and Thorpe and Andrews (2014)), $RF_{2xCO2} = 3.7 \text{ W m}^{-2}$ (Myhre et al., 2013 who give
- 234 the same value for the ERF) and f = 0.8 (Andrews et al. 2010). The equilibrium precipitation
- change ΔP_{2xCO2} (in %, assuming a global-mean precipitation of 2.68 mm day⁻¹), can then be
- written in terms of the equilibrium surface temperature change ΔT_{2xCO2} as

$$\Delta P_{2 \times CO_2} = 2.79(\Delta T_{2 \times CO_2} - 1.35). \tag{4}$$

- This equation shows that if $\Delta T_{2xCO2} = 1.35$ K, which, via $\Delta T_{2xCO2} = \lambda R F_{2xCO2}$, corresponds to a
- climate sensitivity λ of 0.36 K (W m⁻²)⁻¹, ΔP_{2xCO2} would be zero. The slope of the line is 2.79
- 240 % K⁻¹. Such an expression fits well the intercept and slope of the linear fit to equilibrium
- 241 double-CO₂ experiments from a range of climate models found by Allen and Ingram (2002 –
- their Fig. 2). Hence Eq. (4) acts as a further validation of the utility of Eq. (3) for simulating
- 243 global-mean precipitation change across climate models with varying parameterisations of,
- for example, convection, with climate sensitivities varying across the range from about 0.4 to
- 245 1.3 K (W m⁻²)⁻¹. The departures of individual models from this best fit could originate from

- 246 differences in any of the values of k, f, RF_{2xCO2} assumed here, or in inter-model differences in
- 247 the importance of the fast component of $\triangle SH$ which is not accounted for here. The slope of
- 248 the line also corresponds to hydrological sensitivity due only to the T-term, and is in good
- agreement with the multi-model mean derived by Thorpe and Andrews (2014).
- 250 Since more generally, $\Delta T_{eq} = \lambda R F_{eq}$, Equation (3) can also be written in a more general form
- for any ΔT_{eq} (and hence RF_{eq}), so that the equilibrium change in precipitation ΔP_{eq} (in %) is
- 252 given by

$$\Delta P_{eq} = 1.3\Delta T_{eq} (k - f/\lambda). \tag{5}$$

- This emphasizes that the offset between the T- and RF-terms depends strongly on λ . Using a
- 255 mid-range climate sensitivity of 0.8 K (W m⁻²)⁻¹, the RF-term for CO₂ offsets about 50% of
- 256 the precipitation change that would result from the T-term alone. Considering the IPCC
- 257 (2013) "likely" range for λ , which is 0.4 to 1.2 K (W m⁻²)⁻¹, the RF-term offsets the T-term by
- about 90% for low λ and by 30% at high λ . The overall global-mean equilibrium hydrological
- sensitivity ($\Delta P_{eq}/\Delta T_{eq}$) to CO₂ forcing can be derived from equation (5) and varies from about
- 260 0.25 % K^{-1} to 2 % K^{-1} over this range of λ , which can be compared with the value of 2.79 %
- 261 K⁻¹ due solely to the T-term.
- To relate the understanding encapsulated in Equation (3) to an emission of a gas or aerosol,
- 263 we consider first the GPP for a pulse emission of a unit mass of a gas at time t=0 and
- 264 consider the precipitation change at a time H after the emission. Following convention, we
- label this the Absolute GPP (AGPP_P), which is presented here in units of mm day⁻¹ kg⁻¹. The
- 266 GPP relative to a reference gas will be considered in Section 4.
- The T-term in Equation (3) becomes k times the absolute GTP_P (AGTP_P) (e.g. Shine et al.
- 268 2005). Assuming for small perturbations that RF is linear in the concentration of the emitted
- species, x, and that the perturbation decays exponentially with time constant τ_x , then for a unit
- emission, the RF-term is given by $-f_x A_x \exp(-H/\tau_x)$, where A_x is the specific RF (in W m⁻²
- kg⁻¹) of the emitted species. Hence the AGPP (in mm day⁻¹ kg⁻¹) is given by

272
$$AGPP_{p}^{x}(H) = 0.034(kAGTP_{p}^{x}(H) - f_{x}A_{y} \exp(-H/\tau_{y})).$$
 (6)

- 273 Since a perturbation of CO₂ does not decay following a simple exponential (see e.g. Joos et
- 274 al. 2013), the calculation of $AGPP_{P}^{CO_2}(H)$ is slightly more involved see the Appendix for
- 275 more details.
- The effect of a sustained emission of a unit mass of gas per year, from time t=0 can also be
- 277 considered yielding a sustained AGPP (AGPP_S). In this case, the AGTP_S (see Shine et al.
- 278 2005) can be used for the T-term and the RF-term is now proportional to the time variation of
- the perturbation of the species to a step-perturbation (e.g. Fuglestvedt et al. 2010). The
- 280 AGPP_S is given by

281
$$AGPP_s^x(H) = 0.034(kAGTP_s^x(H) - f_x A_x \tau_x (1 - \exp(-H/\tau_x)))$$
 (7)

282 which can also be expressed as a function of both AGTP_S and AGWP_P

283
$$AGPP_{S}^{x}(H) = 0.034(kAGTP_{S}^{x}(H) - f_{x}AGWP_{P}^{x}(H))$$
 (8)

- The calculation of $AGPP_s^{CO_2}(H)$ is explained in the Appendix. Note that when H is long
- compared to the time-scale of the climate response (several hundred years in this case see
- the Appendix) the $AGTP_s^x(H)$ can be related to the $AGWP_p^x(H)$ (see e.g. Shine et al. (2005))
- which would simplify Eq. (8) further.
- Here the AGPP_P and AGPP_S are used to calculate the GPP_P and GPP_S relative to a reference
- 289 gas, and following the common practice for GWP and GTP, CO₂ is used as that reference gas
- 290 here, although difficulties with this choice will be noted. The GPP_P, relative to an equal mass
- 291 emission of CO_2 , is then given by

$$GPP_p^x(H) = \frac{AGPP_p^x(H)}{AGPP_p^{CO_2}(H)}$$
(9)

- with a similar expression for the GPPs.
- Note we have chosen to present the AGPP_P and AGPP_S as end-point metrics i.e. as the
- 295 effect at the time horizon H of an emission at (or starting at) time zero. For some purposes, a
- time-integrated metric might give a useful perspective. Following Peters et al. (2011 see in
- 297 particular its Supplementary Information) we note that the time-integrated pulse metrics are
- 298 mathematically equivalent to the end-point metrics for sustained emissions. Hence, the
- 299 AGPPs and GPPs can equally be interpreted as time-integrated forms of the AGPPp and
- 300 GPP_P.

