

Supplement: Evaluating Climate Emulation: Fundamental Impulse Testing of Simple Climate Models

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50 **S1 Supplementary Method**

We conduct perturbations of three contrasting chemical species: carbon dioxide (CO₂), methane (CH₄), and black carbon (BC). We begin with CO₂ because this well-mixed greenhouse gas is the largest contributor to anthropogenic forcing changes (Myhre et al., 2013). Methane is also of interest because it is a shorter-lived greenhouse gas, with chemical interactions with itself and other species (Cicerone, R.J.; Oremland, 1988). Finally, we use BC perturbations to represent aerosols more generally because we are interested in model responses to short-lived climate forcings (Bond et al., 2013; Harmsen et al., 2015). SCM representations of other aerosols species are similar so we do not conduct impulse tests of other species.

60 The comprehensive SCMs we use are readily comparable because they read in similar emissions. Background trajectory emissions are taken from the published Representative Concentration Pathway (RCP) 4.5 scenario (Thomson et al., 2011) database, which means that all calculations in the main paper are conducted relative to a changing CO₂ concentration background unless otherwise noted. SCMs are often used to project global mean temperature over various future scenarios, so this is the most relevant type of background on which to test these models. 65 Conducting these experiment with a constant CO₂ background, as previously used in the

literature (Joos et al., 2013), requires inverse modeling of the individual models to produce constant CO₂ concentration emissions files. Our methodology is easier to implement as a regular unit test as it only requires the same emissions inputs with no inverse calculations needed. We
70 provide the input emission files used in this paper.

In many SCMs, forcing over historical periods is explicitly calibrated to a model base year, so it is not possible to conduct perturbations during these time periods. Therefore, our perturbations are conducted in 2015 to avoid the model base years of our SCMs. In the main paper, we show
75 some model responses out to 2300, the end of the MAGICC model runs, equal to 285 years after the perturbation. Additional results are in S8.

We run reference scenarios in the SCMs, followed by each perturbation case described below. For each experiment (see below) we report the response, which is obtained by subtracting the
80 reference from the perturbation results. For instance, the CO₂ concentration response is obtained as follows:

$$CO_2Concentration_{response}(t) = CO_2Concentration_{perturbation}(t) - CO_2Concentration_{reference}(t) \quad (1)$$

85 We conducted the following impulse tests:

a. Concentration impulse (CO₂).

These SCMs can be used in a mode where CO₂ concentrations are exogenously specified. We carry out this experiment by instantaneously increasing CO₂ concentration by 200 ppm in 2015.
90 After 2015, CO₂ concentrations return to the baseline levels following the published RCP4.5 scenario. Note, we do not conduct separate forcing impulse experiments because this is functionally equivalent to a concentration impulse. In this experiment, we are only interested in the dynamics of the models' temperature response. This experiment eliminates the added uncertainty in the emissions to concentrations calculation and complicating factors from carbon
95 cycle feedbacks.

b. Emissions impulse (BC, CH₄, CO₂).

For this experiment all models were run with an emissions input. We carry out this experiment by increasing individual emissions (BC, CH₄, or CO₂) in one year. Following that year, the emissions return to the RCP4.5 pathway for all subsequent years. In this experiment CO₂ and other GHG concentrations are allowed to vary as determined by each model. We find our perturbation values by doubling the 2015 value for each chemical species equal to a 9.2 PgC pulse of CO₂, a 329 Tg pulse of CH₄, and a 7981 Gg pulse of BC. We also perturb CO₂ emissions in 2010, 2020, 2030, 2040, 2050 to understand changes in model responses over time and see a very small difference in the model response (S4). We compare results from three comprehensive SCMs to two IR models, AR5-IR and FAIR model (Millar et al., 2017; Myhre et al., 2013) (S2).

We also compared results to several ESMs and EMICs by carrying out a 100 GtC CO₂ impulse, following Joos et al. (Joos et al., 2013) (S12). This is approximately 10x the CO₂ perturbation pulse described above.

Finally, we conduct a 4xBC emissions step experiment. We compare the SCM temperature responses with the response of a complex climate model used by Sand et al. (2016) (S13).

c. Step increase in CO₂ concentration (instantaneous 4×CO₂ concentration experiment). Similar to comparison (a), in this experiment, CO₂ concentrations are prescribed. We have CO₂ concentrations follow a pre-industrial pathway (278.0516 ppmv in 1765) until 2014. The CO₂ concentration is quadrupled (4x) in 2015 and maintained at this level until 2300. This follows the experimental protocol used in the CMIP5 experimental design (Taylor et al., 2012).

We compare these results to drift-corrected (Gupta et al., 2013) global mean temperature results from 20 complex climate models from the CMIP5 archive. We drift-correct the CMIP5 global mean temperature time series by subtracting the slope of the linear fit from the full-time series of the corresponding pre-industrial experiment for each individual model (see S3).

We ran Hector v2.0 with few changes to the default configuration file settings. We changed two model time steps in Hector v2.0: (1) the carbon-cycle-solver.cpp time step from dt(0.3) to dt(0.1)

and (2) the ocean_component.hpp OCEAN_MIN_Timestep from 0.3 to 0.01 to allow for the
130 carbon cycle, in particular, the ocean carbon cycle to accurately integrate across the sharp
gradient introduced by these experiments. In experiments where we constrained the CO₂
concentration, these changes significantly increase the model run time for this scenario.

Additionally, we used an equilibrium climate sensitivity (ECS) value of 3°C in the SCMs, with
135 the exception of the idealized SCMs, FAIR and AR5-IR (see S2 and Table S10). In both FAIR
and AR5-IR, ECS is derived from the choice of ocean parameters given by,

$$ECS = F_{2x}(q_1 + q_2) \quad (2)$$

140 where F_{2x} is the forcing due to CO₂ doubling ($F_{2x} = 3.74 \text{ Wm}^{-2}$) and both q_1 and q_2 are the
ocean parameters thermal adjustment of the upper ocean and thermal equilibrium of the deep
ocean, respectively (Millar et al. 2017; Equation 4).

We conducted additional sensitivity experiments in the SCMs spanning ranges of climate
145 sensitivity and ocean diffusivity and report the results in S11.

S2 Discussion of Model Specifications

We conduct impulse response tests within three comprehensive SCMs and two idealized SCMs.
The three comprehensive SCMs have structural differences worth noting. Hector v2.0, has explicit
150 ocean carbon chemistry in four boxes, where ocean carbon uptake is a non-linear function of the
solubility of carbon. MAGICC 5.3 BC-OC and 6.0 have differential hemispheric forcing over land
and ocean, thereby calculating temperature over each box. Important characteristics of the carbon
and climate components of each model are shown in Table S1.

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160 **Table S1** Main carbon cycle and climate characteristics of SCMs and IRFs

Model	Model description	Carbon cycle	Climate component
Hector v2.0 (Hartin et al., 2015, 2016; Kriegler, 2005)	mechanistic climate carbon-cycle model	One-pool atmosphere, three-pool land, and four-pool ocean	Global Energy balance model, with ocean heat diffusion
MAGICC 5.3 BC-OC (Raper and Cubasch, 1996; Smith and Bond, 2014; Wigley and Raper, 1992)	mechanistic climate carbon-cycle model	One-pool atmosphere, three-pool land, and one-pool ocean	4-box Energy balance model, with ocean heat upwelling diffusion
MAGICC 6.0 (Meinshausen et al., 2011)	mechanistic climate-carbon cycle model	One-pool atmosphere, three-pool land, and one-pool ocean	4-box Energy balance model, with ocean heat upwelling diffusion
AR5-IR (Myhre et al., 2013)	Impulse-response function	Impulse-response function	Equilibrium temperature as a function of RF
FAIR v1.0 (Millar et al., 2017)	Impulse-response function	Four timescale impulse-response function with state-dependence of the CO ₂ airborne fraction	Equilibrium temperature as a function of RF; IRF with two timescales

Some SCMs also include representations of aerosol dynamics, though the model representations differ. As mentioned in the main paper, unlike Hector v2.0, both versions of MAGICC have differential hemispheric forcing over land and ocean. AR5-IR represents BC forcing response as a simple exponential, similar to the response from greenhouse gas forcing. FAIR v1.0, used here, represents the relationship between CO₂-only emissions, concentrations, and temperature. Other versions of FAIR include non-CO₂ forcing, such as BC.

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S2.1 Model Settings

Here we discuss the model settings used in our experiments, noting any changes made to the default settings. All model parameters and input files are provided in the Supplementary Materials.

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The three comprehensive SCMs were run with the same ECS values ($ECS = 3^{\circ}C$), unless otherwise noted, whereas the ECS in FAIR and AR5-IR depends on the respective model parameters noted in S1 above (see Eq. 2).

180

We also acknowledge that vertical ocean diffusivity has a large impact on ocean heat uptake and we do note that the SCMs we compare in our paper either do not have the same definitions of vertical ocean diffusivity, as is the case for the comprehensive SCMs, or ocean diffusivity is not directly represented in the models, as is the case for idealized SCMs. For our purposes, therefore, we kept the ocean diffusivity values at their default values within the comprehensive SCMs. Sensitivity experiments exploring the model response to the range of these two parameters derived from MAGICC 6.0 are available in S11.

