

# Mechanism for potential strengthening of Atlantic overturning prior to collapse

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**Abstract.** The Atlantic meridional overturning circulation (AMOC) carries large amounts of heat into the North Atlantic influencing climate regionally as well as globally. Paleorecords and simulations with comprehensive climate models suggest that the positive salt-advection feedback may yield a threshold behaviour of the system. That is to say that beyond a certain amount of freshwater flux into the North Atlantic, no meridional overturning circulation can be sustained. Concepts of monitoring the AMOC and identifying its vicinity to the threshold rely on the fact that the volume flux defining the AMOC will be reduced when approaching the threshold. Here we advance conceptual models that have been used in a paradigmatic way to understand the AMOC, by introducing a density-dependent parameterization for the Southern Ocean eddies. This additional degree of freedom uncovers a mechanism by which the AMOC can increase with additional freshwater flux into the North Atlantic, before it reaches the threshold and collapses: an AMOC that is mainly wind-driven will have a constant upwelling as long as the Southern Ocean winds do not change significantly. The downward transport of tracers occurs either in the northern sinking regions or through Southern Ocean eddies. If freshwater is transported, either atmospherically or via horizontal gyres, from the low- to high-latitudes, this would reduce the eddy transport and by continuity increase the northern sinking which defines the AMOC until a threshold is reached at which the AMOC cannot be sustained. If dominant in the real ocean this mechanism would have significant consequences for monitoring the AMOC.

## 1 Introduction

The Atlantic meridional overturning circulation (AMOC) is being considered as one of the tipping elements of the climate system (Lenton et al., 2008). While the definition by Lenton et al. (2008) is

based on the idea that tipping elements respond strongly to a small perturbation, the AMOC might also be a tipping element in the dynamic sense of the word (Levermann et al., 2012). That is to say that a small external perturbation induces a self-amplification feedback by which the circulation enters a qualitatively different state. This self-amplification is due to the salt-advection feedback (Stommel, 1961; Rahmstorf, 1996) and has been found in a number of comprehensive ocean as well as coupled climate models (Manabe and Stouffer, 1993; Rahmstorf et al., 2005; Stouffer et al., 2006b; Hawkins et al., 2011). A cessation of the AMOC would have far-reaching implications for global climate (Vellinga and Wood, 2002) which include (1) a strong reduction of northern hemispheric air and ocean temperatures (Manabe and Stouffer, 1988; Mignot et al., 2007), (2) a reduction in European precipitation and (3) its wind pattern (Laurian et al., 2009), (4) a dynamic sea level increase in the North Atlantic (Levermann et al., 2005; Yin et al., 2009), (5) a perturbation of the Atlantic ecosystem (Schmittner, 2005; Kuhlbrodt et al., 2009), (6) a southward shift in the tropical rain belt and associated impacts on vegetation (Stouffer et al., 2006a) and (7) a perturbation of the Asian monsoon system (Goswami et al., 2006).

Conceptual models to capture the basic aspect of a meridional overturning circulation can be divided into models in which the overturning strength is determined by the meridional density difference in the Atlantic (Stommel, 1961; Rahmstorf, 1996) and those in which its strength is linked to the vertical density structure (Gnanadesikan, 1999). Stommel's model captures the salt-advection feedback in a pure form by resolving only the advection of the active tracers in two fixed-size boxes representing the northern downwelling and southern upwelling regions. The overturning strength is assumed to be proportional to the meridional density difference which was found to be valid in a number of ocean and climate models (e.g. Griesel and Morales-Maqueda, 2006; Rahmstorf, 1996; Schewe and Levermann, 2010). The Stommel-model is however missing a representation of the energy-providing processes for the overturning, such as the Drake-Passage effect and low-latitude mixing (Kuhlbrodt et al., 2007) as well as the influence of the Southern Ocean eddy circulation.

These processes are captured in a conceptual way by the model of Gnanadesikan (1999) which links the overturning to the vertical density profile as represented by the pycnocline depth but treats meridional density differences as a constant. It was shown that this kind of model is not consistent with the fact that the meridional density gradient indeed changes with changing overturning in a number of different climatic conditions (Levermann and Griesel, 2004; Griesel and Morales-Maqueda, 2006). By construction it does not capture the salt-advection feedback and can thereby not be used to study the possibility of a threshold behaviour of the overturning.

There have been a number of attempts to combine these two approaches and thereby to comprise the horizontal tracer-advection with the vertical one (Marzeion and Drange, 2006; Johnson et al., 2007; Fürst and Levermann, 2011).

Here we advance the simplest of the suggested models (Fürst and Levermann, 2011) by introducing an additional parametrisation for the Southern Ocean eddy flux. As found in a comprehensive

coarse resolution ocean model (Levermann and Fürst, 2010) the horizontal scale of the Southern  
60 upwelling region can change and neglecting this change leads to a misrepresentation of the circula-  
tion within the Gnanadesikan (1999) framework. We attempt to complement the conceptual model  
in order to correct for this shortcoming. To this end we add a variable, meridional density difference  
in the southern Atlantic ocean in the scaling of the eddy-induced return flow. As will be shown, this  
allows for a qualitatively different response of the AMOC under freshwater forcing compared to  
65 earlier studies: a growth of the northern deep water formation with increasing freshwater flux from  
low- to high northern latitudes within the Atlantic before the threshold is reached and no AMOC  
in the modelled sense can be sustained. The threshold behaviour found here is consistent with the  
salt-advection feedback in the sense of a net-salinity transport from lower latitudes into the northern  
Atlantic by the overturning as suggested by Rahmstorf (1996). This threshold behaviour has been  
70 shown in box models and complex climate models (Huisman et al., 2010; Weaver et al., 2012) but  
also in observations (Bryden et al., 2011).

This paper is structured as followed: firstly we describe the parametrisation of the transport pro-  
cesses, pycnocline dynamics and salinity dynamics, i.e. horizontal density distribution (Sect. 2).  
The transport processes include the two fundamental driving mechanism (Kuhlbrodt et al., 2007)  
75 which are low-latitude upwelling (Munk, 1966; Munk and Wunsch, 1998; Huang, 1999; Wunsch  
and Ferrari, 2004) and wind-driven upwelling in southern latitudes (Toggweiler and Samuels, 1995,  
1998). In order to examine the behaviour of the model we derived governing equations for the two  
driving mechanisms separately as well as for the full case. The threshold behaviour, as described by  
Stommel (1961) is caused by the salinity advection. For simplicity we keep the temperatures fixed  
80 through-out the paper (Sect. 3). Section 4 discusses the change in the AMOC with increasing fresh-  
water flux into the North Atlantic for the wind-driven case and the full case. Also section 5 discusses  
the behavior of the AMOC under freshwater forcing, but for simulations using a climate model of  
intermediate complexity. We conclude in Sect. 6.

## 2 Model description

85 We use a standard inter hemispheric model with four varying boxes (Fig. 1): (1) a northern box  
representing the northern North Atlantic with deep water formation, (2) an upper low-latitude  
box and (3) a deeper low-latitude box below the pycnocline, (4) a southern box with southern  
upwelling and eddy return flow (Gnanadesikan, 1999). The northern and southern boxes are fixed in  
volume while the low-latitude boxes vary in size according to the dynamically computed pycno-  
90 cline depth. The four meridional tracer transport processes between the boxes control the horizontal  
and vertical density structure on the one hand and they control the overturning on the other hand.  
The density structure, in turn, determines the transport processes. Changes in the vertical density  
structure are described by variations in the pycnocline depth. The horizontal density structure is ex-

pressed by a southern and a northern meridional density difference. They depend on the dynamics of  
95 the active tracers, temperature,  $T$ , and salinity,  $S$ . For simplicity we assume a linear density function  
 $\Delta\rho = \rho_0(\beta_S\Delta S - \alpha_T\Delta T)$  (Stommel, 1961). In order to capture the main feedback for a threshold  
behaviour while keeping the model legible, we include salinity advection and neglect changes in  
temperature. The simplification further is justified because the temperature in the upper layers is  
100 strongly coupled to atmospheric temperature which is to first order determined by the solar insula-  
tion. We thus assume, the ocean temperature in the upper layers to be constant. The high-latitude  
boxes represent strong out-cropping regions which homogenizes the water column and extends the  
argument to depth. In steady state, the fourth box, deeper low-latitudes ocean, is determined by  
the three other boxes. That means the approximation is valid for the whole model in equilibrium  
and temperature is used as an external parameter. The base of our work is the model by Fürst and  
105 Levermann (2011). We use the same parametrisations for the northern deep water formation and  
the upwelling processes. For the eddy return flow we introduce a different scaling by implementing  
southern meridional density difference which has strong influences on the behaviour of the model  
(Sects. 3 and 4).