301

3. Illustrative values for the Absolute Global Precipitation-change Potential

- 302 In this section, illustrative calculations of the AGPP are presented. Values for gas lifetimes
- and A_x are taken from Myhre et al. (2013) and are described in more detail in the Appendix.
- 304 The AGTP calculation requires a representation of the surface temperature response, which
- depends on the climate sensitivity and rate of ocean heat uptake. We use the simple impulse-
- response function in Boucher and Reddy (2008) (as used in Myhre et al. (2013) for GTP
- 307 calculations). Details are given in the Appendix. Values of f, which describe the partitioning
- of the RF between surface and atmosphere are taken from Andrews et al. (2010) these will
- 309 likely be quite strongly model dependent, but for the purposes of illustration, they suffice.
- 310 Some sensitivity tests to the representation of the impulse-response function and f are
- 311 presented in Section 6. The calculations for CH₄ and N₂O emissions include indirect effects,
- 312 the most prominent being their impact on ozone. Different values of f should be used for each
- indirect component, but in the absence of robust assessments for these, the same value of f is
- used for all indirect components of the CH₄ and N₂O forcing as is used for the direct
- 315 components.

3.1 Well-mixed greenhouse gases

317

- Figure 1 shows the AGPP_P for CO₂, CH₄ and N₂O, for the total and the RF and T terms
- 319 individually, for a period up to 100 years after the pulse emission. In Andrews et al. (2010), f
- is larger for CO₂ (0.8) than for methane (0.5) because, for present-day concentrations, the
- 321 lower opacity of the methane bands means that the surface feels more of the top-of-the-
- 322 atmosphere forcing than it does for CO₂. Since N₂O has a similar atmospheric opacity to
- 323 CH₄, it is hypothesized that surface-atmosphere partitioning of the RF also behaves in a
- similar way to CH_4 and so the value of f for N_2O is also taken to be 0.5; further work would
- be needed to establish this. Hence, from Equation (3), the degree of offset between the RF-
- and T-terms is larger for CO₂ than for CH₄ and N₂O.
- Figure 1(a) for CO₂ illustrates the general behaviour. For a pulse emission, the size of the RF-
- 328 term is maximised at the time of emission, as this is when the concentration is largest, and
- 329 then decays as the perturbation decays. The T-term is dictated by the timescale of the
- response of the surface temperature to the forcing. The characteristic temperature response to
- a pulse forcing (e.g. Shine et al. 2005) is an initial increase in T, as the thermal inertia of the
- surface means it takes time to respond to the forcing, reaching a maximum, followed by a
- decrease in temperature that is controlled by the timescales of both the decay of the pulse and
- 334 the temperature perturbation. For the first 5 years, the CO₂ precipitation response is negative
- as the RF-term dominates, after which the T-term dominates, but the total is approximately
- 336 50% of the T-term. The long perturbation timescales mean that the effect on precipitation
- persists for more than 100 years after an emission, as does the competition between the T-
- 338 and RF-terms.

343

- N₂O has a lifetime of the order of a century and its AGPP_P (Fig. 1(b)) is qualitatively similar
- to CO_2 but the T-term dominates, because f is smaller. As CH_4 is much shorter lived, its
- behaviour is somewhat different. As the pulse, and the associated RF, has disappeared by
- about year 40, after this time the AGPP_P is determined by the T-term only.

3.2 Short-lived species

- The AGPP is now illustrated for two short-lived species, sulphate and black carbon (BC)
- aerosols. For both cases, the radiative efficiency and lifetime values from Myhre et al. (2013)
- are used and given in the Appendix; for these illustration purposes only the sulphate direct
- 347 effects are included, and the BC values include some aerosol-cloud interaction and surface
- 348 albedo effects. In terms of the surface-atmosphere partitioning of RF, these are two
- contrasting cases. For sulphate, the Andrews et al. (2010) model results indicate an f value
- less than 0.01 in magnitude and so it is assumed here to be zero; this indicates that essentially
- all of the top-of-the-atmosphere forcing reaches the surface. By contrast, Andrews et al.
- 352 (2010) find that for BC, f is 2.5, so that RF_a is much greater than RF; the surface forcing is of
- opposite sign to RF and RF_a as the surface is deprived of energy, while the atmosphere gains
- energy. As will be discussed further in Section 6, there are considerable uncertainties in these
- values, especially for BC, where both RF and f depend strongly on the altitude of the BC.
- Nevertheless, the values used here suffice to illustrate a number of important points.

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- Figure 2 shows the AGPP_P for both black carbon and sulphate. As both are very short-lived
- 358 (weeks) compared to the greenhouse gases, their RF-term decays to zero within a year (and
- hence is not visible on Fig. 2), and it is only the thermal inertia of the climate system that
- enables them to influence temperature beyond this time period.
- 361 An alternative perspective of the effect of sulphate and BC is provided for the sustained-
- emissions case. In this case, because the BC and sulphate perturbations persist, so too does
- 363 the influence of the RF-term on precipitation. Figure 3 shows the AGPP_S for CO₂, BC and
- 364 sulphate. For CO₂, the long-time scales of CO₂ perturbation mean that both the RF term and
- T term increase throughout the 100 year period shown. At short time-horizons, the RF-term
- dominates, leading to suppression of global precipitation, but after about 15 years, the T-term
- starts to dominate, and the AGPP_S becomes positive.
- For BC, the impact of the large RF-term is dramatic. It is strongly negative and constant with
- 369 time (because of the short lifetime), while the T term is positive and increases until the
- temperature is almost in equilibrium with the RF. This counteracts the impact of the RF term
- on the total, but the total nevertheless remains negative throughout. For sulphate, because f is
- assumed to be zero, the total remains equal to the T-term.

373 **4. The GPP relative to CO₂**

377

- While absolute GPP values were presented in section 3, in this section we normalize the GPP
- values to the effects of the reference gas CO₂ to provide a relative measure, using Eq. 9 and
- its equivalent for sustained emissions.

