



A wavelet-based approach to detect climate change on the coherent and turbulent component of the atmospheric circulation

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Abstract. The modifications of atmospheric circulation induced by anthropogenic effects are difficult to capture because wind fields feature a complex spectrum where the signal of large-scale coherent structures (planetary, baroclinic waves and other long-term oscillations) is mixed up with turbulence. Our purpose is to study the effects of climate changes on these two components separately by applying a wavelet analysis to the 700 hPa wind fields obtained in climate simulations for different forcing scenarios. We study the coherent component of the signal via a correlation analysis to detect the persistence of large-scale or long-lasting structures, whereas we use the theory of autoregressive moving-average stochastic processes to measure the spectral complexity of the turbulent component. Under strong anthropogenic forcing, we detect a significant climate change signal. The analysis suggests that coherent structures will play a dominant role in future climate, whereas turbulent spectra will approach a classical Kolmogorov behaviour.

1 Introduction

Scale separation is an essential property for the study of natural systems: Lagrangian mechanics has been applied to the study of the solar system because planets appear so small that they can be considered to be material points with respect to the length of their orbits (Murray and Dermott, 1999). In a less obvious framework, Einstein and Langevin recognized that the behaviour of heavy particles in a gas can be studied by introducing two different scales: the inertial (slow) motion of the heavy particles and the interactions (fast) with the gas particles (Langevin, 1908). In geophysics the same approach has been – sometimes implicitly – applied for understanding important mechanisms driving the atmospheric and oceanic circulation: one can model the baroclinic instability because cyclones have a well-determined size and their structure emerges from the atmospheric turbulence (Charney, 1947), El Niño, because of the precise timescales involved in the phenomenon (Cane and Zebiak, 1985; Penland and Magorian, 1993). The success of a scale-separation-based

approach is due to the intrinsic properties of stratified and rotating flows. In homogeneous and isotropic turbulence, the energy flows towards the small scales and coherent structures are rapidly destroyed. This is the so-called direct cascade proposed in (Kolmogorov, 1941). By contrast, geophysical flows are stratified and rotational flows, where an inverse cascade of energy induces the bidimensionalization of motions and contributes to the formation of large-scale coherent structures (Pouquet and Marino, 2013). In laboratory experiments (Lamriben et al., 2011) and geophysical observations (Craig and Banner, 1994; Holmes et al., 1998) one aims at separating coherent and turbulent components and build theoretical models to describe the associated motions (Charney, 1971; Pitcher, 1977; Jiang et al., 1995; Lucarini et al., 2007). As pointed out by several authors (see Schertzer and Lovejoy (1991) for a review), this task is non-trivial because both the inverse and direct cascades coexist for geophysical motions. The direct cascade is ultimately responsible for the dissipation of energy, the transfer of momentum from the atmosphere to the ocean and the soil, and the disruption of large-

scale structures in the flow resulting in an unpredictable behaviour (Leith, 1971). The inverse cascade contributes to the formation of cyclonic and anticyclonic structures observed in the atmosphere and the ocean. Moreover, it generally enhances the predictability of future states of the atmosphere (Paladin and Vulpiani, 1994; Tribbia and Baumhefner, 2004).

In this paper we present two indicators that describe the statistical properties of large-scale coherent structures as well as turbulent spectra, investigating their response to climate change. The indicators are defined after separating the coherent structures from featureless turbulence via the wavelet filtering technique. For the coherent part, we compute the integral of the autocorrelation function as a measure of the persistence of the coherent structures. For the turbulent component, we use an indicator that measures the complexity of the spectrum with respect to the canonical behaviour theorized by Kolmogorov.

We test the technique on the horizontal wind data measured at 700 hPa for two different anthropogenic emission scenarios (RCP 2.6 and 8.5). We investigate whether the anthropogenic and natural forcing could cause not only a change in the intensity of some defined observable (as it is now evident for the global mean temperature) but also in the direction the energy is cascading and therefore in the relative importance of large-scale coherent structure with respect to turbulence.

2 Methods

The separation between coherent $X(t)$ and turbulent $Y(t)$ components of a time series $Z(t)$ is done via wavelet filters (Farge, 1992). With respect to a simple filtering technique (e.g. moving-average filters), the wavelet filters are useful when the time series contain multiple timescales and there is no trivial scale separation. Wavelet analysis has been widely applied in climate science (Torrence and Compo, 1998) and to the analysis of geophysical time series (Ghil et al., 2002; Grinsted et al., 2004).