## 2.1 Tracer transport processes

110 Different scaling for the deep water formation (as summarized in Fürst and Levermann, 2011) have  
been suggested. Here we use a parametrisation suggested by Marotzke (1997) and apply a  $\beta$ -plane-  
approximation to it. The resulting northern sinking scales linearly with the meridional density dif-  
ference and quadratically with the pycnocline depth following geostrophic balance and vertical in-  
tegration.

$$115 \quad m_N = \frac{Cg}{\beta_N L_y^N} \frac{\Delta\rho}{\rho_0} D^2 = C_N \Delta\rho D^2. \quad (1)$$

Because all values are external parameters (Table 1) except the meridional density difference  $\Delta\rho =$   
 $\rho_N - \rho_U$  and the pycnocline depth  $D$ , the parameters are comprised into one constant  $C_N$ . In contrast  
to previous approaches (e.g. Rahmstorf, 1996) the meridional density difference does not span the  
120 whole Atlantic but instead is taken between low and high northern latitudes in accordance with the  
geostrophic balance between the meridional density difference and the North Atlantic Current.

The low-latitude upwelling follows a vertical advection-diffusion balance (Munk and Wunsch,  
1998). That is to say, downward turbulent heat flux is balanced by upward advection. This balance  
with a constant diffusion coefficient for the full upwelling region yields an inverse proportionality  
125 between upward volume transport and pycnocline depth. Again all external parameters are expressed  
by one constant  $C_U$  to obtain

$$m_U = B L_U \frac{\kappa}{D} = \frac{C_U}{D}. \quad (2)$$

The southern upwelling term is considered to be independent of the pycnocline depth and results from the so-called Drake-Passage effect (Toggweiler and Samuels, 1995):

$$m_W = B \frac{\tau_{Dr}}{|f_{Dr}| \rho_0} = C_W. \quad (3)$$

The eddy return flow is parametrised following Gent and McWilliams (1990) which yields a tracer transport proportional to the slope of the outcropping isopycnals. In the formulation of Gnanadesikan (1999) this is represented by a linear dependence on the pycnocline depth divided by a horizontal scale for the outcropping region which is taken to be constant. The assumption of a constant horizontal scale for the outcropping region is not consistent with freshwater hosing experiments in a comprehensive though coarse resolution ocean model (Levermann and Fürst, 2010). Levermann and Fürst (2010) show that the eddy return flow is proportional to pycnocline depth over a variable horizontal scale of the outcropping. Here we attempt to capture variations in the meridional horizontal length scale of the outcropping region by the meridional density difference between the low-latitude ocean and the Southern Ocean,  $\Delta\rho_{SO} = \rho_S - \rho_U$ . We thus use the parametrisation

$$m_E = B A_{GM} \frac{\Delta\rho_{SO}}{\rho_0} \frac{D}{H} = C_E \Delta\rho_{SO} D. \quad (4)$$

As before, all quantities except  $D$  and  $\Delta\rho_{SO}$  are external parameters and compressed into one constant  $C_E$ .

## 2.2 Pycnocline and salinity dynamics

The temporal evolution of the pycnocline is determined by the tracer transport equation following Marzeion and Drange (2006).

$$BL_U \frac{dD}{dt} = m_U + m_W - m_E - m_N \quad (5)$$

Salinity equations for each box are derived from the advection in and out of the box, conserving salinity, as well as the surface fluxes,  $F_N$  and  $F_S$  which represent atmospheric freshwater transport as well as the horizontal gyre transport. The advection scheme follows the arrows shown in Fig. 1.

In computing the temporal changes in total salinity the changes in volume due to the pycnocline dynamics needs to be accounted for.

$$\frac{d}{dt}(V_U S_U) = m_U S_D + m_W S_S - S_U(m_N + m_W) + S_0(F_N + F_S) \quad (6a)$$

$$\frac{d}{dt}(V_N S_N) = m_N(S_U - S_N) - S_0 F_N \quad (6b)$$

$$\frac{d}{dt}(V_S S_S) = m_W(S_D - S_S) + m_E(S_U - S_S) - F_S S_0 \quad (6c)$$

$$\frac{d}{dt}(V_D S_D) = m_N S_N + m_E S_S - S_D(m_U + m_W). \quad (6d)$$

With finite difference method applied to Eqs. (1)–(6), we made numerical simulations which reached in equilibrium the values shown in Table 2 with the parameters given in Table 1.

### 3 Governing equation

165 Here we derive an equation for the steady-state solution of Eqs. (1)–(6) by comprising them into one equation of the oceanic pycnocline,  $D$ . We derive governing equations for the full case as well as for the analytically solvable cases of a purely mixing- and a purely wind-driven cases. The model is limited to positive and real solutions for the pycnocline ( see figure 2) as well as for non-negative tracer transport values. A parameter combination that does not allow for a solution of this kind  
 170 is thereby inconsistent with an overturning circulation as represented by this model. We denote a parameter region for which no such a physical solution exists as an “AMOC-off-state-region”. As in the earlier version of the model (Fürst and Levermann, 2011) we find a threshold behaviour with respect to an increase of the freshwater flux,  $F_N$ , for all three cases. The focus of this study is not to show the existence of such a threshold of all parameter values. But, it is to present a mechanism by  
 175 which the overturning can increase between steady states under different freshwater forcings before the threshold is reached and no AMOC can be sustained.

#### 3.1 Full case

In the full case the governing equation is a polynomial of 10th order in the pycnocline depth (Appendix A1, Eq. A7). Thus solutions can only be found numerically. Of the 10 mathematical roots,  
 180 two are positive and real but of two adjacent solutions only one can be stable. Numerical solutions were obtained in two ways. First by finding the roots of the polynomial (Appendix A1, Eq. A7) and second by time forward integration of the original set of Eqs. (1)–(6) with different initial conditions. The time integration naturally selects the stable solutions. Though this is not a proof by any means, we feel confident to say that the solution with  $D = 616$  m is the stable of the two physical solutions  
 185 (Fig. 3a). The corresponding tracer transport values are provided in Fig. 3b. The northern sinking decreases with increasing freshwater forcing for the parameter set of Table 1. The equation for the northern sinking as it results from the scaling (Eq. 1) and the salinity equations:

$$m_N = -\frac{1}{2}C_N D^2 \alpha \Delta T \pm \sqrt{\frac{1}{4}C_N^2 D^4 \alpha^2 \Delta T^2 - C_N D^2 \beta F_N S_0} \quad (7)$$

190 was also valid in the earlier version of the model (Fürst and Levermann, 2011). Rahmstorf (1996) provides a similar solution for the northern deep water formation with  $k$  as proportionality factor between the northern sinking and the north-south density difference:

$$m_N = -\frac{1}{2}k\alpha(T_S - T_N) \pm \sqrt{\frac{1}{4}k^2\alpha^2(T_S - T_N)^2 + k\beta F_N S_0}. \quad (8)$$

195 In these earlier models only positive roots of the solution yield stable equilibria. That differs from our model where for certain amounts of freshwater forcing the negative sign of the root in Eq. (7) (respectively Eq. 8) needs to be considered, as for example in the wind-driven case discussed below.