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S2.2 AR5-IR

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The IPCC AR5 (Myhre et al. 2013; See caption under Figure 8.28) describes the underlying multi-gas impulse response model used to quantify the multi-gas equivalence metric, Absolute Global Temperature Potential (AGTP), to compare temperature changes at a chosen time in response to a unit pulse of emissions i . We refer to this model as AR5-IR and describe below how the sums of exponentials are used to find AGTP and the subsequent temperature response.

195

AGTP is found via a convolution of the fraction of the species i remaining in the atmosphere after an emissions pulse and the climate response to a unit forcing,

$$R_T(t) = \sum_{j=1}^M \frac{c_j}{d_j} \exp\left(-\frac{t}{d_j}\right) \quad (3; \text{ See Equation 8.SM.13}).$$

200
$$AGTP_i(H) = \int_0^H RF_i(t)R_T(H-t)dt \quad (4; \text{ See 8.SM.14})$$

and $RF_i(t) = A_i R_i(t)$ (5; See Equation 8.SM.7)

where for most species $R_i(t) = \exp\left(-\frac{t}{\tau_i}\right)$ (6; See Equation 8.SM.8)

and for CO₂ $R_{CO_2}(t) = a_0 + \sum_{i=1}^N a_i \exp\left(-\frac{t}{\tau_i}\right)$ (7; See Equation 8.SM.10)

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and A_i is the radiative efficiency yielding, the general equation:

$$AGTP_i(H) = A_i \sum_{j=1}^2 \frac{\tau c_j}{\tau - d_j} \left(\exp\left(\frac{-H}{\tau}\right) - \exp\left(\frac{-H}{d_j}\right) \right) \quad (8; \text{ See Equation 8.SM.14})$$

210 AGTP can then be used to calculate global mean temperature change from any given emission scenario using,

$$\Delta T = \sum \int_0^t E_i(s)AGTP_i(t-s)ds \quad (9; \text{ See Equation 8.1})$$

215 where E_i are the emissions of a species, t is the time horizon, and s is the time of emissions (Myhre et al. 2013; See 8.7.13 and Equation 8.1). For this paper, AR5-IR was recoded in R and is available for download with the Supplementaty Materials. Additoinally, a brief discussion of the parameter choices for this model is available in S2.4.

220 **S2.3 FAIR**

The FAIR v1.0 model is a modified version of the AR5-IR carbon cycle component to include the state-dependence of the CO₂ airborne fraction to reproduce the relationship between CO₂-only emissions, concentrations, and temperature over the historical period. Millar et al. (2017)

225 began with the impulse response functions used for calculation of multi-gas equivalence metrics
in IPCC-AR5 (Myhre et al., 2013) and extended the CO₂ IRF by coupling the carbon-cycle to the
thermal response and to cumulative carbon uptake by terrestrial and marine sinks. FAIR is
available for download at <https://github.com/OMS-NetZero/FAIR>.

230 FAIR calculates the global mean temperature response as the sum of the temperature response
from the fast and slow timescale components, which represent the upper and deep ocean. The
model does not report the internally-calculated forcing response, so this is not included in Figure
2 in the main paper.

235 Here, we use the first iteration of FAIR, but we note that two new versions have recently been
published, FAIR v1.1 and FAIR v1.3. FAIR v1.3 extends the original version to, “calculate non-
CO₂ greenhouse gas concentrations from emissions, aerosol forcing from aerosol precursor
emissions, tropospheric and stratospheric ozone forcing from the emissions of precursors, and
forcings from black carbon on snow, stratospheric methane oxidation to water vapour, contrails
240 and land use change (Smith et al., 2018).”

Additoinally, a brief discussion of the parameter choices for this model is available in S2.4.

245 **S2.4 FAIR (without carbon cycle) versus AR5-IR**

We expect slight differences in the response of FAIR and AR5-IR to a unit forcing. According to
Equation 8 in Millar et al. (2017), FAIR will have a differential response to changing
background CO₂ concentrations. By contrast, AR5-IR parameterizes the climate response to a
unit forcing, R_T , using a sum of exponentials as given by Equation 8.SM.13 in Myhre et al.
250 (2013):

$$R_T(t) = \sum_j \frac{q_j}{d_j} e^{\frac{-t}{d_j}} \quad (10; \text{ See Equation 8.SM.13})$$

Values of the R_T input parameters, q_j and d_j , are available in Table S2 of this response, where
 255 $j=1,2$ represent the timescales of the fast and slow ocean response. We note all parameters are
 independent of background concentration in AR5.

In the main paper, we used the time constant parameters representing the thermal equilibrium of
 the deep ocean (d_2) and the thermal adjustment of the upper ocean (d_1) from Myhre et al.
 260 (2013), rather than from Millar et al. (2017). We are testing the model responses as they would
 be ‘out of the box’ and only make modifications if required for the models to run, as was the case
 for Hector v1.1 to handle a $4xCO_2$ concentration step.

Here we included additional model responses from the AR5-IR model using parameters from
 265 Millar et al. (2017). The parameter choices are available below in Table S2.

Table S2 Parameter values for the simple impulse-response model, AR5-IR

Parameter (Units)	Value – AR5-IR (from Myhre et al., 2013)	Value – AR5-IR- var (from Millar et al., 2017)	Guiding analogues
α (Wm^{-2})	5.35	5.395 ($\alpha = F2x/\ln(2)$; $F2x=3.74$)	CO ₂ RF scaling parameter
q_1 ($KW^{-1}m^2$)	0.631	0.41	Thermal adjustment of the upper ocean
q_2 ($KW^{-1}m^2$)	0.429	0.33	Thermal equilibrium of the deep ocean
d_1 (year)	8.4	4.1	Thermal adjustment timescale of the upper ocean
d_2 (year)	409.5	239.0	Thermal equilibrium timescale of the deep ocean

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Figure S1 shows the temperature response from a CO₂ concentration impulse and Figure S2 shows the temperature response from a CO₂ concentration step in several SCMs, including the AR5-IR response found using the Millar et al. (2017) time constants, which we refer to as “AR5-IR-Millar-parameters” in this figure. We note that the AR5-IR-parameters response is still not identical to FAIR because FAIR has a differential response to changing background CO₂ concentrations.

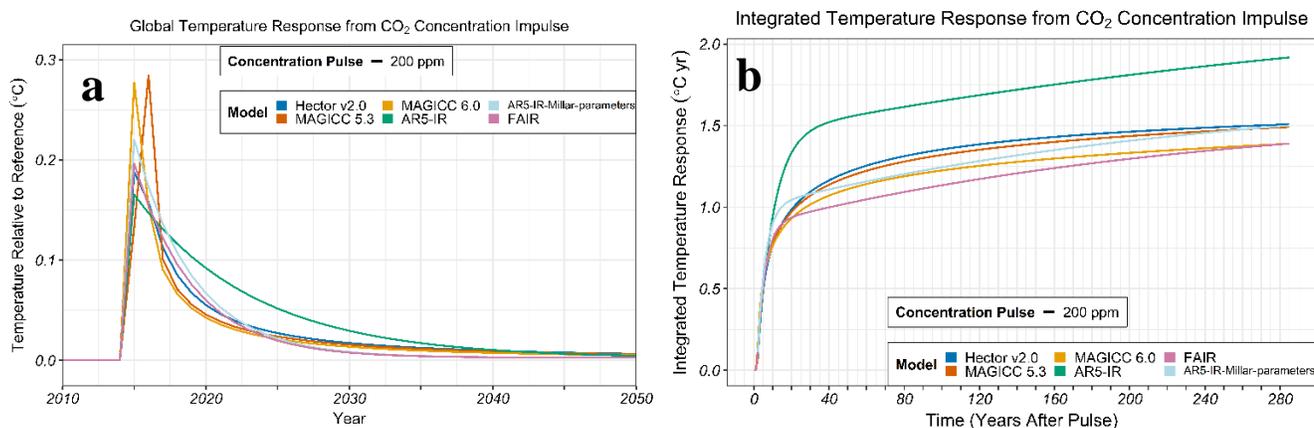


Figure S1 Global mean temperature response (a) and integrated global mean temperature response (b) from a CO₂ concentration perturbation in SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR – pink, AR5-IR-Millar-parameters – light blue). The time-integrated response, analogous to the Absolute Global Temperature Potential, is reported as 0-285 years after the perturbation.