4.1 Well-mixed greenhouse gases

- Figure 4 shows the GPP_P for N₂O and CH₄; for comparison, the GTP_P is also shown. Note
- that the plots start at H=20 years, as the time at which the different AGPP_P's cross the zero
- axis differs slightly amongst the gases, and this results in a singularity in Eq. (9). For N₂O,
- the GPP_P is at least 300 times greater than CO₂ on all timescales shown, and, per unit
- emission, is more than 40% more effective at changing precipitation than temperature (as
- given by the GTP_P), compared to CO₂. This is because the RF term is less effective at muting
- the T-term for N₂O's GPP_P than is the case for CO₂. For CH₄ the difference between the
- 385 GPP_P and GTP_P is most marked in an absolute sense at shorter time horizons, when the GPP_P
- of methane is affected most by the RF-term; the GPP_P and the absolute difference with the
- 387 GTP decline at longer time scales when it is entirely due to the difference between the
- 388 AGTP_P and AGPP_P for CO₂.
- Table 1 presents the values of all absolute metrics used here for CO₂ and Table 2 presents the
- values of the GWP_P, GTP_P and GPP_P for H of 20 and 100 years; these time horizons are
- 391 chosen for illustrative purposes, rather than being indicative that they have special
- significance, except insofar as 100 years is used for the GWP within the Kyoto Protocol (e.g.
- Myhre et al. 2013). For CH₄, the GPP_P(20) is 50% larger than the GWP_P(20) and almost
- double the GTP_P(20) mostly because of the larger effect of the RF-term on the GPP_P for CO₂.
- 395 The time-integrated nature of the GWP_P means that it is much higher than the GTP_P and
- 396 GPP_P at 100 years, while the GPP_P remains about double the GTP_P. The GPP_P for N₂O is 25-

397	of the RF-term on the GPP _P for CO_2 .
399	
400	4.2 Short-lived species
401	Figure 5 shows the GPP _P and GTP _P for black carbon and sulphate. As noted in Section 3.2,
402	the radical difference in their values of $f(2.5)$ for black carbon, 0 for sulphate) has no impact
403	on the AGPP for BC and sulphate beyond very short timescales. Because of this, in Fig. 5,
404	the only difference between the GPP _P and GTP _P comes from the influence of the RF-term on
405	the $AGPP_P^{CO_2}$, and on an equal emissions basis both short-lived species are, relative to CO ₂ ,
406	more effective at changing precipitation than temperature – this is also shown in Table 3.
407	Figure 6 shows the GPP _S , comparing it with the GTP _S . For sulphate, the difference between
408	the GPP _S and GTP _S originates entirely from the effect of the RF-term on $AGPP_S^{CO_2}$, because
409	of the assumption that f is zero. For black carbon they differ dramatically – whilst both BC
410	and CO ₂ cause a warming, so that the GTP _S is positive, their impact on precipitation is
411	opposite, and the BC GPP _S is negative.
412	Table 3 presents values of the GTP_S and GPP_S for $H=20$ and 100 years, including the values
413	for CH ₄ and N ₂ O for completeness. The GPP _S values at 20 years are particularly influenced
414	by the fact that the AGPP _S for CO ₂ is relatively small at this time, due to the strong
415 416	cancellation between the T and RF terms. At both values of H, the GPP _S values are higher in magnitude than the corresponding GTP _S values for all non-CO ₂ components considered here.
417	5. Precipitation response to realistic emissions
418	To illustrate a further usage of the AGPP _P and AGPP _S , Figs. 7 and 8 apply them to 2008
419	emissions, to examine the consequences of the emissions of the 5 example species on
420	precipitation. Figure 8.33 of Myhre et al. (2013) presents a similar calculation applying the
421	AGTP _P and shows that the 5 species used here are the dominant emissions for determining
422	temperature change; hence it was felt useful to present the total effect of the 5 emissions in
423	the figures as well. Emissions are taken from Table 8.SM.18 of Myhre et al. (2013) and
424	reproduced in Table A.1. For reference, the corresponding values using the AGTP _P and
425	AGTP _s are also shown.
426	Figure 7 shows the impact of the 2008 emissions, emitted as a single pulse, on global
427	precipitation and temperature change in subsequent years. While the emissions of CH ₄ ,
428	sulphate and BC are 2 to 4 orders of magnitude smaller than those of CO ₂ , in the early years
429	after the emission, their effects are competitive with CO ₂ because of the size of the GPP _P and
430	GTP _P ; emissions of N ₂ O are small enough that , despite its large GPP _P , its absolute
431	contribution remains low throughout. Because of the differing compensations between the T-
432	and RF-terms for CO ₂ and CH ₄ , their relative importance differs quite significantly between
433 434	the precipitation and temperature calculations. Methane's contribution to precipitation change is less negative or more positive than that of CO ₂ until about 20 years; it exceeds the

- 435 CO₂ contribution by a factor of 2 at about 10 years, and remains 25% of the CO₂ effect even
- at 50 years. For temperature, the contributions are approximately the same until 10 years,
- after which the CO₂ contribution dominates, being about 7 times larger by 50 years. For the
- 438 two aerosol components, the GPP_P is unaffected by the RF-term (because the RF due to a
- pulse emission of a short-lived gas declines rapidly see Section 3) but their importance for
- precipitation relative to CO₂ is enhanced, because the RF-term acts to suppress the effect of
- 441 CO₂ on precipitation change. Thus, for example, the BC effect on precipitation is larger than
- 442 CO₂ out to year 10, compared to year 4 for temperature.
- Figure 8 shows the effect of assuming sustained emissions at 2008 levels. Although not a
- plausible future scenario (since, for example, emissions of greenhouse gases are at present
- continuing to rise) it provides a useful baseline experiment to assess the relative roles of
- current emissions when their atmospheric burdens are replenished each year. As expected
- from the AGPPs values, the role of the short-lived species differs considerably from the pulse
- case, as the RF-term remains active in the case of precipitation, BC's effect is now negative
- throughout. Until about 30 years, the net effect of all 5 emissions is a reduction of
- 450 precipitation, after which the warming due to CH₄ and CO₂ is sufficient for their T-terms to
- overwhelm the reduction caused by sulphate (due to its T-term) and BC (due to its RF-term).
- This near-term reduction of precipitation is also seen in the results of Allan et al. (2014),
- where the precipitation changes are driven directly by forcings and temperatures (rather than
- by emissions, as is the case here). By contrast, the temperature effect is positive after year 1.
- Perhaps most marked is the role of CH₄. It is the dominant driver of positive precipitation
- change until about year 50 and even after 100 years its effect is about 50% of that due to CO₂.
- This differs from temperature, where the CO₂ effect is greatest after 15 years and 3 times
- larger by 100 years. Fig.8 also illustrates the extent to which the sulphate and BC emissions
- are opposing the precipitation increase due to the greenhouse gases, at large values of H;
- those components would be relatively quickly responsive to any changes in emissions.
- While these are clearly idealised applications of uncertain metrics, they nevertheless illustrate
- their potential utility for assessing the relative importance over time of different emissions on
- global precipitation change. The approach could be extended to past or possible future
- emission profiles, by convolving the time-dependent emissions with the GTP_P and GPP_S
- values.