The threshold of the overturning is reached when the eddy return flow becomes negative (Fig. 3b, grey shaded area) because the parametrization of the eddy return flow, i.e. the model itself, is only

200 valid for positive values. Therefore, the shift to negative eddy return flow is interpreted as a point of instability of the circulation pattern described by the model. Physically, reaching the threshold means that there is no outcropping of iso-pycnals in the Southern Ocean anymore. Thus the eddy return flow does not follow the physics that is described by the baroclinic instability and thereby it does not follow the parametrisation by Gent and McWilliams (1990). This also establishes a qualitatively different circulation pattern.

It should be noted that also negative freshwater forcing was applied, which might not be applicable with surface transport. However, the threshold freshwater forcing is in the positive range. This is also true for the mixing- and wind- driven case.

210 Besides freshwater forcing from lower latitudes into the northern box only, experiments were performed with freshwater forcing from the lower latitudes into the southern box and from lower latitudes into both southern and northern box. All experiments showed the same behaviour in the overturning as all experiments affect the meridional density differences in the same way.

### 3.2 Mixing-driven case

The purely mixing-driven case is defined by  $C_E = C_W = 0$ . In this case the pycnocline dynamics in steady state (Eq. 5) reduces to  $m_N = m_U = C_U/D$ . As the eddy return flow is eliminated from the equation, this case has not changed compared to the model of Fürst and Levermann (2011): the governing equation is a polynomial of fourth order in pycnocline depth and has one physical solution which decreases with increasing freshwater forcing (Fig. 4a). The overturning decreases until a threshold level (Fig. 4b) which is reached when the pycnocline and therefore the tracer transport processes become complex. The critical northern freshwater flux can be calculated by zero-crossing of the discriminant of the polynomial.

$$F_{N,\text{mixing}}^{\text{crit}} = \frac{3(2C_N)^{1/3}C_U^{2/3}\alpha^{4/3}}{8\beta S_0}|\Delta T|^{4/3} \quad (9)$$

### 3.3 Wind-driven case

225 The purely wind-driven circulation is defined by  $C_U = 0$ . Thus the tracer-transport balance in steady state (Eq. 5) reduces to  $m_N = m_W - m_E$  into which the eddy return flow and the northern sinking are included as functions of the pycnocline depth and external parameters of Table 1 (see Appendix A for a detailed derivation). For the northern sinking the northern salinity difference is calculated via the salinity balance of North Atlantic (Eq. 6b) and inserted into the scaling of the northern sinking (Eq. 1), similarly for the eddy return flow by using the Southern Ocean salinity balance (Eq. 6c). The emerging governing equation is a third order polynomial of the pycnocline depth  $D$  which we

solve analytically.

$$\begin{aligned}
& D^3 C_E C_N \alpha \Delta T \left[ \frac{\beta S_0 (F_N + F_S)}{C_W} + \alpha \Delta T_{SO} \right] \\
& + D^2 \left[ C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + \frac{C_E^2}{C_W^2} (S_0 \beta (F_N + F_S) + C_W \alpha \Delta T_{SO})^2 \right] \\
235 \quad & + D 2 C_E [\beta S_0 (F_N + F_S) + C_W \alpha \Delta T_{SO}] + C_W^2 = 0
\end{aligned}$$

The solutions depend on the sign of the discriminant of the polynomial  $d = (q/2)^2 + (p/3)^3$  with  $p$  and  $q$  defined as:

$$\begin{aligned}
\frac{q}{2} &= \frac{1}{2} \left( \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + C_E^2 A^2}{3 C_E \alpha \Delta T A} \right)^3 - \frac{C_W F_N S_0 \beta + C_W^2 \alpha \Delta T}{3 C_E C_N \alpha^2 \Delta T^2 A} \\
240 \quad & - \frac{C_E C_W A}{3 C_N^2 \alpha^2 \Delta T^2} + \frac{C_W^2}{2 C_E C_N \alpha \Delta T A} \\
\frac{p}{3} &= \frac{6 C_W C_N \alpha \Delta T - 1}{9 C_N^2 \alpha^2 \Delta T^2} - \frac{F_N S_0 \beta + C_W \alpha \Delta T}{9 C_E^2 C_N^2 \alpha^2 \Delta T^2 A^2} \\
& \text{with } A = \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right).
\end{aligned}$$

A polynomial of third order has either one root (Appendix A2, Eq. A10) if the discriminant is  
245 positive, or three roots (Appendix A2, Eq. A11) if the discriminant is negative which is the case for  
the parameters of Table 1 near the threshold (Fig. 5). Only one of the three mathematical roots is  
a physical solution of equilibrium state of the model because one root is negative (Fig. 5, solution 1)  
and the other solution has a negative northern sinking and the pycnocline values are out of range of  
the ocean depth (Fig. 5, solution 0). No physical solution exists, when the eddy return flow becomes  
250 negative. At this threshold the discriminant of the governing equation has a negative pole which  
can be used to calculate the critical freshwater flux. In the following we describe a more straight  
forward way to give dependencies of the critical freshwater flux. Assuming steady state for the  
salinity balance of the upper low-latitude box (Eq. 6a equal to zero, with  $m_U = 0$ ) and for the  
tracer transport balance ( $m_E + m_N = m_W = C_W$ ), the salinity difference between the Southern  
255 Ocean and the upper low-latitudes emerges:

$$\Delta S_{SO} = S_S - S_U = -\frac{S_0}{C_W} (F_N + F_S).$$

The salinity difference contains no variables. As the temperature dynamics are not considered in  
this model, the horizontal density difference between these two boxes is constant for a fixed set of  
260 parameters.

$$\Delta \rho_{SO} = \beta \Delta S_{SO} - \alpha \Delta T_{SO} = -\beta \frac{S_0}{C_W} (F_N + F_S) - \alpha \Delta T_{SO} \quad (10)$$

The critical eddy return flow is equal to zero. Using the definition of the flow (Eq. 4) and the fact that  
the critical pycnocline depth is far in the positive range, Eq. (10) can be set to zero at the threshold



265 level. The critical freshwater flow becomes:

$$F_{N,\text{wind}}^{\text{crit}} = -\frac{\alpha\Delta T_{\text{SO}}C_W}{S_0\beta} - F_S$$

The critical northern freshwater flow depends linearly on the southern temperature difference and on the southern wind stress (via  $C_W$ ) and a higher southern freshwater flux would lower the critical  
270 northern freshwater flow. Please note that this is a significant difference to previous approaches (Fürst and Levermann, 2011; Rahmstorf, 1996), where the critical freshwater flow is in first or higher order (Eq. 9) sensitive to the northern temperature difference which has no influence onto the critical freshwater flux in this case.

#### 4 Freshwater-induced AMOC strengthening

275 The introduction of the southern density difference as a variable changing the eddy return flow results in a mechanism that has rarely been reported before: an increasing overturning under northern freshwater forcing prior to a threshold in freshwater beyond no AMOC, as described here, can be sustained. Cimadoribus et al. (2014) found a similar behaviour in a different box model, but under freshwater forcing from the southern into the northern Atlantic. The mechanism in the model presented here is simple: a freshwater flux from low-latitudes into the high northern latitudes reduces  
280 the eddy return flow. If this reduction is not compensated by a reduction in mixing-driven upwelling (as for example in a mainly wind-driven AMOC) then due to continuity northern sinking has to increase since Southern Ocean upwelling is constant. Furthermore, it should be noted that this result depends on the assumption that the northern sinking,  $m_N$ , is a function of the square of the pycnocline depth and the meridional density difference (see equation 1). Consequently, only solutions of  
285 the pycnocline depth for the governing equation (see equation A7 and A9) under freshwater forcing which fulfill the parametrization of the northern sinking (see equation 1) are allowed. In general, the changes in the meridional density differences are the main driver for changes in the northern sinking and the eddy return flow, i.e. the drivers for the freshwater induced strengthening of the AMOC.  
290 Changes in the vertical density differences, implemented here as changes in the pycnocline depth, stabilize the overturning circulation. The mechanism of an AMOC strengthening under freshwater forcing is always dominant in the wind-driven case which we will proof at the end of this section. In the full case the mechanism takes not effect for the parameters of Table 1 but it emerges if the Southern Ocean temperature difference is changed in such a way as to make the mixing less relevant  
295 (Fig. 6).