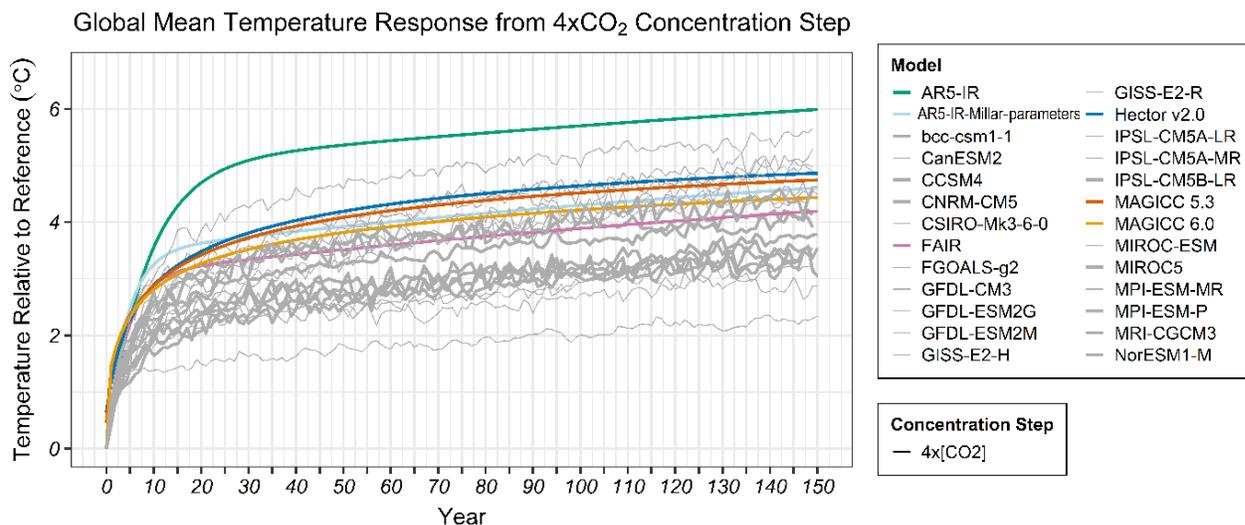


Figure S2 Global mean temperature response from 4xCO₂ concentration step in CMIP5 models (grey) and SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, FAIR – pink, AR5-IR – green, AR5-IR-Millar-parameters – light blue). A climate sensitivity value of 3°C was used in the SCMs and the thick lines represent CMIP5 models with an ECS between 2.5 - 3.5 °C.

We note that, while the Millar et al. (2017) parameters in Table S2 may provide a better short-term fit, they underestimate the long-term response of the ocean. The long-term ocean thermal time scale, which can only be estimated using multi-century model runs, is known to be longer than 200 years from basic physical principles (as seen in the original literature cited by the AR5 model, which used longer model runs to inform those parameters). While this may be an acceptable tradeoff if this model is only going to be used over a 100-year timescale, this will inevitably lead to bias on longer time-scales. The simple climate models tested in this study are used for a variety of purposes and over a range of time-scales. This illustrates why we use the original parameters of the models as set by their designers.

S2.4 MAGICC 5.3 BC-OC

MAGICC 5.3 BC-OC is a version of MAGICC 5.3 developed in conjunction with the Global Change Assessment Model (GCAM). MAGICC 5.3 used here is available in GCAM version 4.4, available for download at <https://github.com/JGCRI/gcam-core/releases>. The major change in this version of MAGICC was the addition of explicit BC and OC (Smith and Bond, 2014). To enable MAGICC 5.3 within GCAM, the climate model must be set to <Value name = "climate">../input/climate/magicc.xml</Value> within the configuration file. We ran this model with all its default configuration settings unless otherwise noted in the text. We reiterate that all model parameters and input files are provided in the Supplementary Materials.

S2.5 MAGICC 6.0

MAGICC 6.0 was run with all the default settings. For the main experiments, the climate sensitivity was set to 3.0°C to match the default setting of MAGICC 5.3 BC-OC and Hector v2.0, unless otherwise noted. The MAGICC 6.0 executable is available for free download here: <http://www.magicc.org/>. We reiterate that all model parameters and input files are provided in the Supplementary Materials.

S2.6 Hector v2.0 Settings

In the version we use here, Hector (v2.0), is coupled to a 1-D diffusive heat and energy balance model (DOECLIM: Diffusion Ocean Energy balance CLIMate model). We are using the 1-D diffusive ocean heat component of DOECLIM. DOECLIM is well documented and has been widely used in climate uncertainty studies (Bakker et al., 2017; Kriegler, 2005; Urban et al., 2014). Using default Hector parameter values for climate sensitivity and heat diffusivity, we find that the new coupled model (Hector v2.0) exhibits improved vertical ocean structure and heat uptake, as well as surface temperature response to radiative forcing, compared to earlier versions of Hector. We reiterate that all model parameters and input files are provided in the Supplementary Materials.

S3 CMIP5 Model Data

The CMIP5 model data used to produce Figure 4 is described here. Raw climate model output from 20 models was obtained from the CMIP5 data archive (http://cmip-pcmdi.llnl.gov/cmip5/data_portal.html) and the World Data Center for Climate site (<http://cera-www.dkrz.de/WDCC/ui/Index.jsp>). The monthly temperature data is aggregated to the global annual mean level using code developed using CDOs (see CDO 2018: Climate Data Operators. Available at <http://www.mpimet.mpg.de/cdo>). The long-term drift is removed from the CMIP5 model data by subtracting the linear trend from the corresponding pre-industrial control run (Gupta et al., 2013). Table S3 provides the CMIP5 modeling centre name and the model name from Figure 4.

Table S3 CMIP5 and SCM model information

Centre(s)	Model name
Beijing Climate Center (BCC) China	BCC-CSM1.1
Canadian Centre for Climate Modelling and Analysis (CCCma) Canada	CanESM2
National Center for Atmospheric Research USA	CCSM4

Centre National de Recherches Météorologiques, Centre Européen de Recherche et de Formation Avancée en Calcul Scientifique (CNRM-CERFACS) France	CNRM-CM5
Commonwealth Scientific and Industrial Research Organization/Queensland Climate Change Centre of Excellence Australia	CSIRO-Mk3-6-0
Institute of Atmospheric Physics, Chinese Academy of Sciences (LASG-CESS) China	FGOALS-g2
Geophysical Fluid Dynamics Laboratory (NCAR; NSF-DOE-NCAR) USA	GFDL-CM3
	GFDL-ESM2G
	GFDL-ESM2M
NASA/GISS (Goddard Institute for Space Studies; NASA-GISS) USA	GISS-E2-H
	GISS-E2-R
Institut Pierre Simon Laplace (IPSL) France	IPSL-CM5A-LR
	IPSL-CM5A-MR
	IPSL-CM5B-LR
Atmosphere and Ocean Research Institute (The University of Tokyo), National Institute for Environmental Studies, and Japan Agency for Marine-Earth Science and Technology (MIROC) Japan	MIROC-ESM
	MIROC5
Max Planck Institute for Meteorology (MPI-M) Germany	MPI-ESM-MR
	MPI-ESM-P
Meteorological Research Institute Japan	MRI-CGCM3
Norwegian Meteorological Institute Norway	NorESM1-M

S3.1 Abrupt 4xCO₂ concentration step response from Geoffroy et al. (2013)

340 Conducting impulse tests with complex models is computationally expensive, illustrated by the few studies employing this technique to understand the responses of models. We cite the Sand et

al. (2016) study that specifically investigated NorESM's response to black carbon (BC) perturbations (Sand et al., 2016). Another study by Yang et al. (2019) conducted similar BC perturbations in CESM (Yang et al., 2019). Other stylized CMIP5 experiments, such as the 1% CO₂ concentration experiment, are not included in our comparison because we do not consider them to be impulse response tests. It is not possible to cleanly extract the impulse response from the 1% experiments. The CMIP5 4xCO₂ concentration step experiment is mathematically related to impulse responses, so are a reasonable comparison, particularly because these are the largest suite of such tests conducted in complex models, which is the reason we highlight these results in the paper.

Geoffroy et al. (2013) reported the 4xCO₂ concentration step temperature change relative to the 150-year temperature mean from the corresponding pre-industrial control run. For comparison to the simple models, we report the drift corrected 4xCO₂ concentration step temperature change relative to the start of the 4xCO₂ concentration run. Therefore, there will be a difference in the temperature reported.

Figure S3 shows the global mean temperature response from the 4xCO₂ concentration step experiment for the 20 CMIP5 models used in our comparison following the Geoffroy et al. (2013) procedure of reporting the 4xCO₂ concentration step temperature change relative to the 150-year temperature mean from the corresponding pre-industrial control run. The responses reported in Figure S3 are consistent with Geoffroy et al. (2013).