6. Sensitivities and uncertainties

- There are many uncertainties and sensitivities in the calculation of metrics such as
- assumptions about the background state (which can affect A_x and τ_x), and the impulse-
- response function for CO₂ (see e.g. Fuglestvedt et al. 2010; Joos et al. 2013; Myhre et al.
- 470 2013). Two sensitivities are explored. First, the impulse-response model for surface
- 471 temperature change used here (see beginning of Section 3) is a fit to output from experiments
- with one particular climate model with its own particular climate sensitivity. Olivié et al.
- 473 (2012) present similar fits derived from 17 different climate models, or model variants the
- 474 fits shown in Table 5 of Olivié et al. (2012) are used, along with the Boucher and Reddy
- 475 (2008) fit used in Section 3 and cover a wide range of climate sensitivities (0.49 to 1.06 K (W

- 476 m⁻²)⁻¹) and timescales of climate response, although we note that model uncertainty range
- may not fully straddle the true uncertainty range. Olivié and Peters (2013) used these fits to
- 478 explore the sensitivity of the GTP calculations. Figure 9 shows the mean and standard
- deviation of the pulse and sustained GTP and GPP derived using these 18 different
- 480 representations.
- Considering the absolute pulse metrics for CO₂, Fig. 9a shows that the AGTP_P is only
- 482 moderately sensitive (with a coefficient of variation (cv) of about 20%) to model choice. By
- contrast the cv is about 60 and 40% for the AGPP_P(20) and AGPP_P(100), respectively. This is
- because the T-term is highly sensitive to the choice of impulse-response model, whilst the
- 485 RF-term is independent; hence the degree of compensation between these two terms varies
- amongst these models. The GTP_P is most sensitive for short-lived species and this uncertainty
- is amplified for the GPP_P, by up to a factor of 2 for the GPP_P(100) for sulphate (Fig. 9d). By
- contrast, for the longer-lived species the uncertainty in the GTP_P and GPP_P differ greatly for
- 489 N₂O (Fig. 9c), the cv for GTP_P values is only a percent or so, but is typically 40% for the
- 490 GPP_P, as both the numerator and denominator in Eq. (9) are impacted by compensations in
- 491 the T- and RF-terms to different degrees at different times.
- The GPPs is more sensitive because even the sign of the $AGPP_s^{co_2}$ is not well constrained at 20
- 493 years (Fig. 9a). Roughly half of the impulse-response models yield positive values and half a
- 494 negative ones, with two near zero, because of the differing degrees of compensation between
- the T- and RF-terms. The value of H at which the $AGPP_s^{CO_2}$ is zero varies from 11 to 61 years
- amongst the models. (For comparison, for the $AGPP_p^{CO_2}$, the corresponding range is 4 to 13
- 497 years.) In these circumstances, it becomes difficult to compare the GPPs values as they vary
- wildly from model to model (from -18000 to 24000 for the GPP_S(20) for N₂O) and for this
- reason the AGPP_S are presented in Fig. 9. Even the $AGPP_S^{CO_2}(100)$ values vary by over an
- order of magnitude across the 18 models. In general, the uncertainties in the AGPP_s exceed
- those in the AGTPs; this is most marked in the case of N₂O, where the GTPs is almost
- insensitive to the choice of impulse-response model, as the effect of this choice on the
- AGTP_S for CO₂ and N₂O is almost the same.
- The second sensitivity explored here is to the assumed values of f by replacing the Andrews
- et al. (2010) values by those from Kvalevåg et al. (2013) (see Table 1). Where available, we
- use the values of f from the larger forcing perturbations given by Kvalevåg et al. (2013) as
- 507 these give a clearer signal. For BC, Kvalevåg et al. (2013) present a range of values, for
- perturbations at different altitudes for example they find a value of f of 6.2 (for 10 times the
- model-derived vertical profile of BC in response to present-day emissions) and 13 (when 10
- 510 times the present-day burden is placed entirely at 550 hPa); these can be compared to the
- Andrews et al. (2010) value of 2.5. The difference results mostly from the semi-direct effect
- of BC and clouds; when BC is entirely placed at certain pressures (750 and 650 hPa),
- Kvalevåg et al.'s (2013) results indicate that f is particularly poorly constrained, because RF
- is close to zero, while RF_a is large and positive. This is an example of where casting Eq. (3)
- in terms of RF_a rather than RF would be advantageous (see Section 2). It should be noted that
- this sensitivity test concerns the impact of BC altitude on f rather than on τ_r , and A_r .

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- Table 1 shows the AGPP_P and AGPP_S for CO₂ and Table 4 shows the GPP_P and GPP_S; these
- should be compared with the appropriate columns in Tables 2 and 3 (the GWP, GTP_P and
- GTP_S are unaffected by f). For the GPP_P for CH₄ and N₂O, the effect of changing the f values
- is rather modest (10-20%) because changes in the numerator and denominator of Eq. (9)
- 521 compensate to some extent. For BC and sulphate, changes are entirely dependent on the
- change in $AGPP_p^{CO_2}$, as the change in f factor has little influence (see Section 3.2) and hence
- 523 changes are correspondingly larger (20-30%).
- The $AGPP_s^{CO_2}(20)$ (Table 1) is rather sensitive to the change in f because of the degree of
- 525 compensation between the T- and RF-terms, and increases by more than a factor of 2 (Table
- 1). This is the dominant reason why the GPP_S(20) for N₂O and CH₄ decrease by about a
- factor of 2. The changes at 100 years are much smaller, nearer 10%. The AGPPs for the short-
- lived species are, unlike the AGPP_P, now affected by the change in f. Table 5 shows the effect
- on the sulphate $GPP_S(20)$ to be about a factor of 2, while the $GPP_S(100)$ is little affected. By
- contrast, the GPP_S for black carbon at both time horizons depends significantly on the
- altitude of the black carbon perturbation.