We give a brief illustration of the wavelet filtering technique by analysing a time series of u_{500} taken from the scenario RCP 2.6 at the point 78° W, 38° N. The series consists of 512 monthly observations and it is shown in Fig. 1a. Its power spectral density (psd) is visualized in Fig. 1b. The series shows an evident periodic component (the seasonal cycle) captured by the spectral peak. The spectrum is compared with a flat one (dotted line), reproducing a perfect white-noise signal. The results of the wavelet filter are shown in Fig. 1c–f. The coherent component $X(t)$ and its spectrum are shown in Fig. 1c and d respectively. The effects of the filter are not directly visible on the detrended time series but rather on the spectra. The psd for the coherent part of the signal presents a significant slope with the energy concentrated on large timescales. By contrast, the incoherent component $Y(t)$ represented in Fig. 1e has a rather flat psd (Fig. 1f),

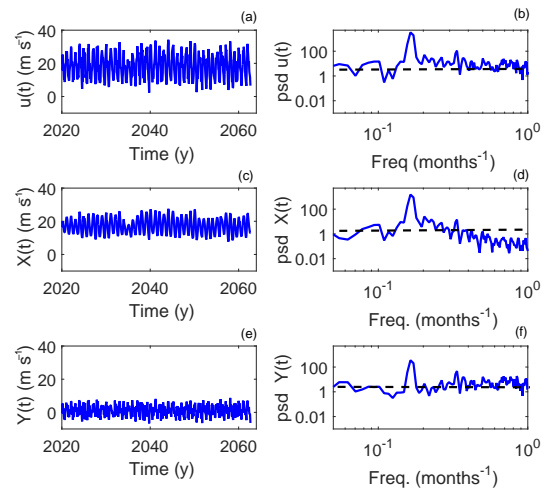


Figure 1. Example of wavelet filtering. (a) u_{500} monthly time series at 78° W, 38° N and (b) corresponding power spectral density (psd). (c) Time series of the coherent component $X(t)$ extracted by the wavelet filter and (d) its psd. (e) Time series of the noisy component $Y(t)$ extracted by the wavelet filter and (f) its psd.

as expected from a successful application of the technique. Nonetheless, the limits of the wavelet filtering approach appear when one looks at the spectral peak corresponding to the seasonal cycle, which cannot be completely eliminated, although it represents a coherent component of the signal.

Once the separation between coherent and noisy component is done, we study the property of $X(t)$ and $Y(t)$ separately. For the coherent component $X(t)$ we use the memory of the system as an indicator of persistence by measuring the integral of the autocorrelation function (ACF) defined as

$$\text{ACF}(X)(\tau) = E[X(t)X^*(\tau)],$$

where $E[X]$ stands for expectation value. The ACF measures how long the system remember an initial condition. For a white-noise signal, it decays to 0 as $\tau > 1$. For a correlated signal it decays slowly to 0 for large τ . For a perfectly periodic signal, the ACF is periodic itself. The integral of the ACF in its discrete version is written as

$$\Lambda = \sum_{\tau=0}^T \text{ACF}(X)(\tau),$$

where we sum the correlation up to a time T sufficiently large for the ACF to decay to 0. Λ measures how long coherent structures persist in time, and it is therefore linked to predictability: the higher the correlation, the higher the probability that the structure will be preserved in future times (Schubert et al., 1992). The link between correlations decay and predictability is well known in dynamical systems theory and in physics (Osborne and Provenzale, 1989; Govindan et al., 1998; Crisanti et al., 1993), and we now exploit it to study properties of geophysical time series.

For the noisy component $Y(t)$, we use an indicator of the spectral complexity with respect to the canonical Kolmogorov behaviour. In order to introduce this indicator we will use the class of autoregressive moving-average (ARMA) stochastic processes. In general, a stationary time series $Y(t)$ of an observable with unknown underlying dynamics can be modelled by an ARMA(p, q) process such that for all t

$$Y_t = \sum_{i=1}^p \phi_i Y(t-i) + \varepsilon(t) + \sum_{j=1}^q \theta_j \varepsilon(t-j), \quad (1)$$

with $\varepsilon(t) \sim \text{WN}(0, \sigma^2)$ – where WN stands for white noise – and the polynomials $\phi(z) = 1 - \phi_1 z(t-1) - \dots - \phi_p z(t-p)$ and $\theta(z) = 1 - \theta_1 z(t-1) - \dots - \theta_q z(t-q)$. Notice that, hereinafter, the noise term $\varepsilon(t)$ will be assumed to be white noise, which is a very general condition (Box and Jenkins, 1970).