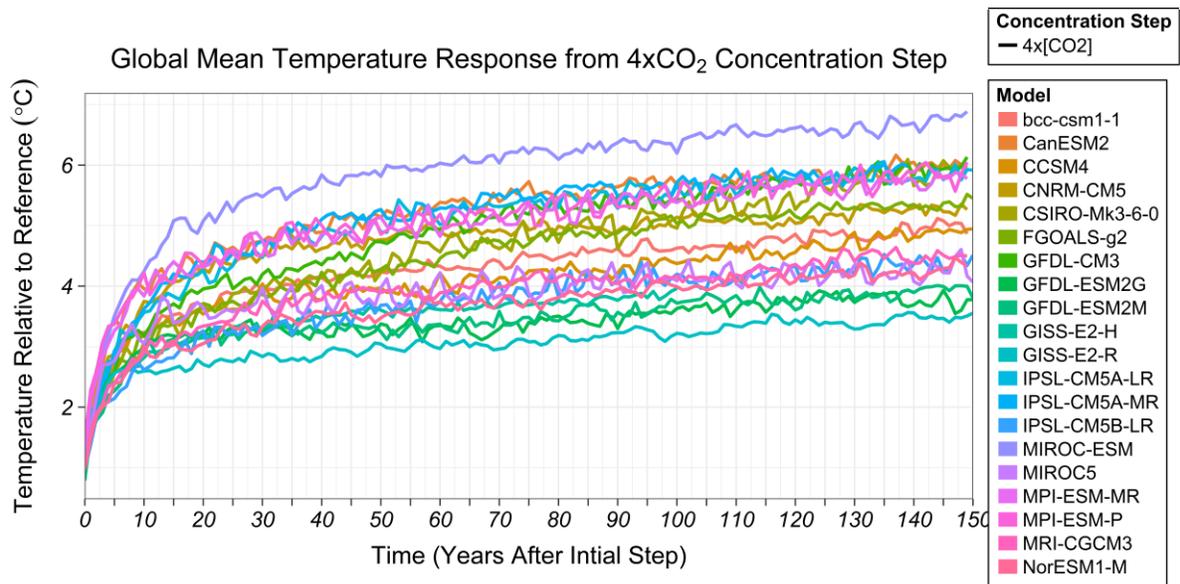


Figure S3 Global mean temperature response from $4xCO_2$ concentration step in CMIP5 models following the Geoffroy et al. methodology.

365 **S4 Sensitivity Experiments in MAGICC 5.3**

We conduct two sensitivity experiments to illustrate there is little impact of these choices on the model responses: (1) perturb CO_2 emissions in different years and (2) perturb CO_2 emissions at different levels in 2015.

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S4.1 Impact of Changes to the Years of Emission Impulses

We test CO_2 emissions perturbations in different years from the default 2015 used in the main text. Figure S4 shows the global mean temperature response normalized by the 2010 global mean temperature response from a CO_2 emissions pulse in MAGICC 5.3. We found a maximum of $0.028^\circ C/PgC$ difference in the response in MAGICC 5.3 and, therefore, carried out the remainder of the experiment in 2015, avoiding model base years.

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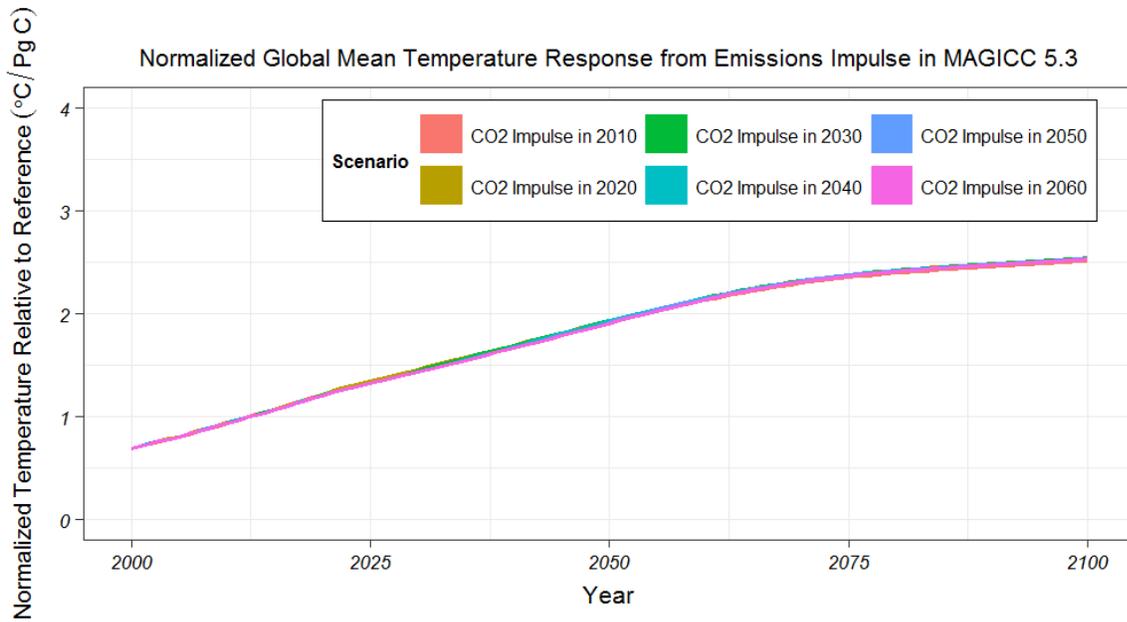


Figure S4 Normalized global mean temperature response from CO₂ emissions impulses in MAGICC 5.3 carried out in different years.

S4.2 Impact of Emissions Pulses Size on Temperature Response

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In the main text, we carried out annual emissions perturbations equivalent to doubling the value in 2015 to avoid model base years. Figure S5 shows the global mean temperature response normalized by the perturbation size for different CO₂ perturbation sizes in 2015 in MAGICC 5.3. We found there was a maximum difference of 0.0015°C/PgC, and thus we continued our

400

experiments using only one perturbation value.

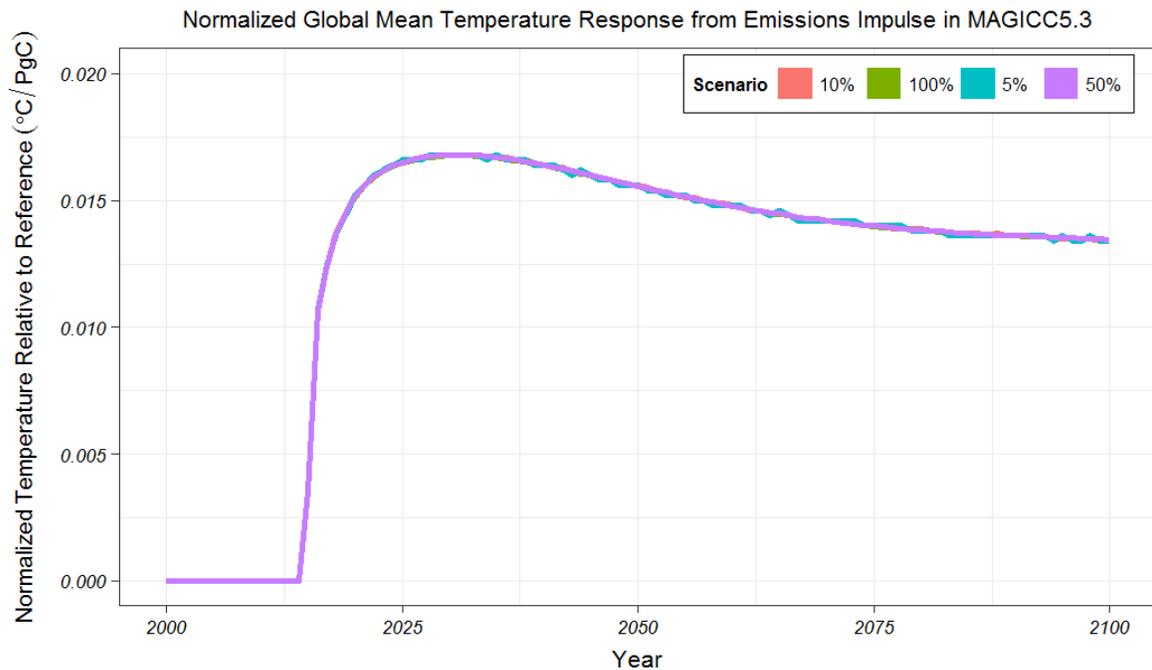
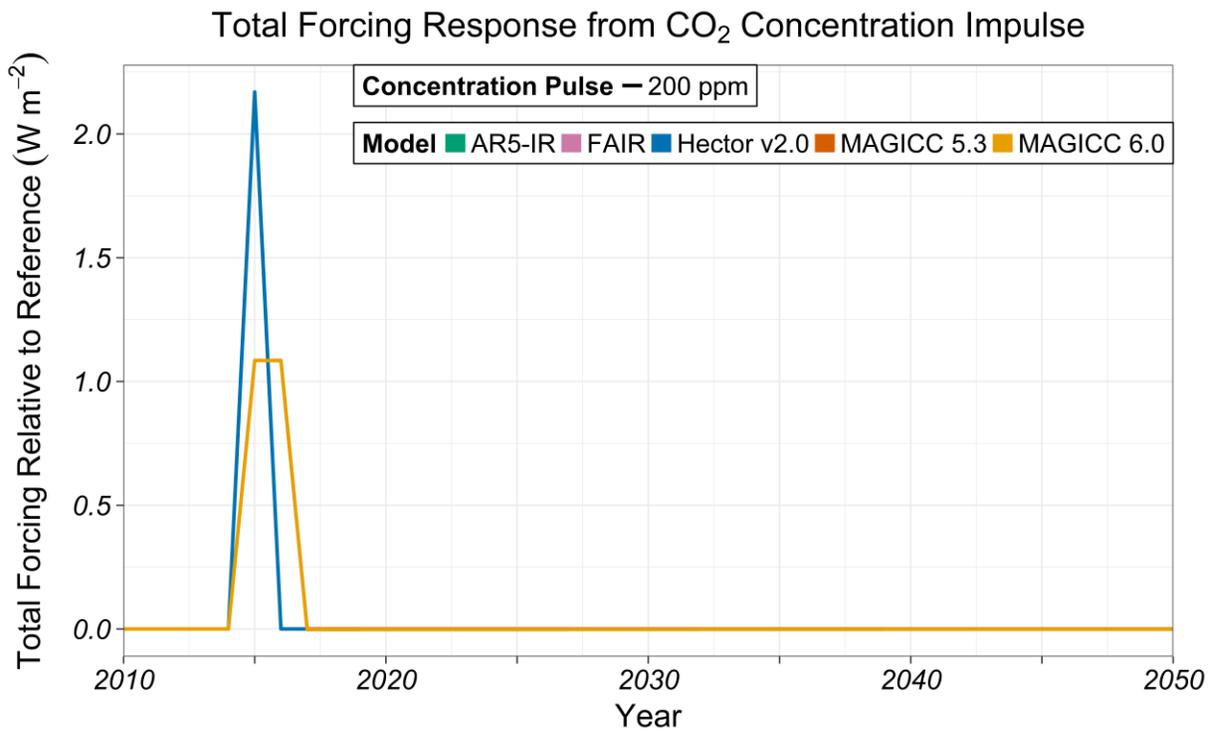


Figure S5 Normalized global mean temperature response from different sized CO₂ emissions impulses in MAGICC 5.3 in 2015.