7. Discussion and Conclusions

- This paper has used a simple, but demonstrably useful, conceptual model of the drivers of
- global-mean precipitation change in response to the imposition of a radiative forcing, to relate
- precipitation change directly to emissions. The GPP_P and GPP_S metrics illustrate the interplay
- between the two drivers (the atmospheric component of the radiative forcing, and the surface
- temperature change) for different forcings, at different time horizons, and for both pulse and
- sustained emissions. The GPP_P and GPP_S are given as the change at a specific time horizon
- 539 (and hence are end-point metrics). There may be climate effects related to the total change in
- 540 precipitation over time for which an integrated metric would be appropriate, so it is useful to
- note that the GPP_S can also be interpreted as the time-integrated GPP_P.
- It has been shown that relative to CO₂, the pulse and sustained GPP values for the non-CO₂
- species examined here are larger than the corresponding GTP values, because the CO₂ GPP is
- 544 the sum of two quite strongly opposing terms. Further, for black carbon emissions, while
- they act to warm the climate system, they also act to reduce global-mean precipitation; while
- 546 this has been clear from the modelling literature for some time, the present work shows how
- 547 the perspective is different for pulse and sustained emissions. The reduction of precipitation
- is driven entirely by the radiative forcing component and since, for pulse emissions of short-
- 549 lived species this falls away on time scales of weeks, it is only apparent on longer time-scales
- for the sustained perspective. This is an example of how the perturbation design can have a
- large impact on the calculated response.
- The evaluation of precipitation metrics assumes that the parameters required for the simple
- conceptual model are available, and in particular the partitioning of radiative forcing between
- surface and atmosphere. Only a rather limited number of model studies of this partitioning
- are currently available, and there are significant differences amongst these and particular
- sensitivity to the altitude of absorbing aerosol (e.g. Ming et al. (2010), Kvalevåg et al.

557 (2013)). In addition, further development of the simple conceptual model (particularly to 558 account for fast changes in the sensible heat flux) would be beneficial, once understanding improves, as would a fully consistent usage of effective radiative forcings. The ongoing 559 Precipitation Driver Response Model Intercomparison Project (PDRMIP) 560 (http://cicero.uio.no/PDRMIP/) should provide important information on the utility of the 561 562 conceptual model and of the degree of robustness of the surface-atmosphere partitioning amongst a range of climate models for a number of radiative forcing mechanisms. Clearly 563 further studies, for a wider range of forcing agents are also needed and indeed casting Eq. (3) 564 565 directly in terms of atmospheric radiative forcing (rather than top-of-atmosphere radiative 566 forcing) would be desirable if atmospheric radiative forcing values became more readily 567 available. It is not suggested that the new metrics could replace conventional emissions metrics such as 568 569 the GWP and GTP in climate policies or emission trading context, but they do provide a 570 useful additional perspective for assessing the effects of emissions; they particularly help to 571 emphasise where the impact on precipitation differs significantly from that on temperature or 572 forcing. One difficulty in its application is that conventional metrics generally use CO₂ as a 573 reference gas. For precipitation change, the forcing and surface temperature components 574 oppose each other, which means that the effect of CO₂ emissions on precipitation can be zero 575 (at least in the global-mean) at short time horizons for both pulse and sustained emissions. This is clearly undesirable for a reference gas, and it has also been shown that the timing of 576 577 this zero point is rather sensitive to the particular parameters used in its calculation. Hence 578 absolute metrics may be more instructive. By applying the absolute metrics to a specific illustrative case (emissions in 2008, either as a pulse, or sustained indefinitely) the 579 580 importance of methane in influencing the global-mean precipitation change is highlighted – 581 using the default model parameters here, in the sustained 2008 emissions case, the precipitation change from methane exceeds that from CO₂ for about 50 years, By contrast, for 582 583 the temperature case, the effect of CO₂ emissions are almost immediately at least comparable 584 to, or stronger than, methane. 585 It has been stressed that use of global-mean precipitation change as a measure of impact has 586 difficulties, because predicted future changes differ in sign between regions – the global-587 mean is a small residual of these opposing more localised changes and hence it only gives rather general guidance on the effect of different drivers on the changing hydrological cycle. 588 589 Nevertheless, as noted in the Introduction, some of that regional variability can be understood 590 as a generic response to temperature change. The approach here could be enhanced to a more 591 regional level of response by either using a simple pattern-scaling approach (whereby the 592 pattern of predicted precipitation change scales with the global-mean) or, better, to derive a regional variation that accounts for the different effects of the forcing and temperature 593 594 response on precipitation change (Good et al. 2012). The patterns emerging from such an 595 approach would likely depend significantly on which climate model was used to derive them. 596 In addition, such patterns would be needed for all the primary forcing agents. For short-lived 597 emissions, it is known that even global-mean metrics such as the GWP and GTP depend on

the emission location (e.g., Fuglestvedt et al. 2010) – this will also be true for the

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599 precipitation metrics. Metrics can also be posed in terms of the regional response to regional 600 emissions. For example, Collins et al. (2013) employed the Regional Temperature Potential proposed by Shindell (2012) whereby a matrix is produced that characterises the effect of 601 RFs in a set of given regions on the temperature change in a set of given regions; a similar 602 603 approach could be taken using the Regional Precipitation Potential proposed by Shindell et al. 604 (2012).605 In spite of the difficulties in quantifying the precipitation metrics given present knowledge of the driving parameters, the framework presented here adds a useful extra dimension to simple 606 607 tools that are currently available for assessing the impact of emissions of different gases and 608 particulates. 609 **Author contribution:** KPS conceived the idea of the emissions metrics for precipitation, through conversations with RPA, performed the calculations and led the writing. RPA, WJC 610 611 and JSF provided major critical input to the drafts, including ideas on adjusting the emphasis of the paper and on possible applications of the metrics. 612 613 Acknowledgements: We acknowledge funding from the European Commission, under the ECLIPSE (Evaluating the Climate and Air Quality Impacts of Short-Lived Pollutants) Project 614 615 (Grant Agreement 282688) and thank other ECLIPSE partners for their encouragement and input to this work. We are grateful to Katsumasa Tanaka, an anonymous reviewer and the 616 617 Editor for their helpful comments, and for suggestions and input from participants in 618 PDRMIP.