##### 4.1 Full case

In order to gain a better understanding of this behaviour, the tracer transport processes balance in steady state (Eq. 5 equal to zero) is differentiated with respect to the northern freshwater flux. That

gives an equation for the derivative of northern sinking:

$$300 \quad \frac{dm_N}{dF_N} = -\frac{dm_E}{dF_N} + \frac{dm_U}{dF_N} \quad (11)$$

Using the parametrisations of the eddy return flow (Eq. 4) and low-latitude upwelling (Eq. 2), Eq. (11) yields

$$305 \quad \frac{dm_N}{dF_N} = -\left(\frac{C_U}{D^2} + C_E \Delta \rho_{SO}\right) \frac{\partial D}{\partial F_N} - C_E D \frac{\partial \Delta \rho_{SO}}{\partial F_N}.$$

The polynomial consists of two terms of opposing sign: the first term on the left depends on the change of pycnocline depth (representing the vertical density structure) with increasing freshwater flux. Since this derivative,  $\frac{\partial D}{\partial F_N}$ , is generally positive the full term is negative. The second term is positive since the horizontal density difference in the Southern Ocean declines when  $F_N$  is increased.

310 The sign of the derivative of the northern sinking is determined by the ratio between the two terms. Thus strongly increasing pycnocline depth, i.e. strong positive changes in vertical density structure, shift the overturning to a decreasing threshold behaviour. If the southern meridional density difference decreases stronger (in absolute values), then the overturning rises under freshwater forcing. The crucial point is that the absolute value of pycnocline depth is present in the term with the derivative of  
 315 southern meridional density difference. That means rising pycnocline depth also amplifies the term that depends on horizontal density structure and vice versa for the meridional density difference. A stronger statement can be derived for the purely wind-driven case.

## 4.2 Wind-driven case

Upwelling in the lower latitudes amplifies the decreasing of northern sinking with increasing fresh-  
 320 water flow. Therefore, the wind-driven case provides a better example and a clearer image. Without low-latitude upwelling the derivative of northern sinking (Eq. 11) equals the negative derivative of the eddy return flow ( $dm_N/dF_N = -dm_E/dF_N$ ). From the scaling of the eddy return flow (Eq. 4) and the derivative of the southern horizontal density difference (Eq. 10) the derivative of the northern sinking emerges.

$$325 \quad \begin{aligned} \frac{dm_N}{dF_N} &= -C_E \Delta \rho_{SO} \frac{\partial D}{\partial F_N} - C_E D \frac{\partial \Delta \rho_{SO}}{\partial F_N} \\ &= C_E \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right) \frac{\partial D}{\partial F_N} + C_E D \frac{S_0 \beta}{C_W} \end{aligned}$$

Now, solely the term depending on the negative southern density difference could diminish the derivative. For the values given in Table 1,  $\frac{\partial D}{\partial F_N} \simeq \frac{100 \text{ m}}{0.1 \text{ Sv}}$ , and  $D \simeq 1000 \text{ m}$ , the derivative is far  
 330 in the positive range ( $\frac{\partial m_N}{\partial F_N} \simeq 5000$ ). In order to calculate the critical derivative, we use again the fact that the southern density difference equals zero at the threshold.

$$\left( \frac{dm_N}{dF_N} \right)_{\text{crit}} = C_E D_{\text{crit}} \frac{S_0 \beta}{C_W} > 0$$

The emerging critical derivative depends only on positive constants and the positive critical pycnocline depth, i.e. the overturning always increases close to the threshold. This result is not surprising in light of the heuristic explanation given above, but it is not trivial due to the still complex vertical and horizontal density dynamics.

## 5 Climate model experiments

In order to investigate the possibility of the occurrence of a freshwater induced AMOC strengthening in a more complex climate model experiments were performed with the University of Victoria Earth System Climate Model, version 2.9 (UVic ESCM). UVic ESCM 2.9 is a model of intermediate complexity, with a simple 1-dimensional atmosphere but a 3-dimensional dynamic ocean (Weaver et al., 2001; Eby et al., 2009). The model is forced with a constant freshwater flux, ranging from 0.025Sv to 0.2Sv, and run to equilibrium over 4300 years. Freshwater was transferred from the southern Atlantic (10°S to 30°S) into the northern Atlantic (10°N to 30°N) in all simulations. The maximum overturning, averaged over 1000 years, increases for a freshwater forcing of 0.075Sv before it declines at 0.1Sv (see figure 7). It creases under a freshwater forcing of 0.16Sv or higher (see figure 7). The AMOC strengthening is less pronounced compared to the box model behavior. However, due to the strong differences between the box model and UVic ESCM slightly different behaviors can be expected. Especially differences in the freshwater forcing and the lack of thermal feedbacks in the box model lead to different overturning behavior between the models. In the simulations using UVic ESCM the freshwater forcing is applied via a constant surface salinity flux because the simulations are time dependent. In the box model, a set amount of salinity flux is applied to one whole box (negative in the northern box and positive in the lower box) because instantaneous equilibrium is assumed. Also, a comparison of the location of the freshwater forcing is not straight forward because the latitudinal extension of the boxes is not specified due to the conceptual nature of the box model. Furthermore, the southern ocean is not well represented in complex climate models, especially eddy flows. These experiments show that an increase of the AMOC under freshwater forcing is a possible behavior of the overturning. However, further experiments would be needed to investigate the robustness of this behavior.

## 6 Conclusion and discussion

The conceptual model of the Atlantic overturning presented here builds on a previous model (Fürst and Levermann, 2011) and advances the model by the introduction of a dynamic southern ocean density difference for the eddy return flow as imposed by comparison with comprehensive ocean model results (Levermann and Fürst, 2010). As a first result the model reproduces the qualitative result that a threshold behaviour is a robust feature that is independent of the driving mechanism, i.e. it is present in a mixing-, a wind-driven as well as in a combined case. The regime of existence

of a solution for the overturning for a specific parameter combination is defined by the simultaneous compliance of a number of conditions, e.g. positive volume fluxes and pycnocline depth. In the presented model the threshold is generally reached when the eddy return flow becomes negative. Similar to the predecessor of the model also here the threshold is associated with the salt-advection feedback. As suggested by Rahmstorf (1996), a threshold thus only exists when the salinity in the low-latitude box is higher than in the northern box. This is the case here (see Table 2). Whether the real ocean is in a bistable regime and thereby exhibits a threshold behaviour is of yet unclear. According to a diagnostic by Rahmstorf (1996), an overturning is bistable if the overturning carries a net salinity transport at 35 N. This diagnostic was confirmed to be valid in a comprehensive climate model (Dijkstra, 2007) and is discussed in depth by Hofmann and Rahmstorf (2009). Following this diagnostic most climate models do not show a threshold behaviour in earlier studies (Drijfhout et al., 2010). However, in a more recent model in-comparison study the majority of climate models do show a threshold behaviour (Weaver et al., 2012). Also observational data indicates that the real ocean is in a bistable regime (Bryden et al., 2011), i.e. the current circulation pattern could change after reaching a threshold. It should be noted that the model presented here does not capture an "off-state" of the circulation, i.e. describing a circulation pattern after the threshold in freshwater forcing has been crossed. There are models showing an inverse circulation, which is sometimes associated with the Antarctic Bottom Water filling up the Atlantic (Rahmstorf et al., 2005) and other models show a seemingly stagnant ocean (Stouffer et al., 2006b). Neither of these patterns would be properly captured by the physics that is incorporated in the conceptual model presented here. Therefore, a bistable situation can not be described but rather a threshold behaviour. This threshold behaviour shows that beyond a certain freshwater flux the circulation in the Atlantic cannot be captured by the conceptual model and is thereby not a classic overturning circulation as presently observed.