S5 Adjusted Total Forcing Response

We found that MAGICC 5.3, MAGICC 6.0, and Hector v2.0 respond similarly to a CO₂ concentration impulse, with differences in the forcing and temperature responses arising from the treatment of time within each model. Hector v2.0, for example, reads in annual average emissions and carries out calculations using that same classification of time. MAGICC 5.3 and MAGICC 6.0 read in annual emissions and interpolate to obtain mid-year and end-of-year values and uses those internally to calculate concentration, forcing, and temperature at mid-year values, and successively reports temperature at the end-of-year. This change in the timing affects the impulse response by distributing the pulse over more time periods. Here, we demonstrate the impact of the adjustment for the forcing response to a CO₂ concentration impulse.



415 **Figure S6** Total forcing response from a CO₂ concentration impulse in SCMs. Three comprehensive SCMs have a collinear response (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue). The responses are collinear past 2016.

Due to the differences in model treatment of time, we offer a correction to the forcing in two of the SCMs. MAGICC 5.3 and MAGICC 6.0 calculate forcing in mid-year, while Hector v2.0 reports forcing at the end of a year. The result is a broadened impulse response peak in both versions of MAGICC, compared to Hector v2.0. The total forcing response from both version of MAGICC, however, can be adjusted with the following equation:

$$F_i = (2xf_i) - f_{i-1} \tag{11}$$

425

where F_i is the adjusted forcing, f_i is the unadjusted forcing at the current time step, and f_{i-1} is the unadjusted forcing at the previous time step.

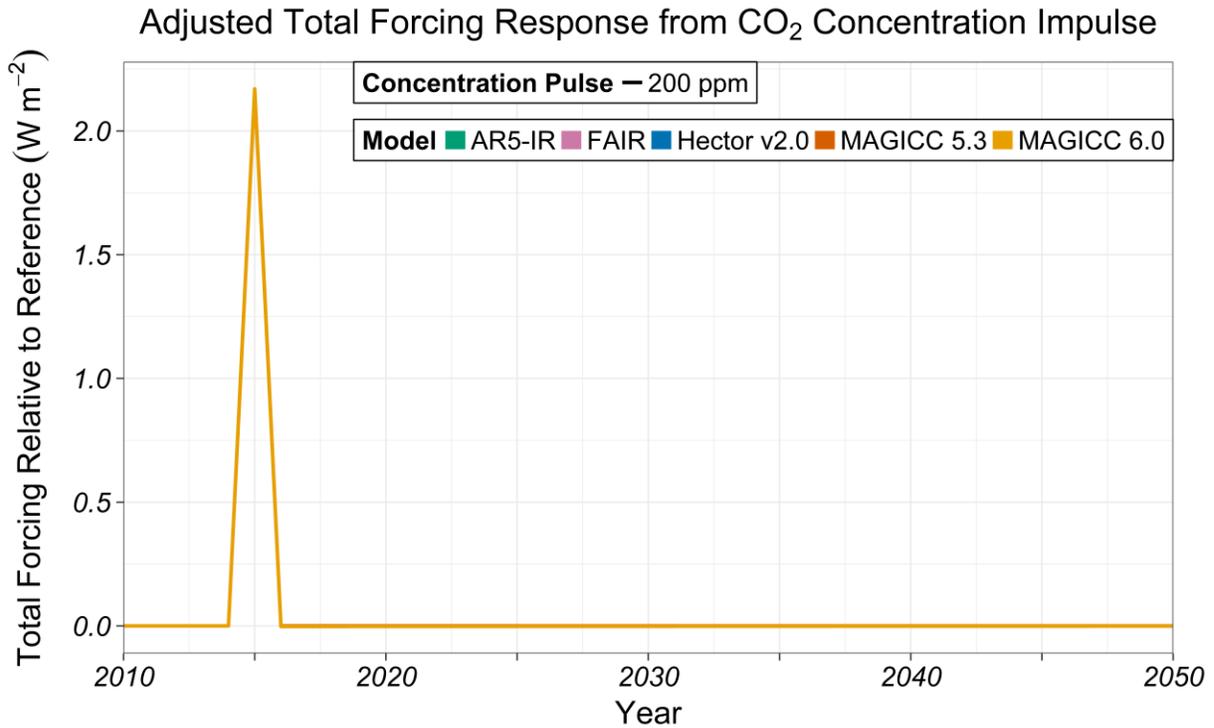


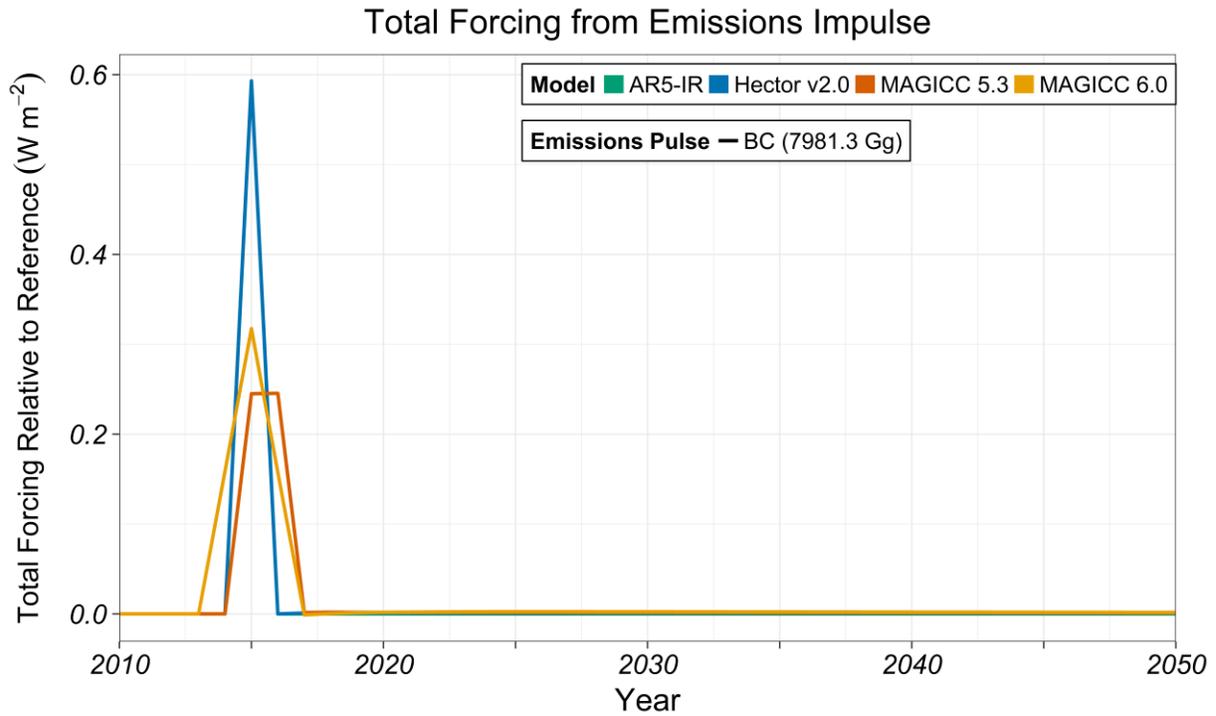
Figure S7 Total forcing response from a CO₂ concentration impulse in SCMs. All three SCMs have a collinear response (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR –pink).

430 Figure S7 shows the total forcing response adjusted from mid-year reporting to end-year reporting using equation (Eqn. S11). We can also apply this adjustment to the BC impulse, however, the MAGICC 6.0 distribution is larger in this case because MAGICC 6.0 annual emissions are interpolated to produce end-of-year and intermediate values. An annual emissions pulse is effectively spread over two model years. In the main paper, we report the integrated response because over these periods, the timing of the internal model calculations has minimal impact on the model results. Additional integrated model responses are in S9.