619 Appendix

- The impulse response function, R(t), for a pulse emission of CO_2 is assumed to be of the
- 621 form

622
$$R(t) = a_o + \sum_j a_j \exp\left(-\frac{t}{\alpha_j}\right)$$
 (A1)

- where the parameters used here follow Myhre et al. (2013), with a_0 =0.2173, a_1 =0.2240,
- 624 a_2 =0.2824, a_4 =0.2763 and α_1 = 394.4 years, α_2 = 36.54 years and α_3 = 4.304 years.
- The impulse response function for global-mean surface temperature in Sections 3 to 5 is
- taken from Boucher and Reddy (2008) and is of the form

$$R(t) = \sum_{i} \frac{c_i}{d_i} \exp\left(-\frac{t}{d_i}\right)$$
 (A2)

- 628 with c_1 =0.631 K (W m⁻²)⁻¹, c_2 =0.429 K (W m⁻²)⁻¹ and d_1 =8.4 years and d_2 =409.5 years. The
- equilibrium climate sensitivity for this function is 1.06 K (W m⁻²)⁻¹, equivalent to an
- equilibrium surface temperature change for a doubling of CO₂ of about 3.9 K. Additional
- 631 impulse-response functions are used in Section 6, with alternative values of c_i and d_i .
- To derive the AGPP_P in Eq. (6), for species for which the perturbation decays exponentially
- with a single time-constant τ_x , requires an expression for the AGTP_P. For a species with a
- specific RF A_x and using Eq. (A2) this is given by (see, for example, Fuglestvedt et al.
- 635 (2010))

636
$$AGTP_{p}^{x}(t) = A_{x}\tau_{x}\sum_{i=1}^{2} \frac{c_{i}}{\tau_{x} - d_{i}} \left(\exp(-t/\tau_{x}) - \exp(-t/d_{i})\right). \quad (A3)$$

- This equation does not apply in the case where $\tau_x = d_i$; the appropriate expression is given in
- Shine et al. (2005) for this case, which has to be modified for the two-term form of Eq. (A2).
- For the case of CO₂, where the decay of a pulse is given by Eq. (A1), the AGTP_P is given by
- 640 (see, for example, Fuglestvedt et al. (2010))

641
$$AGTP_{P}^{CO_{2}}(t) = A_{CO_{2}} \left[a_{o} \sum_{i=1}^{2} c_{i} (1 - \exp(-\frac{t}{d_{i}})) + \sum_{i=1}^{2} c_{i} \sum_{j=1}^{3} \frac{a_{j} \alpha_{j}}{\alpha_{j} - d_{i}} (\exp(-t/\alpha_{j}) - \exp(-t/d_{i})) \right].$$
(A4)

- For the case of CO₂, the exponential in the second term on the right-hand side of Eq. (6) is
- replaced by Eq. (A1) for the calculation of $AGPP_p^{CO_2}(H)$.
- To derive the AGPPs in Eq. (7), the GTPs for non-CO₂ species is given by (e.g. by
- rearranging the expression in Shine et al. (2010) following Peters et al. (2011))

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646
$$AGTP_{S}^{x}(t) = A_{x}\tau_{x} \left[\sum_{i=1}^{2} \frac{c_{i}}{\tau_{x} - d_{i}} (\tau_{x}(1 - \exp(-t/\tau_{x})) - d_{i}(1 - \exp(-t/d_{i}))) \right]$$
(A5)

- and again the case where $\tau_i = d_i$ is given in Shine et al. (2005), which has to be modified for
- 648 the two-term form of Eq. (A2).
- The calculation of the AGPPs for CO₂ requires the AGTPs and is given by

650
$$AGTP_{s}^{CO_{2}}(t) = \sum_{i=1}^{2} A_{CO_{2}} c_{i} \left[a_{o}(t - d_{i}(1 - \exp(-t/d_{i}))) + \sum_{j=1}^{3} \frac{\alpha_{j} a_{j}}{\alpha_{j} - d_{i}} (\alpha_{j}(1 - \exp(-t/\alpha_{i})) - d_{i}(1 - \exp(-t/d_{i}))) \right]$$
(A6)

and also the $AGWP_p^{CO_2}$, for the second term on the right hand side of Eq. (7) which is

653
$$AGWP_{p}^{CO_{2}}(t) = A_{CO_{2}}(a_{o}t + \sum_{j=1}^{3} a_{j}\alpha_{j}(1 - \exp(-\frac{t}{\alpha_{j}}))) \quad . \tag{A7}$$

The parameters used for the 5 different species employed here are presented in Table A1.

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Table 1. Absolute metrics, AGWP, AGTP_P, AGTP_S, AGPP_P and AGPP_S for CO₂ at time horizons of 20 and 100 years, which are chosen for illustrative purposes. The first and second sets of AGPP values use the CO₂ *f* factor from Andrews et al. (2010) and Kvalevåg et al. (2013) respectively (see Table A1).

-		Time horizon (years)		
	unit	20	100	
AGWP	W m ⁻² kg ⁻¹ year	2.50 x 10 ⁻¹⁴	9.19 x 10 ⁻¹⁴	
$AGTP_P$	K kg ⁻¹	6.85 x 10 ⁻¹⁶	5.48 x 10 ⁻¹⁶	
$AGTP_S$	K kg ⁻¹ year	1.05 x 10 ⁻¹⁴	5.90 x 10 ⁻¹⁴	
AGPP _P (Andrews)	mm day ⁻¹ kg ⁻¹	2.27 x 10 ⁻¹⁷	2.13 x 10 ⁻¹⁷	
AGPP _S (Andrews)	mm day ⁻¹ kg ⁻¹ year	0.105×10^{-15}	1.91 x 10 ⁻¹⁵	
AGPP _P (Kvalevåg)	mm day ⁻¹ kg ⁻¹	2.99 x 10 ⁻¹⁷	2.63 x 10 ⁻¹⁷	
AGPP _S (Kvalevåg)	mm day ⁻¹ kg ⁻¹ year	0.275 x 10 ⁻¹⁵	2.53 x 10 ⁻¹⁵	

Table 2: The GWP, GTP_P and GPP_P, relative to CO₂, for pulse emissions of 4 species at time horizons of 20 and 100 years, which are chosen for illustrative purposes. The absolute values of metrics for CO₂ are given in Table 2.