The main result is the observation that the overturning can increase prior to its collapse in response to a freshwater flux from low-latitudes to high northern latitudes. Previous models including the base models (Johnson et al., 2007; Marzeion and Drange, 2006; Fürst and Levermann, 2011) show the opposite behaviour, similar to the bifurcation in the initial model of Stommel (1961). The emergence of the effect depends on the inclusion of Southern Ocean winds as a driving-mechanism for the overturning and the inclusion of a dynamic southern ocean horizontal density difference. It thus does not include in the mixing-driven case. Thus our model has opposite behavior prior to reaching the threshold depending on whether the circulation is wind- or mixing-driven.

This has strong implications for potential monitoring systems that aim to detect the vicinity to the threshold. Methods that depend on the decline of the overturning prior to the threshold for example in order to detect an increase in variability might not be suitable in a situation (Lenton, 2011; Scheffer et al., 2009) in which the presented mechanism is relevant. However, applicability of these findings for monitoring purposes are limited as the presented results refer to a system in equilibrium, and not a time dependent state as we see under current global warming.

405 Whether the mechanism described here is dominant in the real ocean is beyond the scope of this  
 paper. This study presents the physical processes which need to be investigated with compre-  
 hensive quantitative models and verified against observation in order to assess its relevance. Though  
 a large number of so-called water hosing experiments have been carried out (e.g. Manabe and Stouf-  
 fer, 1995; Rahmstorf et al., 2005; Stouffer et al., 2007), few studies have focussed on freshwater  
 410 transport from low- to high-latitudes. We were able to show a strengthening of the AMOC under  
 freshwater forcing prior to a decline of the overturning by prescribing different amounts of constant  
 freshwater transport from low latitudes in the southern Atlantic into the northern Atlantic. How-  
 ever, this behavior is not strongly pronounced. Thus further experiments are needed in order to find  
 whether the mechanism is indeed relevant for the real ocean.

## 415 **Appendix A: Analytical calculations**

### **A1 Full case**

The salinities are exchanged by salinity differences between the boxes except the salinity of the  
 northern box. The new salinity variables are defined as  $\Delta S = S_N - S_U$ ,  $\Delta S_D = S_N - S_D$ ,  $\Delta S_{SO} =$   
 $S_S - S_U$ , and  $S_N$ . The salinity balance of the northern box gives for the northern salinity difference:

$$420 \quad \Delta S = -\frac{S_0 F_N}{m_N}. \quad (\text{A1})$$

The scaling of the northern sinking (Eq. 1) with the linearly scaling of the meridional density differ-  
 ence  $\Delta \rho = \beta \Delta S - \alpha \Delta T$  and Eq. (A1) yields into a quadratic polynomial of  $m_N$ .

$$425 \quad 0 = m_N^2 + m_N C_N D^2 \alpha \Delta T + C_N D^2 \beta F_N S_0 \quad (\text{A2})$$

It has the solution:

$$m_N = -\frac{1}{2} C_N D^2 \alpha \Delta T \pm \sqrt{\frac{1}{4} C_N^2 D^4 \alpha^2 \Delta T^2 - C_N D^2 \beta F_N S_0}. \quad (\text{A3})$$

The salinity balance of the upper box can be used to calculate  $\Delta S_D$ :

$$430 \quad \Delta S_D = \frac{m_W}{m_U} \Delta S_{SO} + \Delta S + \frac{S_0}{m_U} (F_N + F_S). \quad (\text{A4})$$

The salinity balance of the southern box combined with Eq. (A4) results into an equation for the  
 southern salinity difference.

$$435 \quad \Delta S_{SO} = -S_0 \frac{m_W (F_N + F_S) + m_U F_S}{m_W^2 + m_W m_U + m_E m_U} \quad (\text{A5})$$

The scaling of the eddy return flow (Eq. 4), the linear density function for southern meridional den-  
 sity difference ( $\Delta \rho_{SO} = \beta \Delta S_{SO} - \alpha \Delta T_{SO}$ ), and Eq. (A5) can be collapsed into a quadratic equation  
 for  $m_E$ .

$$440 \quad 0 = m_E + C_E D \beta S_0 \frac{m_W (F_N + F_S) + m_U F_S}{m_W^2 + m_W m_U + m_E m_U} + C_E D \alpha \Delta T_{SO} \quad (\text{A6})$$

It has the solution:

$$m_E = -\frac{1}{2} \left( \frac{m_W^2}{m_U} + m_W + C_E D \alpha \Delta T_{\text{so}} \right) + \sqrt{\frac{1}{4} \left( \frac{m_W^2}{m_U} + m_W + C_E D \alpha \Delta T_{\text{so}} \right)^2 - C_E D \beta S_0 \left( \frac{m_W}{m_U} (F_N + F_S) + F_S \right) - C_E D \alpha \Delta T_{\text{so}} \left( \frac{m_W^2}{m_U} + m_W \right)}.$$

445 The governing equation of the pycnocline depth emerges by using Eq. (A6) and replacing the eddy return flow by  $m_E = m_U + m_W - m_N$ ,  $m_N^2$  by Eq. (A2), and the upwelling transport processes,  $m_U$  and  $m_W$ , by their scaling (Eqs. 2 and 3).

$$\begin{aligned} & D^{10} C_E C_U C_W C_N^2 \alpha^2 \Delta T^2 [S_0 \beta (F_N + F_S) + C_W \alpha \Delta T_{\text{so}}] \\ & + D^9 C_N \alpha \Delta T [C_E C_W (C_W^2 + C_E C_U \alpha \Delta T_{\text{so}}) (F_N S_0 \beta + F_S S_0 \beta + C_W \alpha \Delta T_{\text{so}}) \\ 450 & + C_U C_N (C_W^2 F_N S_0 \beta + C_W^3 \alpha \Delta T + 2 C_E C_U C_W \alpha^2 \Delta T \Delta T_{\text{so}} + C_E C_U S_0 \alpha \beta (F_S \Delta T + F_N \Delta T_{\text{so}}))] \\ & + D^8 [C_E^2 C_W^2 (F_N S_0 \beta + F_S S_0 \beta + C_W \alpha \Delta T_{\text{so}})^2 \\ & + C_N^2 C_U^2 (F_N^2 S_0^2 \beta^2 + 3 C_W F_N S_0 \alpha \beta \Delta T + \alpha^2 \Delta T^2 (3 C_W^2 + C_E C_U \alpha \Delta T_{\text{so}})) \\ & + C_N (C_W^4 F_N S_0 \beta + C_W^5 \alpha \Delta T + C_E C_U C_W^2 S_0 \alpha \beta \Delta T (3 F_N + 4 F_S) + 6 C_E C_U C_W^3 \alpha^2 \Delta T \Delta T_{\text{so}} \\ & + C_E^2 C_U^2 S_0 \alpha^2 \beta \Delta T_{\text{so}} (F_S \Delta T + F_N \Delta T_{\text{so}}) \\ 455 & + 2 C_E C_U C_W (-F_N^2 S_0^2 \beta^2 - F_N F_S S_0^2 \beta^2 + C_E C_U \alpha^3 \Delta T \Delta T_{\text{so}}^2))] \\ & + D^7 [C_N^2 C_U^3 \alpha \Delta T (2 F_N S_0 \beta + 3 C_W \alpha \Delta T) \\ & + 2 C_E C_W (F_N S_0 \beta + F_S S_0 \beta + C_W \alpha \Delta T_{\text{so}}) (C_W^3 + C_E C_U F_S S_0 \beta + 2 C_E C_U C_W \alpha \Delta T_{\text{so}}) \\ & + C_N C_U (4 C_W^3 F_N S_0 \beta + 6 C_W^4 \alpha \Delta T + 12 C_E C_U C_W^2 \alpha^2 \Delta T \Delta T_{\text{so}} \\ & + C_E C_U (-2 F_N F_S S_0^2 \beta^2 + C_E C_U \alpha^3 \Delta T \Delta T_{\text{so}}^2) + C_E C_U C_W S_0 \alpha \beta (5 F_S \Delta T + 2 F_N (\Delta T + \Delta T_{\text{so}}))] \\ 460 & + D^6 [C_W^6 + 2 C_U C_W^3 (C_E S_0 \beta (3 F_N + 4 F_S) + 7 C_N C_U \alpha \Delta T) + 10 C_E C_U C_W^4 \alpha \Delta T_{\text{so}} \\ & + 2 C_E C_U^2 C_W \alpha \Delta T_{\text{so}} (C_E S_0 \beta (F_N + 3 F_S) + 5 C_N C_U \alpha \Delta T) + C_U^2 C_W^2 (7 C_N F_N S_0 \beta + 6 C_E^2 \alpha^2 \Delta T_{\text{so}}^2) \\ & + C_U^2 (C_E^2 F_S^2 S_0^2 \beta^2 + C_N^2 C_U^2 \alpha^2 \Delta T^2 + 2 C_E C_N C_U S_0 \alpha \beta (F_S \Delta T + F_N \Delta T_{\text{so}}))] \\ & + D^5 C_U [6 C_W^5 + 2 C_U C_W^2 (3 C_E S_0 \beta (F_N + 2 F_S) + 8 C_N C_U \alpha \Delta T) + 20 C_E C_U C_W^3 \alpha \Delta T_{\text{so}} \\ & + C_E C_U^2 \alpha \Delta T_{\text{so}} (2 C_E F_S S_0 \beta + 3 C_N C_U \alpha \Delta T) + 2 C_U^2 C_W (3 C_N F_N S_0 \beta + 2 C_E^2 \alpha^2 \Delta T_{\text{so}}^2)] \\ 465 & + D^4 C_U^2 [15 C_W^4 + C_U C_W (2 C_E S_0 \beta (F_N + 4 F_S) + 9 C_N C_U \alpha \Delta T) + 20 C_E C_U C_W^2 \alpha \Delta T_{\text{so}} \\ & + C_U^2 (2 C_N F_N S_0 \beta + C_E^2 \alpha^2 \Delta T_{\text{so}}^2)] \\ & + D^3 2 C_U^3 [10 C_W^3 + C_U C_E F_S S_0 \beta + C_N C_U^2 \alpha \Delta T + 5 C_E C_U C_W \alpha \Delta T_{\text{so}}] \\ & + D^2 C_U^4 [15 C_W^2 + 2 C_E C_U \alpha \Delta T_{\text{so}}] + D 6 C_U^5 C_W + C_U^6 = 0 \end{aligned} \quad (\text{A7})$$