435

S6 Total Forcing Response from BC Emissions Impulse

440 We see in Figure S8 that the model responses to a pulse of BC have similar patterns of instantaneous behavior seen in Figure 1 from the CO₂ concentration pulse. In general, the models behave similarly in response to a BC pulse; Hector v2.0 and AR5-IR have a collinear response, while MAGICC 6.0 distributes the BC emissions pulse over 3 years.



445 **Figure S8** Total forcing response from a BC emissions perturbation in SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR-green). AR5-IR and Hector v2.0 are collinear.

S7 CO₂ Concentration Responses from Emissions Impulses

450 Figure S9 shows the CO₂ concentration responses from a BC and CH₄ emissions pulse. Every
model response shows an eventual CO₂ concentration increases from a BC impulse; a feedback
from the temp increase impact on the carbon cycle. From a CH₄ and BC emissions pulse, the
CO₂ concentration response is stronger in MAGICC 6.0, followed by MAGICC 5.3 and Hector
v2.0. MAGICC 6.0, however, shows an initial decrease in CO₂ concentration response from the
455 BC pulse.

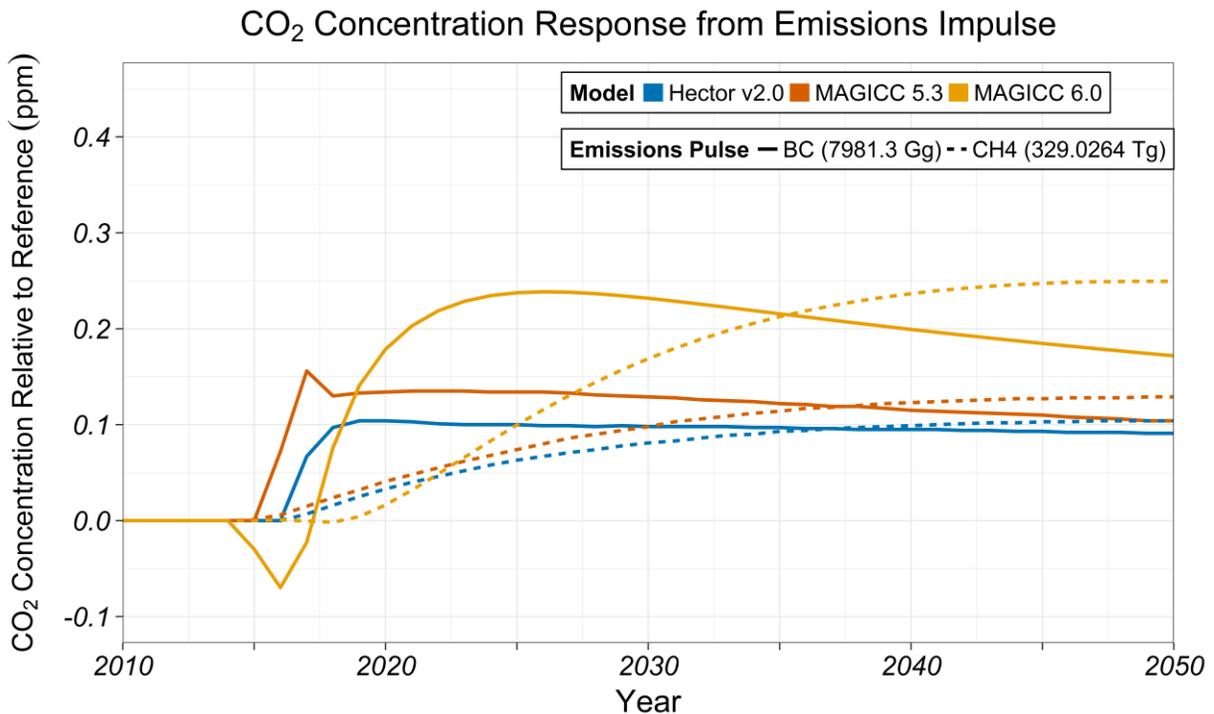


Figure S9 CO₂ concentration response from CH₄ and BC emissions perturbation (B) in SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue) illustrating the carbon-cycle feedbacks present in each model.

460

Figure S9 also shows that CH₄ emission perturbations impact CO₂ concentration within both versions of MAGICC. The discrepancy between the MAGICC and Hector responses is partly due to CH₄ oxidation in MAGICC 5.3. The MAGICC 6.0 response is larger in Figure S9 presumably due to feedback effects in the model, however, the general shape of the response is similar to the other two SCMs.

AR5-IR is notably absent from Figure S9 because, in this IRF model, the CO₂ concentrations are not affected by changing temperature (Millar et al., 2017). Rising temps in general and including temp changes due to CH₄ and BC emissions perturbations. FAIR v1.0 model (Millar et al., 2017) is absent from Figure S9 because the model does not report out the internally-calculated forcing response. The CO₂ concentration response to a CO₂ emissions impulse in FAIR can be seen in Figure S11.

The CH₄ chemistry components in Hector v2.0 and MAGICC 5.3 BC-OC are nearly identical, accounting for the similarities between these two SCMs responses (Hartin et al., 2015). MAGICC 5.3, however, includes CH₄ oxidation to CO₂, which might account for this response difference. To test this, Figure S10 shows the CO₂ concentration response from emissions impulse in SCMs. MAGICC 5.3 is shown with and without CH₄ oxidation included for a clearer comparison of the Hector v2.0 response. With the CH₄ oxidation turned off, the MAGICC 5.3 BC-OC response is similar to Hector v2.0 with only a slight difference after 2025.

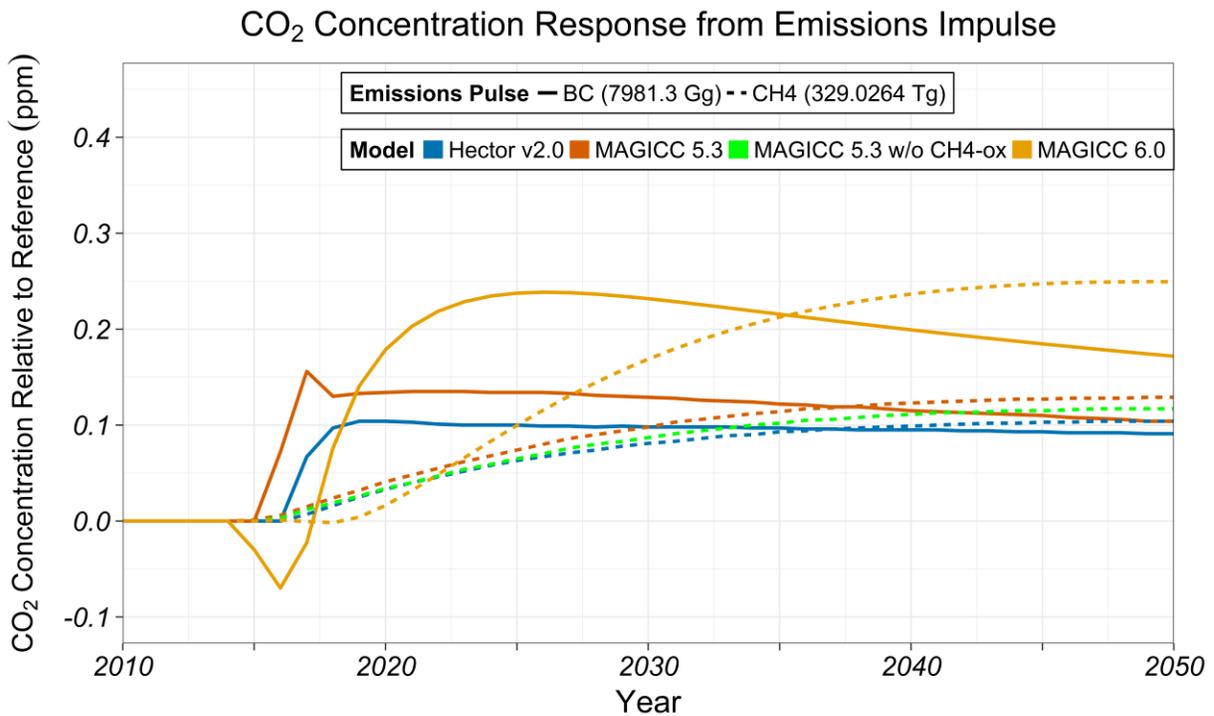


Figure S10 CO₂ concentration response from emissions impulse in SCMs. MAGICC 5.3 is shown with and without CH₄ oxidation included (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue)..

S8 Model Responses out to 2300

485

Figure S11 - Figure S15 show the CO₂ concentration response, total forcing response, and global mean temperature response from an emissions impulse, respectively, to the end of the model period equal to 2300.

490 S8.1 CO₂ Concentration Response to a CO₂ Emissions Pulse

Figure S11 shows the CO₂ concentration response from a CO₂ emissions pulse in the SCMs out to 2300. We see that the SCMs respond similarly to this perturbation, with the exception of the idealized SCM, FAIR, which has a weaker response.