The basic model for the noisy component is the ARMA(1,0) or simply AR(1) model, which is the simplest model compatible with the Kolmogorov spectrum (Thomson, 1987). When the spectral complexity increases, the best ARMA model describing the velocity time series will deviate from the basic one. We can define a normalized distance between the reference ARMA(\bar{p}, \bar{q}) and any other ARMA(p, q) by using the Bayesian information criterion (BIC), which measures the relative quality of a statistical model, as

$$\text{BIC} = -2 \ln \hat{L}(n, \hat{\sigma}^2, p, q) + k[\ln(n) + \ln(2\pi)], \quad (2)$$

where $\hat{L}(n, \hat{\sigma}^2, p, q)$ is the likelihood function for the investigated model and in our case $k = p + q$ and n is the length of the sample. The variance $\hat{\sigma}^2$ is computed from the sample and is a series-specific quantity.

Our indicator is a normalized difference between the BIC($n, \hat{\sigma}^2, p + 1, q$) and the ARMA(\bar{p}, \bar{q}) BIC($n, \hat{\sigma}^2, \bar{p}, \bar{q}$):

$$\Upsilon = 1 - \exp\{[\text{BIC}(p + 1, q) - \text{BIC}(\bar{p}, \bar{q})] / n\}, \quad (3)$$

with $0 \leq \Upsilon \leq 1$; it goes to 0 if the dataset is well described by an ARMA(\bar{p}, \bar{q}) model and tends to 1 in the opposite case.

We have checked that such indicators perform well in different physical systems and generally provide more information than the ones based on correlations analysis only. Such results can be found in Faranda et al. (2014), where indicators similar to Υ have been used to model different physical systems: Ising and Langevin models and turbulence. A large Υ corresponds to a complex spectrum with non-trivial scale interactions and non-constant energy transfers; a small Υ corresponds to a spectrum compatible with the Kolmogorov spectrum with constant energy fluxes between scales. The predictability will decrease with a higher Υ because more structures on different scales will have to be taken into account to describe the behaviour of the system. In other words, for high Υ the component $Y(t)$ cannot just be modelled as simple noise.

3 Analysis

We illustrate the potential of Λ and Υ indicators on a climate change experiment used in the CMIP5 framework for the IPCC AR5 report (Collins et al., 2013). To explore climate change in the next century, the IPCC has developed four different scenarios, defined in terms of radiative evolution and corresponding to a concentration of greenhouse gases year by year between 2006 and 2100, extended until 2300. Here we consider two scenarios: (i) the low-emission scenario (RCP 2.6), leading to a radiative balance of 2.6 W m^{-2} in 2100 with a peak at 3 W m^{-2} and a decreasing trend; (ii) the higher-emission scenario (RCP 8.5), predicting an increase up to 8.5 W m^{-2} in 2100. The effect of such greenhouse gas perturbations are well known for some observables, e.g. the global temperature increase ranges from 1 ± 0.4 to 3.7 ± 0.7 °C in the last part of the period 2081–2100 (Collins et al., 2013).

We focus on the daily horizontal winds at 700 hPa (u_{700}, v_{700}) obtained from the IPSLCM5-LR model, where LR stands for low resolution. This model is developed by the Institut Pierre-Simon Laplace with several laboratories. It consists of several components: atmosphere (LMDZ), ocean (NEMO), continent (ORCHIDEE), and sea ice (LIM). For LMDZ and ORCHIDEE, the spatial resolution is $3.75^\circ \times 1.875^\circ$ (longitude \times latitude) with 39 vertical levels. For NEMO, the resolution is of about 2° , with a higher latitudinal resolution of 0.5° in the equatorial ocean and 31 vertical levels. ORCHIDEE takes into account the evolution of the lands (urbanization, forests, agriculture) (Dufresne et al., 2013). We chose 700 hPa (about 3 km) because it has been recognized as the best level for tracking the coherent atmospheric structures as shortwaves, extratropical cyclones, and convective storms, since they are all advected, in first approximation, by 700 hPa horizontal winds (Mölders and Kramm, 2014). We have also performed robustness tests by considering the medium-resolution (MR) version of the IPSLCM5 model ($2.5^\circ \times 1.25^\circ$ in longitude and latitude for LMDZ and ORCHIDEE, while the resolution of other models is the same as LR). These tests are reported and explained in the Supplement.