470 **A2 Wind-driven case**

For a wind-driven overturning the upwelling in the lower latitudes is zero by setting  $C_U = 0$ . Thus the tracer transport balance in steady state (5 equal to zero) reduces to  $m_W = m_N + m_E$ . Differences in salinity are defined as in the full problem and the salinity balance in the northern box is the same as in the full problem. Therefore Eqs. (A1)–(A3) are valid. Using the salinity balance of the southern  
475 box, in this case the southern salinity difference reduces to:

$$\Delta S_{SO} = -\frac{S_0(F_N + F_S)}{m_W}.$$

For the eddy return flow it follows:

$$m_E = -C_E D \beta \frac{S_0(F_N + F_S)}{C_W} - \alpha \Delta T_{SO} C_E D. \quad (\text{A8})$$

480 Replacing the northern sinking by Eq. (A3) and the eddy return flow by Eq. (A8) in the tracer transport balance the governing equation of the pycnocline depth emerges.

$$\begin{aligned} & D^3 C_E C_N \alpha \Delta T \left[ \frac{\beta S_0(F_N + F_S)}{C_W} + \alpha \Delta T_{SO} \right] \\ & + D^2 \left[ C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + \frac{C_E^2}{C_W^2} (S_0 \beta (F_N + F_S) + C_W \alpha \Delta T_{SO})^2 \right] \\ & + D 2 C_E [\beta S_0 (F_N + F_S) + C_W \alpha \Delta T_{SO}] + C_W^2 = 0 \end{aligned} \quad (\text{A9})$$

485 The solutions of the polynomial depend on the sign of the discriminant  $d = (q/2)^2 + (p/3)^3$  with  $p$  and  $q$  defined as:

$$\begin{aligned} \frac{q}{2} &= \frac{1}{2} \left( \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + C_E^2 A^2}{3 C_E \alpha \Delta T A} \right)^3 - \frac{C_W F_N S_0 \beta + C_W^2 \alpha \Delta T}{3 C_E C_N \alpha^2 \Delta T^2 A} \\ &\quad - \frac{C_E C_W A}{3 C_N^2 \alpha^2 \Delta T^2} + \frac{C_W^2}{2 C_E C_N \alpha \Delta T A} \\ \frac{p}{3} &= \frac{6 C_W C_N \alpha \Delta T - 1}{9 C_N^2 \alpha^2 \Delta T^2} - \frac{F_N S_0 \beta + C_W \alpha \Delta T}{9 C_E^2 C_N^2 \alpha^2 \Delta T^2 A^2} \\ \text{with } A &= \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right). \end{aligned}$$

If the discriminant is positive the governing equation has one real solution.

$$490 \quad D = \sqrt[3]{-\frac{q}{2} + \sqrt{\left(\frac{q}{2}\right)^2 + \left(\frac{p}{3}\right)^3}} + \sqrt[3]{-\frac{q}{2} - \sqrt{\left(\frac{q}{2}\right)^2 + \left(\frac{p}{3}\right)^3}} \quad (\text{A10})$$

For a negative discriminant there are three real solutions.

$$\begin{aligned} D_1 &= 2 \sqrt[3]{-\frac{p}{3}} \cos \left( \frac{1}{3} \arccos \left( -\frac{3q}{2p \sqrt{-\frac{p}{3}}} \right) \right) - \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \\ &\quad + \frac{C_E^2 \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)^2}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \\ &\quad - \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + C_E^2 \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)^2}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \\ 495 \quad D_2 &= 2 \sqrt[3]{-\frac{p}{3}} \cos \left( \frac{1}{3} \arccos \left( -\frac{3q}{2p \sqrt{-\frac{p}{3}}} \right) + \frac{2}{3} \pi \right) \end{aligned}$$



$$\begin{aligned}
& - \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} + \frac{C_E^2 \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)^2}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \\
& - \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + C_E^2 \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)^2}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \\
D_3 = & 2 \sqrt{-\frac{p}{3}} \cos \left( \frac{1}{3} \arccos \left( -\frac{3q}{2p \sqrt{-\frac{p}{3}}} \right) + \frac{4}{3} \pi \right) \\
& - \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} + \frac{C_E^2 \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)^2}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \\
& - \frac{C_N F_N S_0 \beta + C_N C_W \alpha \Delta T + C_E^2 \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)^2}{3 C_E C_N \alpha \Delta T \left( \frac{S_0 \beta}{C_W} (F_N + F_S) + \alpha \Delta T_{SO} \right)} \tag{A11}
\end{aligned}$$

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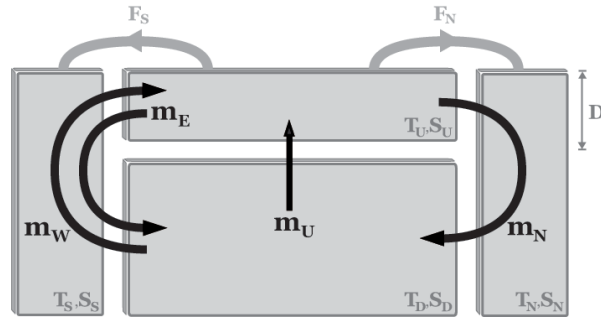
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**Table 1.** Physical parameters for used for the model.