495

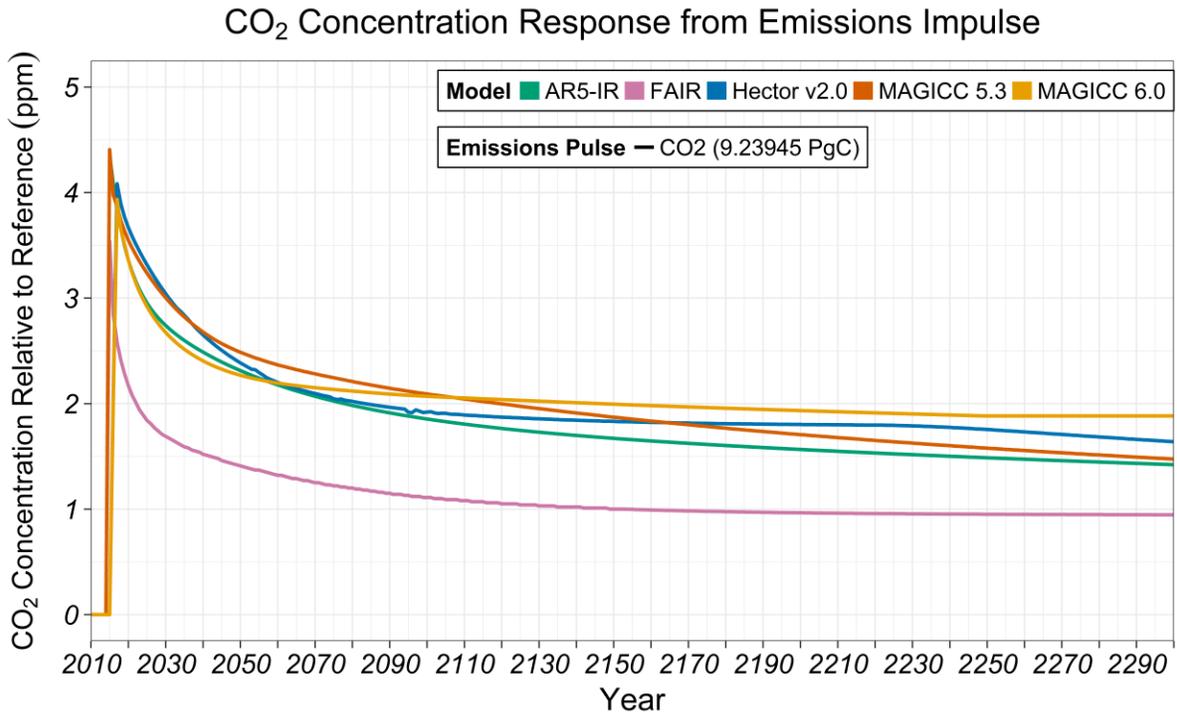


Figure S11 Carbon dioxide concentration response from a CO₂ emissions pulse in SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR - pink).

500 **S8.2 CH₄ Concentration Response from CH₄ Emissions Pulse**

Figure S12 shows the CH₄ concentration response from a CH₄ emissions pulse in the comprehensive SCMs out to 2300. The idealized SCMs do not report CH₄ concentrations. We see that the comprehensive SCMs behave similarly in their response to this perturbation, especially after 2050 when the response tends towards 0 ppb.

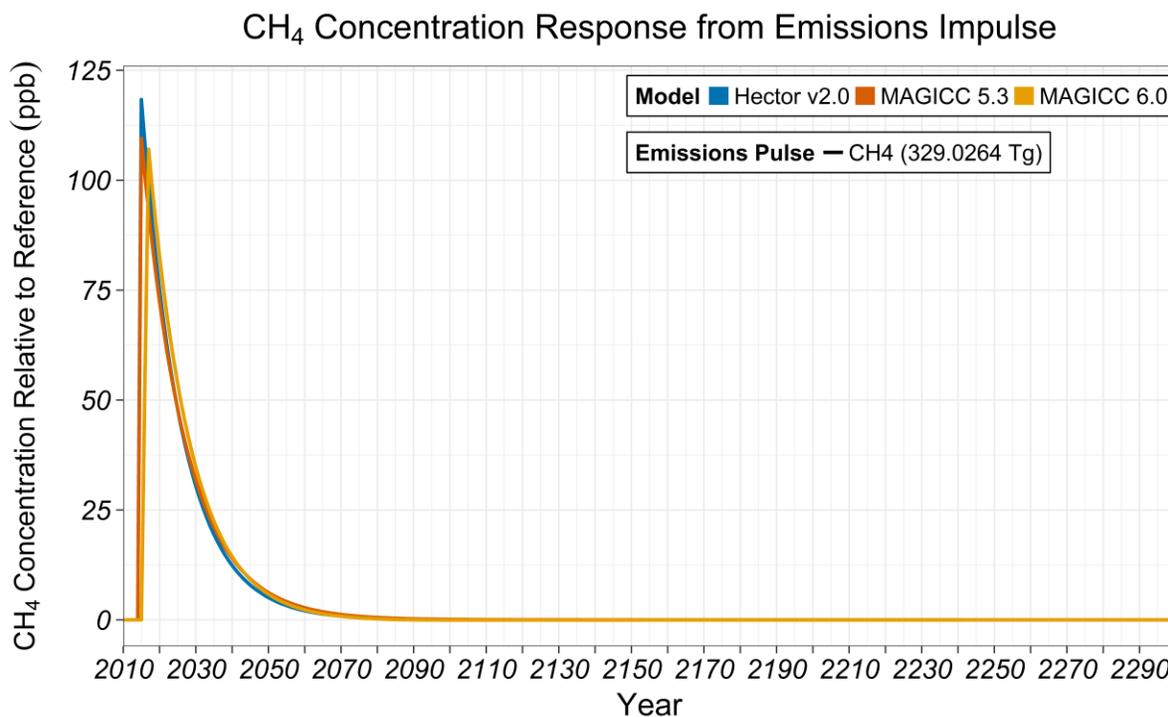


Figure S12 Methane concentration response from a CH₄ emissions pulse in SCMs out to 2300 (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue).

510

S8.3 CO₂ Concentration Response to a BC or CH₄ Emissions Pulse

Figure S13 shows the CO₂ concentration response from a CH₄ and BC emissions perturbations in the SCMs out to 2300. We see that the SCMs behave differently across the entire time series.

515 Hector v2.0 appears to change state after 2225.

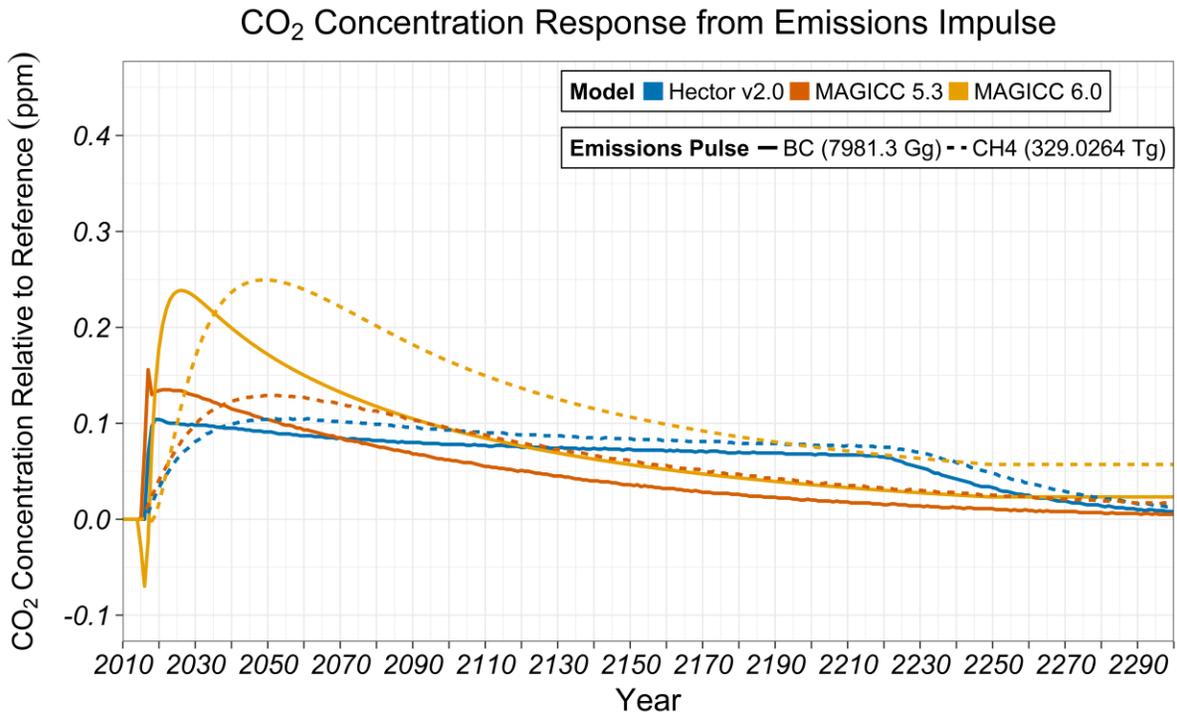


Figure S13 CO₂ concentration response from emissions perturbations in SCMs out to 2300 (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue).