We begin the analysis by showing typical maps of Λ and Υ for the scenario RCP 2.6 and the two components: the zonal u_{700} and the meridional v_{700} (Fig. 2). Λ shows, for the zonal component, a rich structure with several areas where persistent coherent structures are well identified (Fig. 2a). Because we are using daily time series, the values of Λ can be directly interpreted as the number of days of persistence of these structures. At the midlatitudes, the signature of stationary planetary waves is visible. In correspondence to the location of such waves, we find $\Lambda \sim 16$ days, a value compatible with the work of Torrence and Compo (1998), who studied planetary waves using other indicators based on the wavelet approach. In the tropics, the high values of Λ can be linked to the easterly jets (Koteswaram, 1958). The core of

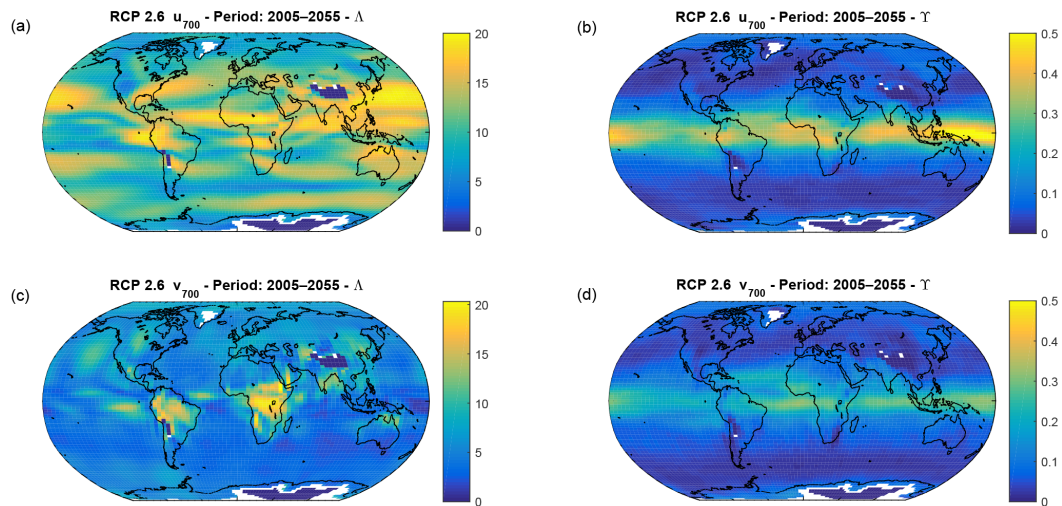


Figure 2. Integral of the autocorrelation function Δ for the period 2005–2055 for the u_{700} (a) and for the v_{700} (c) daily time series. Spectral complexity Υ for the period 2005–2055 for the u_{700} (b) and for the v_{700} (d) daily time series.

the African easterly jet is located at about this level (Nicholson, 2009), as are the Choco and Caribbean low-level jets (Wang, 2007). The results for Δ computed on the meridional component v_{700} are shown in Fig. 2c. Here the largest values are found in correspondence to the regions affected by monsoons. The strongest signal is for the African monsoon because the IPSL model localizes it better than the Indian one (Dufresne et al., 2013). At the midlatitudes the patches visible near the Pacific coast and over the USA correspond to areas where the zonal flow is blocked by the Rocky Mountains and meridional winds blow to allow the flows go round the mountains.

For the Υ analysis, there is not much difference in the structure of the zonal component (Fig. 2b) and the meridional component (Fig. 2d). The spatial pattern of Υ can be explained in light of the tropical atmospheric dynamics. Higher values are located in the tropics, where turbulence is associated with the convective activity in the area. We note that, as the resolution is increased, the $\Delta\Upsilon$ increases (see Fig. 7 in the Supplement). This means that turbulent contribution becomes more relevant when finer scales are included in the analysis, although the scale of the analysis remains, even in the MR simulation, much larger than the scales of convective structures (~ 10 km).