	GWP(20)	GWP(100)	GTP _P (20)	$GTP_{P}(100)$	GPP _P (20)	GPP _P (100)
CH ₄	84	28	67	4.3	120	8.1
N_2O	263	264	276	234	396	325
Sulphate	-141	-38	-41	-5.28	-92	-10.1
Black carbon	2415	657	701	91	1580	173

Table 3. The GTP_S and GPP_S, relative to CO₂, for sustained emissions of 4 other species at time horizons of 20 and 100 years, which are chosen for illustrative purposes. The absolute values of metrics for CO₂ are given in Table 2.

7	9	9
-/	9	9

	$GTP_{S}(20)$	$GTP_{S}(100)$	$GPP_S(20)$	GPP _S (100)
CH ₄	93	31.5	357	49.6
N_2O	256	267	846	401
Sulphate	-199	-43.2	-1490	-100
Black carbon	3410	741	-23500	-979

Table 4: The GPP_P and GPP_S, relative to CO₂, for pulse emissions of 4 other species at time horizons of 20 and 100 years, which are chosen for illustrative purposes, using the values of surface-atmosphere partitioning of radiative forcing from Kvalevåg et al. (2013). The two black carbon values are, respectively, using a model-derived vertical profile for present-day emissions and assuming that the present-day burden is placed entirely at 550 hPa. The absolute values of metrics for CO₂ are given in Table 2.

	GPP _P (20)	GPP _P (100)	GPP _S (20)	GPP _S (100)
CH ₄	101	6.6	187	44.4
N_2O	370	303	486	367
Sulphate	-70	-8.2	-741	-94.0
Black Carbon	1200	141	-36600, -87400	-3740, -9250

Table A1: Parameter values used for each species included in calculations. All values are taken from Myhre et al. (2013), unless otherwise stated, and the CH₄ and N₂O values of A_x include the indirect effects described there

	A_{x} $(W m^{-2} kg^{-1})$	τ_x (years)	f (Andrews et al., 2010)	f (Kvalevåg et al. (2013))	2008 emissions (kg)
CO_2	1.76 x 10 ⁻¹⁵	See text	0.8	0.6	3.69×10^{13}
$\mathrm{CH_4}$	2.11 x 10 ⁻¹³	12.4	0.5	0.3	3.64×10^{11}
N_2O	3.57×10^{-13}	121.0	0.5	0.3	1.07×10^{10}
Sulphate	-3.2×10^{-10}	0.011	0.0	-0.4	1.27×10^{11}
Black carbon	3.02 x 10 ⁻⁹	0.02	2.5	6.2, 13.0	5.31×10^9

Figures

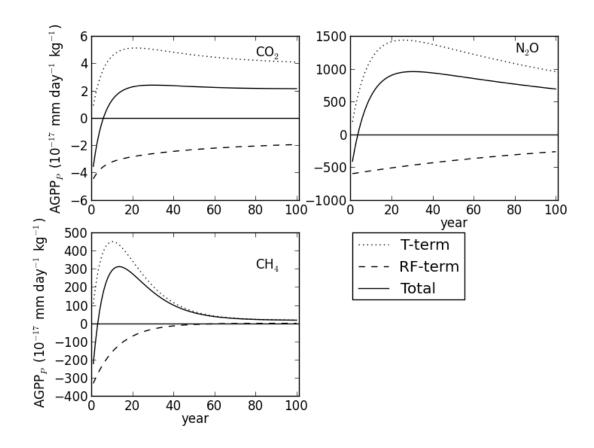


Figure 1: AGPP_P for 1 kg pulse emissions of CO_2 , N_2O and CH_4 . The T-term and RF-term refer to the first and second terms on the right hand side of Eq. (3) respectively, and the Total term is the sum of these.

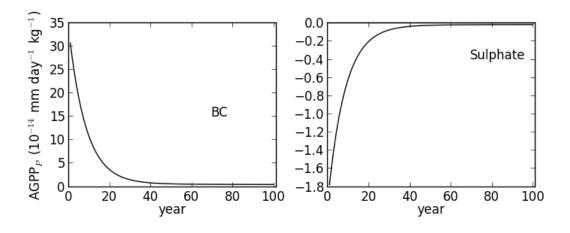


Figure 2: AGPP_P for 1 kg pulse emissions of black carbon (BC) and sulphate. Note that the RF-term in Eq. (3) is negligible for such short-lived gases, except at time horizons less than a few weeks, and only the total is shown.

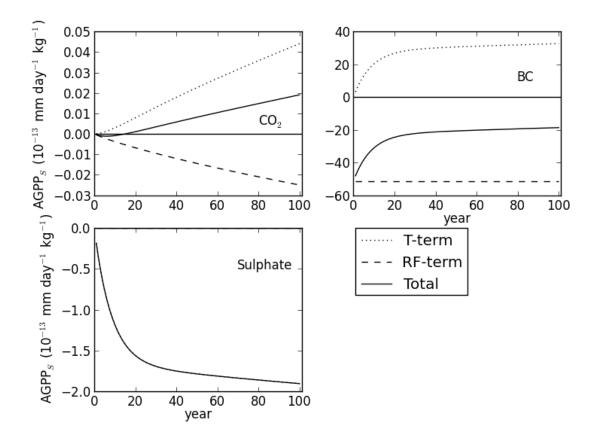


Figure 3: AGPP_S for 1 kg year⁻¹ sustained emissions of CO₂, BC and sulphate. The T-term and RF-term refer to the first and second terms on the right hand side of Eq. (3) respectively, and the Total term is the sum of these. For sulphate, the RF term is assumed to be zero (see text) and so only the Total is shown.

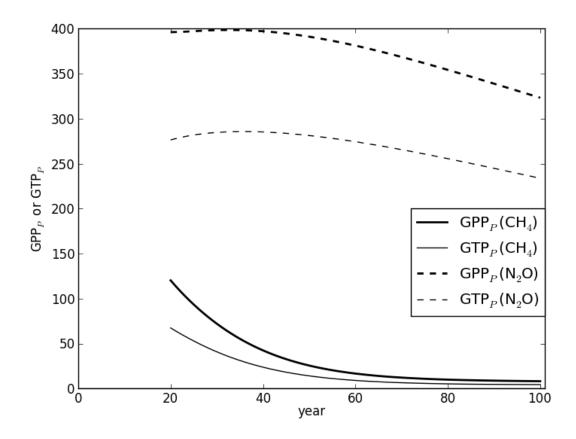


Figure 4: GPP_P (in bold) and GTP_P for 1 kg pulse emissions of N_2O and CH_4 relative to a 1 kg pulse emission of CO_2 .