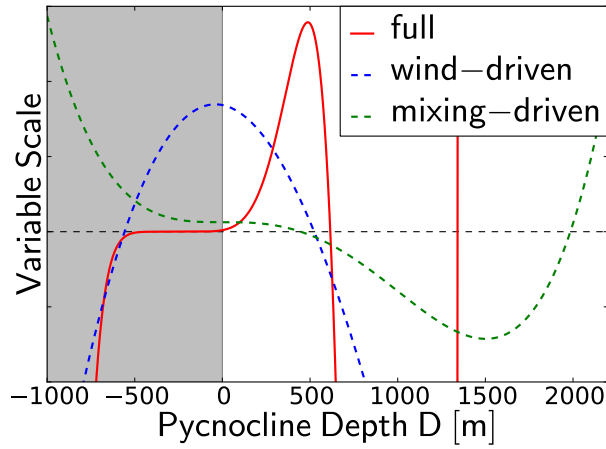
Parameter	Value	Unit	Description
Geometry			
$H$	$4 \times 10^3$	m	Average depth of the Atlantic Ocean basin
$B$	$1 \times 10^7$	m	Average width of the Atlantic Ocean
$L_N$	$3.34 \times 10^6$	m	Meridional extend of the northern box
$L_U$	$8.90 \times 10^6$	m	Meridional extend of the tropical box
$L_S$	$3.34 \times 10^6$	m	Meridional extend of the southern box
Stratification			
$\rho_0$	1027	$\text{kg m}^{-3}$	Average density of the Atlantic Ocean
$S_0$	35	psu	Average salinity of the Atlantic ocean
$L_y^N$	$1.5 \times 10^6$	m	Meridional extent of the northern outcropping
$A_{GM}$	$1 \times 10^6$	$\text{m}^2 \text{s}^{-1}$	Thickness diffusivity
$\kappa$	$4 \times 10^{-5}$	$\text{m}^2 \text{s}^{-1}$	Background vertical diffusivity
$\alpha_T$	$2.1 \times 10^{-4}$	$1 \text{ }^\circ\text{C}^{-1}$	Thermal coefficient for isobars
$\alpha$		$\text{kg (m}^3 \text{ }^\circ\text{C)}^{-1}$	Product of $\rho_0$ and $\alpha_T$
$\beta_S$	$8 \times 10^{-4}$	$1 \text{ psu}^{-1}$	Haline coefficient for isobars
$\beta$		$\text{kg (m}^3 \text{ psu)}^{-1}$	Product of $\rho_0$ and $\beta_S$
$C$	0.1	–	Constant accounting for geometry and stratification
External forcing			
$\beta_N$	$2 \times 10^{-11}$	$1 \text{ ms}^{-1}$	Coefficient for $\beta$ -plane approximation in the North Atlantic
$f_{Dr}$	$-7.5 \times 10^{-5}$	$1 \text{ s}^{-1}$	Coriolis parameter in the Drake Passage
$\tau_{Dr}$	0.1	$\text{N m}^{-2}$	Average zonal wind stress in the Drake Passage
$F_N$	0.1	Sv	Northern meridional atmospheric freshwater transport
$F_S$	0.1	Sv	Southern meridional atmospheric freshwater transport
$T_N$	5.0	$^\circ\text{C}$	Temperature of the northern box
$T_U$	12.5	$^\circ\text{C}$	Temperature of the tropical surface box
$T_S$	7.0	$^\circ\text{C}$	Temperature of the southern box

**Table 2.** Numerical solution of the model by applying finite difference method on Eqs. (1)–(6). Equilibrium state is obtained after 2000 yr with a time step of 14 days and the starting conditions: Salinities set to 35 psu and the pycnocline depth set to 500 m.

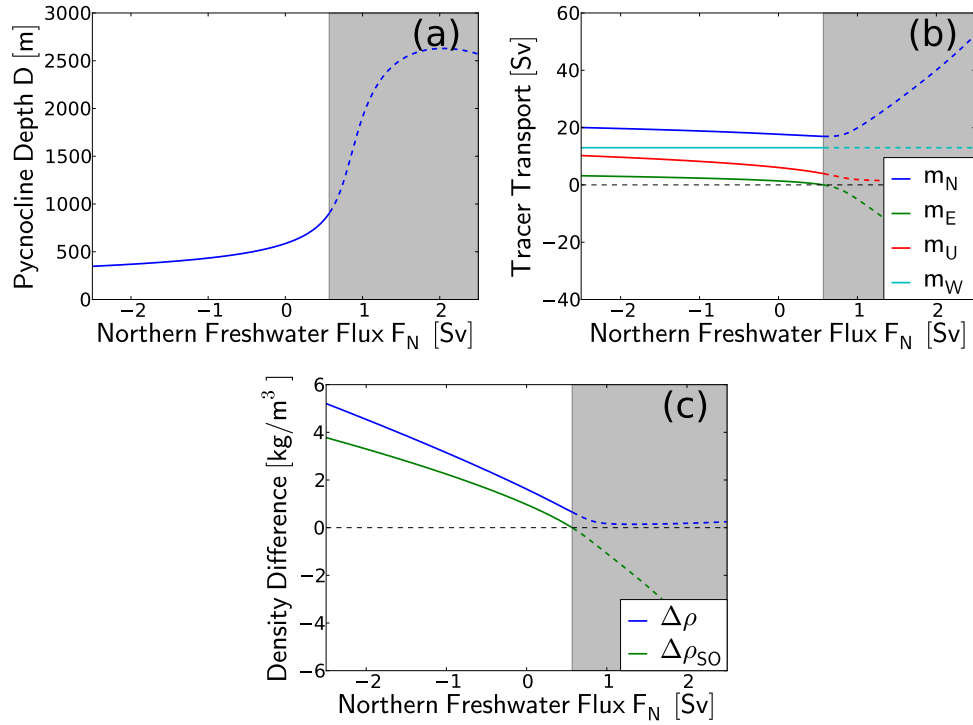
Name		Value
Salinities	$S_N$	35.04 psu
	$S_U$	35.24 psu
	$S_D$	35.02 psu
	$S_S$	34.79 psu
Tracer transports	$m_U$	17.5 Sv
	$m_U$	5.8 Sv
	$m_W$	13.0 Sv
	$m_E$	1.2 Sv
Meridional density differences	$\Delta\rho$	$1.45 \text{ kg m}^{-3}$
	$\Delta\rho_{SO}$	$0.82 \text{ kg m}^{-3}$
Pycnocline depth	$D$	615 m



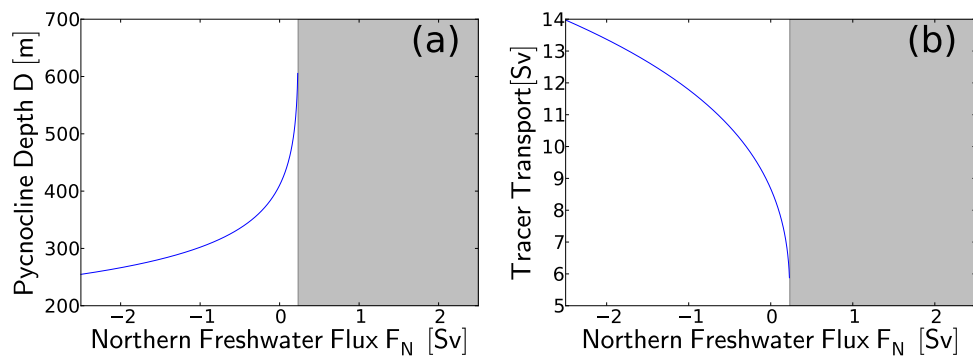
**Figure 1.** Schematic of the conceptual model as suggested in Fürst and Levermann (2011) and used here. The depth of the pycnocline  $D$  is determined by the balance between the northern deep water formation  $m_N$ , the upwelling in the low-latitudes  $m_U$  in response to downward mixing, the Ekman upwelling  $m_W$  and the eddy-induced return flow  $m_E$ . Salinity is advected along with these transport processes and determines together with a fixed temperature distribution the horizontal density differences. The differences are between low-latitude box and northern box,  $\Delta\rho$ , and low-latitude and southern box,  $\Delta\rho_{SO}$ , respectively. The density differences, in turn, determines the northern sinking,  $m_N \propto D^2 \Delta\rho$ , and the eddy-induced return flow,  $m_E \propto D \Delta\rho_{SO}$ .