We now investigate whether Δ and Υ can detect changes in the coherent or noisy components of the 700 hPa horizontal winds under the climate change RCP 2.6 and RCP 8.5 scenarios. We divide the daily time series into two periods (2005–2055 and 2055–2105) and compute the quantities $\Delta\Delta = \Delta_{2055-2105} - \Delta_{2005-2055}$ and $\Delta\Upsilon = \Upsilon_{2055-2105} - \Upsilon_{2005-2055}$ (Fig. 3). For both the indicators, the RCP 8.5 scenario shows considerable impacts, whereas the changes for the RCP 2.6 are appreciable only for the u_{700} component. In the Supplement, we report the results also for time windows

of 30 and 40 years. By decreasing the time window considered, we observe that the spatial structure of $\Delta\Delta$ and $\Delta\Upsilon$ does not change (Figs. 1–6 in the Supplement). However, the changes in the indicator become locally sharper as shorter time windows are considered, as one would expect by taking differences of periods with a larger time separation (Fig. 7 in the Supplement).

The $\Delta\Delta$ fields for the u_{700} and the v_{700} components present interesting structures: the strongest signals are located over the Pacific Ocean in correspondence to the El Niño Region 3 (for u_{700}) and Region 3.4 for v_{700} , described in Trenberth (1997). At the midlatitudes, dipolar structures appear both for the zonal and for the meridional flow (Barnston et al., 1997). This is the signature of the jet stream shift observed by several studies. For the Northern Hemisphere, changes in the pattern of meridional winds are highlighted by an alternation of negative and positive $\Delta\Delta$: we can link these changes to the modification in stationary planetary waves associated with the change in the jet stream intensity and positions. Several studies have recently appeared on this issue, although is not clear whether the cause can be linked to the so-called Arctic amplification (Serreze and Francis, 2006) rather than to changes in El Niño–Southern Oscillation (Moritz et al., 2002) or even to the stratospheric dynamics (Serreze and Barry, 2011). $\Delta\Delta$ also suggests that some regions will experience an increase in persistence of meridional winds, i.e. an increasing of blocking conditions (e.g. central USA, western Europe), whereas some other areas will have an increase in the persistence of the zonal winds (e.g. eastern Europe, Alberta (CA)).

The results for $\Delta\Upsilon$ indicate that the spectral complexity in the tropical regions tends to reduce by about 10% ($\Delta\Upsilon \sim -0.1$) in the RCP 8.5 scenario. Although the model does not resolve the convective scales, a possible explana-