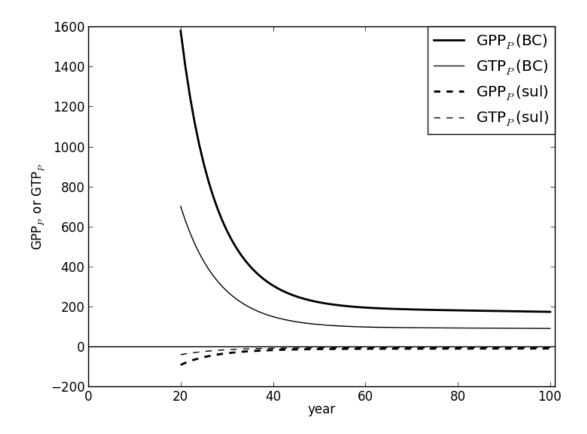


Figure 5: GPP_P (in bold) and GTP_P for 1 kg pulse emissions of BC and sulphate relative to a 1 kg pulse emission of CO_2 .

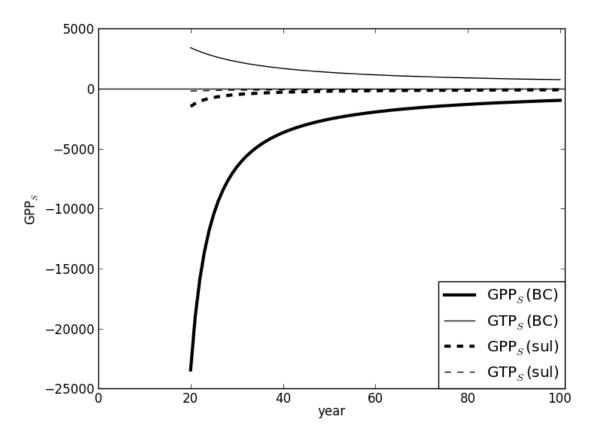


Figure 6. GPP_S (in bold) and GTP_S for 1 kg year⁻¹ sustained emissions of BC and sulphate relative to a 1 kg year⁻¹ sustained emission of CO₂.

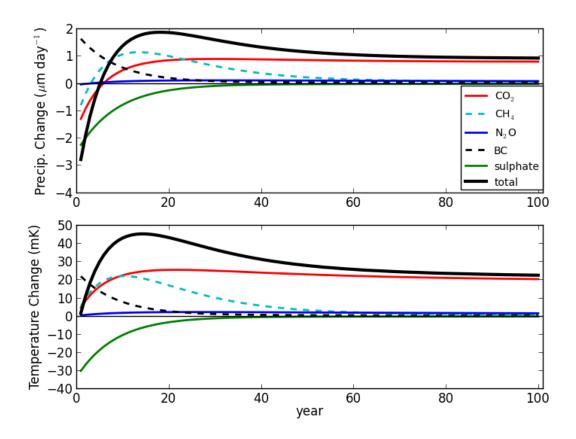


Figure 7. Precipitation change, in μm day⁻¹ (top), and temperature change, in mK, (bottom) in the years after 2008, following a pulse emission in 2008, calculated using the AGPP_P and AGTP_P and using estimated emissions of the species in 2008.

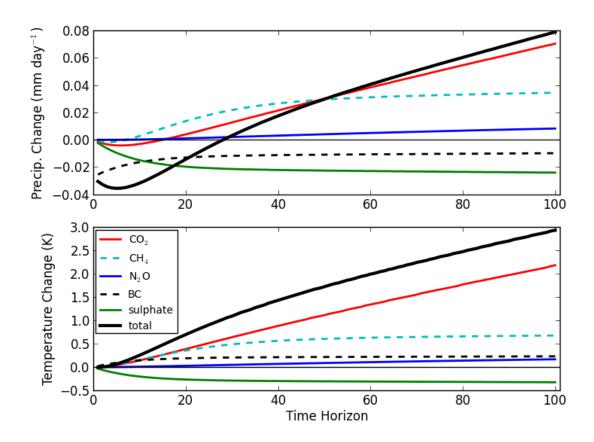


Figure 8. Precipitation change, in mm day⁻¹ (top), and temperature change, in K, (bottom) in the years after 2008, assuming constant emissions at 2008 levels, calculated using the AGPP_S and AGTP_S and using estimated emissions of the species in 2008.

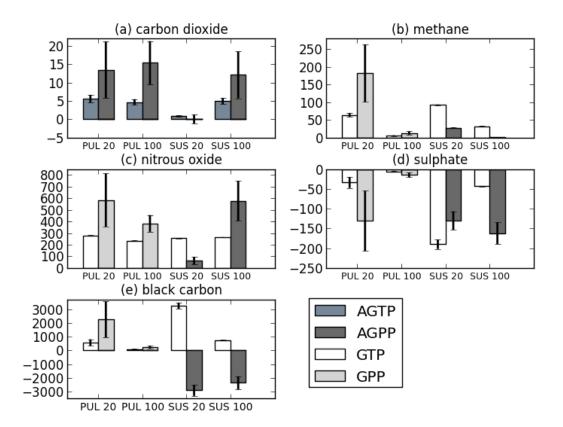


Figure 9: Mean and standard deviations of the AGTP, AGPP, GTP and GPP for both pulse (PUL) and sustained (SUS) emissions for time horizons of 20 and 100 years (which are chosen for illustrative purposes), using 18 different representations of the impulse-response function for temperature change. (a) AGTP and AGPP for carbon dioxide, for both pulse and sustained emissions, and then GTP_P, GPP_P, GTP_S and AGPP_S for (b) methane, (c) nitrous oxide, (d) sulphate and (e) black carbon. For CO₂ the units are 10^{-16} K kg⁻¹ for AGTP_P, 10^{-14} K kg⁻¹ year for AGTP_S, 10^{-18} mm day⁻¹ kg⁻¹ for AGPP_P and 10^{-16} mm day⁻¹ kg⁻¹ year for AGPP_S. The AGPP_S for all other gases are in 10^{-15} mm day⁻¹ kg⁻¹ year.