**Figure 2.** Trend of the governing equation for the full case (red line), the wind-driven case ( $m_U = 0$ , blue line) and the mixing-driven case ( $m_W = m_E = 0$ , green line). The intersections with zero (black dashed line) are solutions of the polynomial but those in the grey shadowed area correspond to a negative pycnocline depth. Therefore they are not physical. In all three cases there are two positive solutions, a lower stable, physical one  $D$  and a higher unstable or non-physical one  $\hat{D}$ . In the wind-driven case the non-physical solution is out of range of the pycnocline but is shown in Fig. 5. For the full case the solutions are  $D = 616$  m and  $\hat{D} = 1342$  m, for the wind-driven case they are  $D = 523$  m and  $\hat{D} = 6190$  m and for the mixing-driven case they are  $D = 446$  m and  $\hat{D} = 1985$  m.

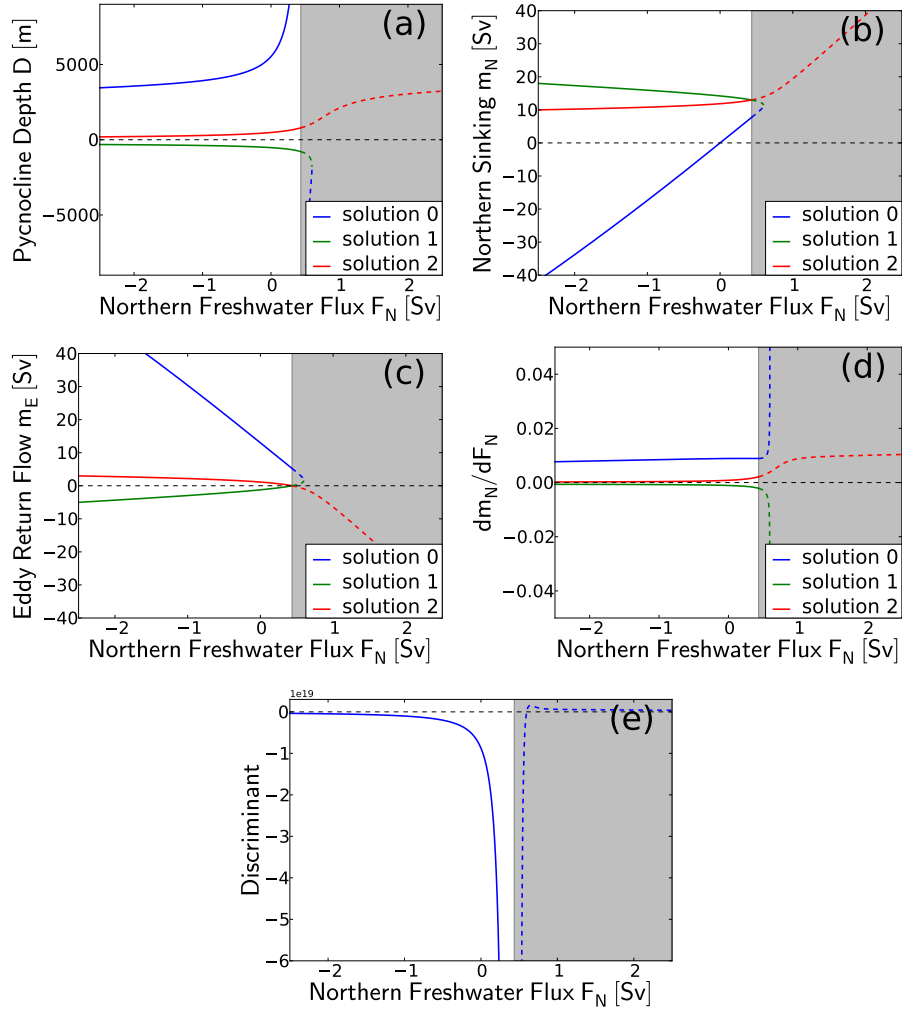


**Figure 3.** In steady state only one real stable solution of governing equation of the full exists which increases under freshwater forcing (a). The tracer transport processes show different behaviours (b). The eddy return flow  $m_E$  decreases (b, green line) until it becomes negative and the break down of circulation is reached (grey shaded area). Also the density difference between the southern box and the low-latitudinal box,  $\Delta\rho_{SO}$ , crosses zero at the threshold level (c, green line).

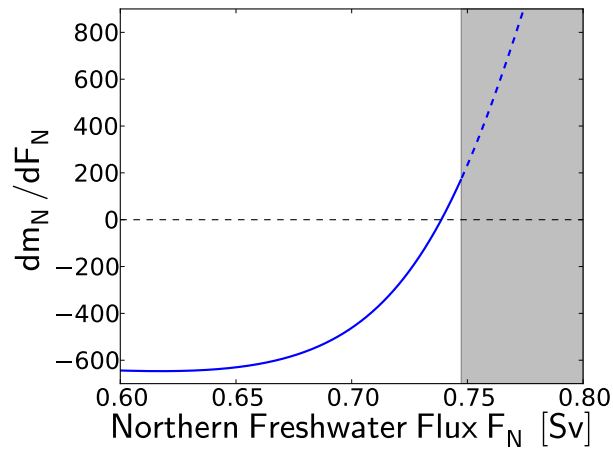


**Figure 4.** In steady state the governing equation for the mixing-driven case has one real, stable solution until a threshold level is reached (a). Thereafter, no real solution exists. The tracer transports are upwelling in the mid latitudes and northern sinking which balance each other ( $m_N = m_U$ ) and decrease under increasing freshwater forcing (b).

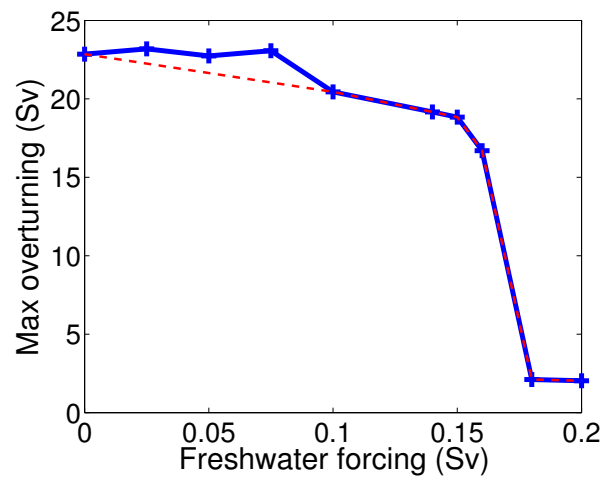




**Figure 5.** In steady state only one physical solution of governing equation for the wind-driven case exists. There are three real solutions before the circulation breaks down (a, white area) because the discriminant is negative (e). The physical branch is solution 2 (red line). The threshold (grey shaded area) is reached when the eddy return flow becomes negative (c, red line) and the discriminant of the governing equation has a negative pole (e). The zero crossing of the discriminant, which was in the parent model (Fürst and Levermann, 2011) the indicator for a cessation of the circulation, does not appear within the range applicability of our model. Within that range the northern sinking always increases (b, red line) and its derivative is positive (d, red line).



**Figure 6.** The derivative of the northern sinking with respect to freshwater forcing in full case. The derivative is positive before the circulation collapses (white area). This behaviour is caused by a change in the Southern Ocean temperature from  $T_S = 7^\circ\text{C}$  to  $T_S = 5^\circ\text{C}$ .



**Figure 7.** Maximum overturning for freshwater experiments with UVic ESCM 2.9. Freshwater was taken out at  $10^\circ\text{S}$  to  $30^\circ\text{S}$  and dumped into the Atlantic at  $10^\circ\text{N}$  to  $30^\circ\text{N}$  prescribing different constant amounts of freshwater. For each simulation the maximum overturning is averaged over the last 1000 years of the simulation (blue curve). Each blue cross corresponds to one equilibrium simulation. If the model would not show an AMOC strengthening, the modeled maximum overturning would be expected to follow the red curve.