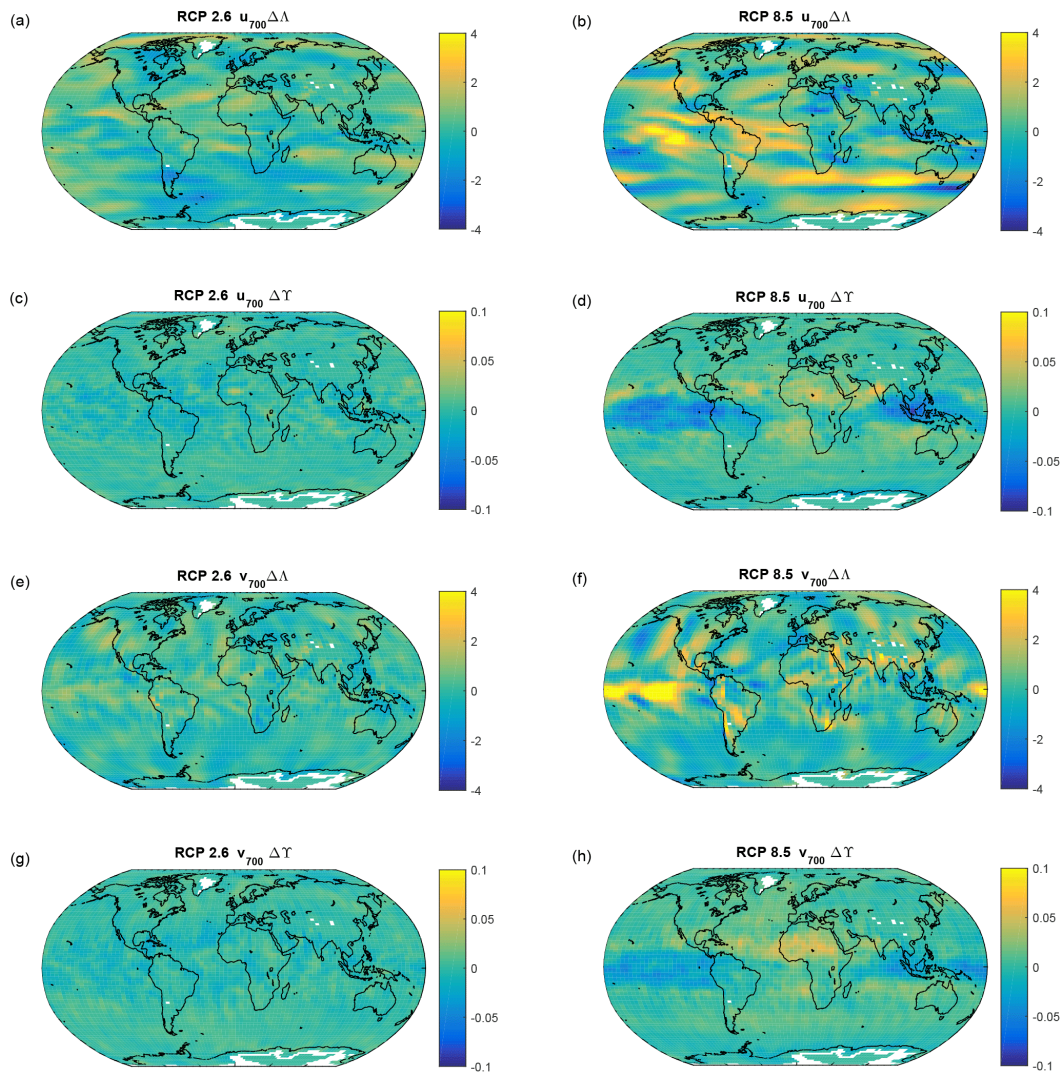


Figure 3. Differences in the integral of the autocorrelation function $\Delta\Lambda$ for the 2055–2105 and the 2005–2055 period for the u_{700} in the RCP 2.6 (a) and in the RCP 8.5 (b). Differences in the spectral complexity $\Delta\Upsilon$ for the 2055–2105 and the 2005–2055 period for the u_{700} in the RCP 2.6 (c) and RCP 8.5 (d) scenario. $\Delta\Lambda$ for v_{700} for the RCP 2.6 (e) and the RCP 8.5 (f) scenarios. $\Delta\Upsilon$ for the v_{700} in the RCP 2.6 (g) and RCP 8.5 (h) scenario.

tion for this result relies on the enhanced convective activity resulting from the sea surface warming and resulting in an increase in precipitation in the area, as we have verified for the IPSL model and as reported by other studies (Huang et al., 2013). This consideration is valid only if convective parametrization transfers energy from the convective scales to the scale of the analysis. In other words, at the actual resolution of climate models, we can only observe the footprints of these phenomena. If turbulence becomes stronger and anisotropic, then it should approach the Kolmogorov behaviour and Υ should tend to 0.

4 Conclusions

We have devised two indicators to study the changes in the atmospheric circulation by separating the coherent structures from the turbulent part of the signals analysed, i.e. the velocity fields at 700 hPa. The indicator $\Delta\Lambda$ is a measure of the total persistence of the coherent structures, whereas $\Delta\Upsilon$ is a measure of the residual complexity of the turbulent spectrum, once the coherent component has been removed.

The indicators show significant changes when the climate system is subject to greenhouse gas forcing. The difference in the indicators for the RCP 8.5 scenario between the second half and the first half of the 21st century suggests that El Niño–Southern Oscillation will play a major role and block-

ing conditions will change the trajectory of coherent structures observed at the midlatitudes.

Besides the regional patterns, we believe that the most important message is contained in the global average of our indicators. For the RCP 8.5 scenario, $\Delta\Lambda$ increases by 0.5 days in the second half of the century for u_{700} and by 0.2 days for v_{700} . On the other hand, the spectral complexity decreases by about 10% in the tropical regions. This suggests that the coherent structures will play a major role in the atmospheric dynamics. This will probably result in an enhanced predictability of the atmosphere on weekly to monthly timescales. The contrast between these two effects could be one of the causes of the difficulty in finding significant traces of climate change in the circulation dynamics, a problem recently highlighted by Shepherd (2014).

Our indicators have been here illustrated for a single model at two different spatial resolutions and in two climate change scenarios. They could be useful to evaluate the response of atmospheric circulation to changes in the forcing for several models. Moreover, the technique does not require the variables to be velocity fields and it could be extended to any physical time series in which a non-trivial scale separation is present.

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