520 **S8.4 Total Forcing Response to a CO₂ or CH₄ Emissions Pulse**

We report the total forcing response from the models, rather than the individual species' forcing responses for comparability. Additionally, the total forcing is similar to the individual forcing responses because forcing is dominated by the forcing from the perturbed species.

525 Figure S14 shows the total forcing response from a CH₄ and CO₂ emissions perturbations in the SCMs out to 2300. FAIR does not report total forcing.

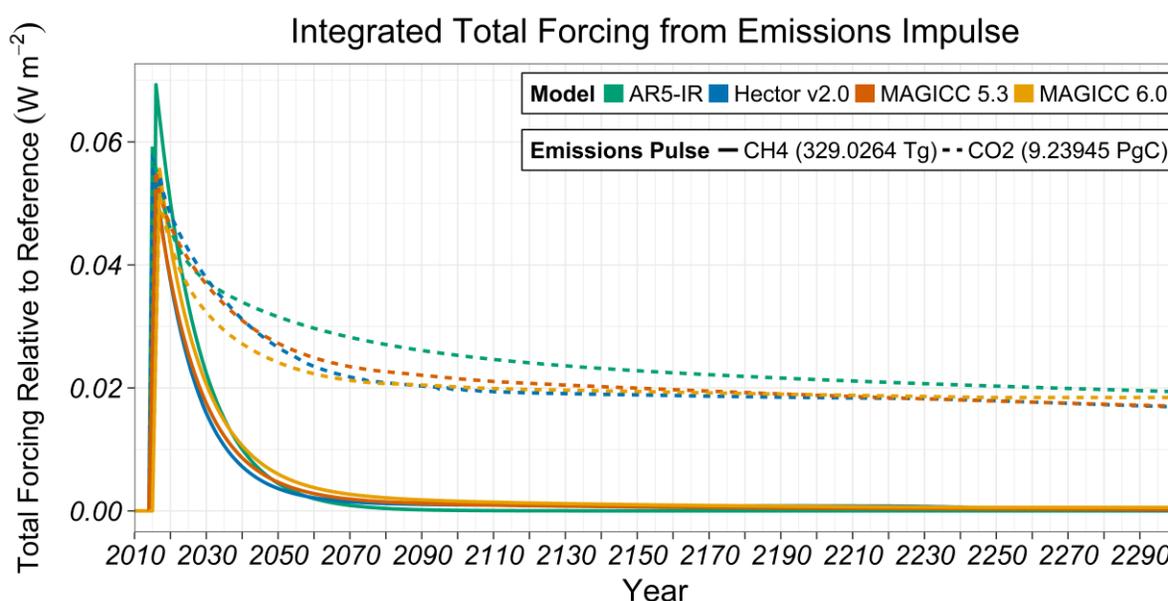


Figure S14 Total forcing response from emissions perturbations in SCMs out to 2300 (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green).

530

S8.5 Global Mean Temperature Response to a CH₄ or CO₂ Emissions Pulse

535 Figure S15 shows the temperature response from a CH₄ and CO₂ emissions perturbations in the SCMs out to 2300. We see that most of the SCM responses differ slightly immediately following the perturbation, but converge over time. AR5-IR has a stronger response than the other SCMs immediately following the perturbation. More details are included in the main paper.

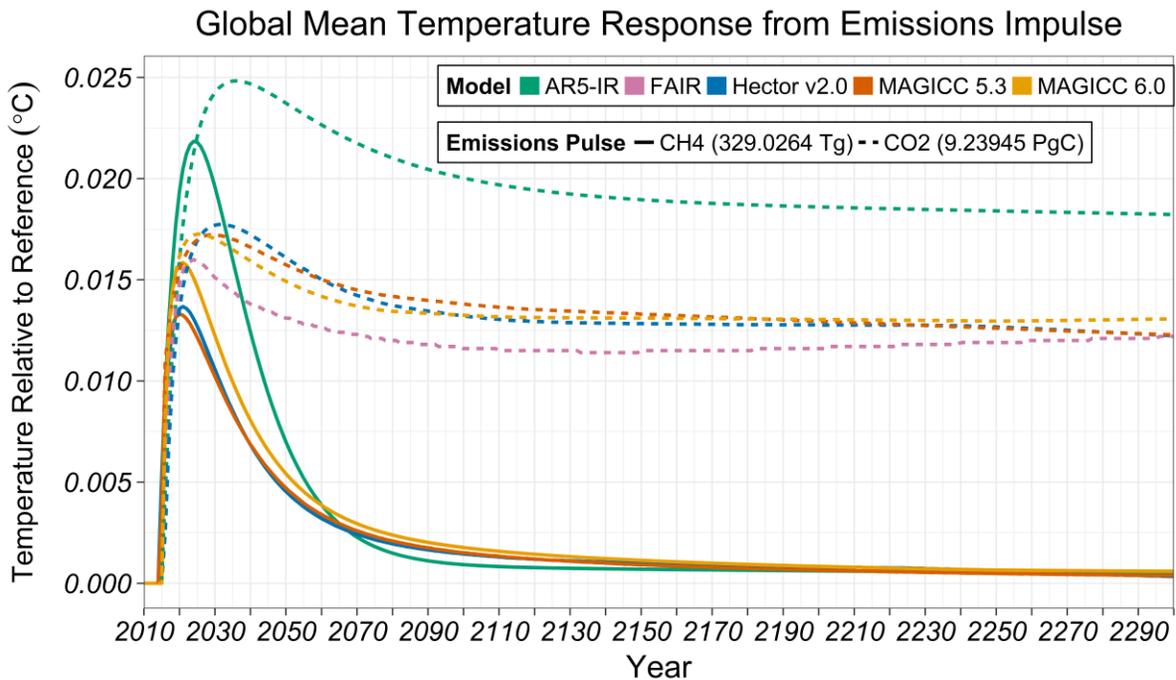


Figure S15 Global mean temperature response from emissions perturbations in SCMs out to 2300 (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR - pink).

540

S9 Time Integrated Responses

Figure S16 – Figure S21 shows the integrated forcing and temperature response for the full suite of experiments to the end of the model period. The data tables in this section provide numerical data (rounded to three significant figures) supporting the integrated forcing or temperature response figures. The data tables also include percent differences found using the following formula:

545

$$\text{Percent Difference}_{i,t} = \left(\frac{\text{Model response}_{i,t} - \text{Average Comprehensive Model Response}_t}{\text{Average Comprehensive Model Response}_t} \right) \times 100 \quad (12)$$

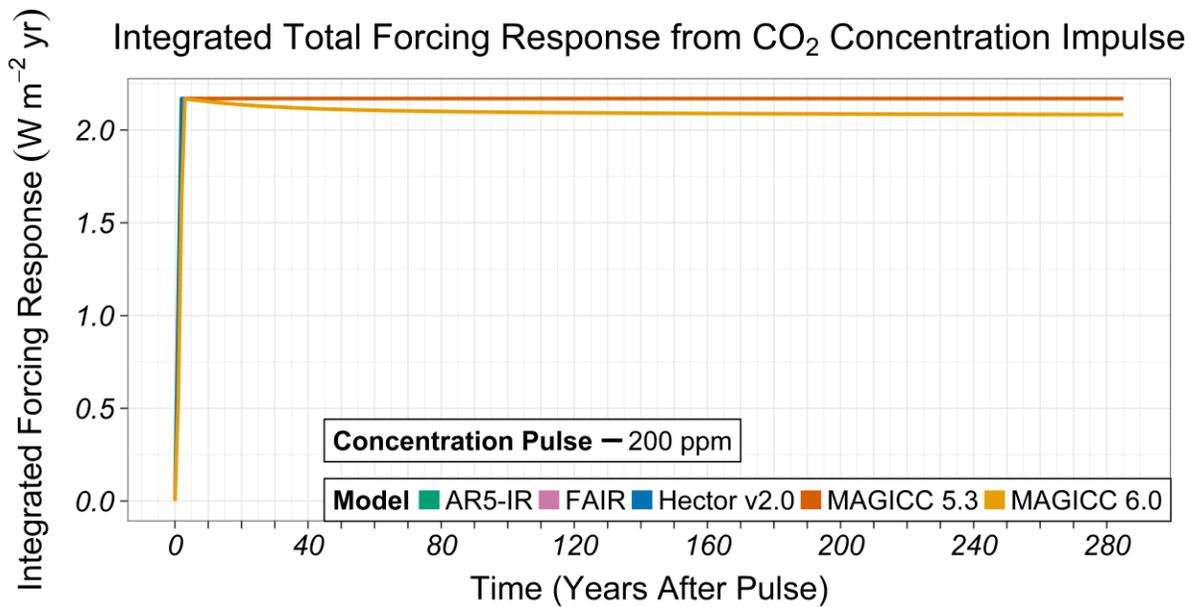
550

where t is the time horizon and i is the individual model. A positive percent difference indicates that the model response is stronger than the average comprehensive model response, while a negative value indicates the model response was weaker than the average comprehensive model response.

555

S9.1 Time Integrated Responses from a CO₂ Concentration Impulse

Figure S16 shows the time-integrated total forcing response from a CO₂ concentration impulse.

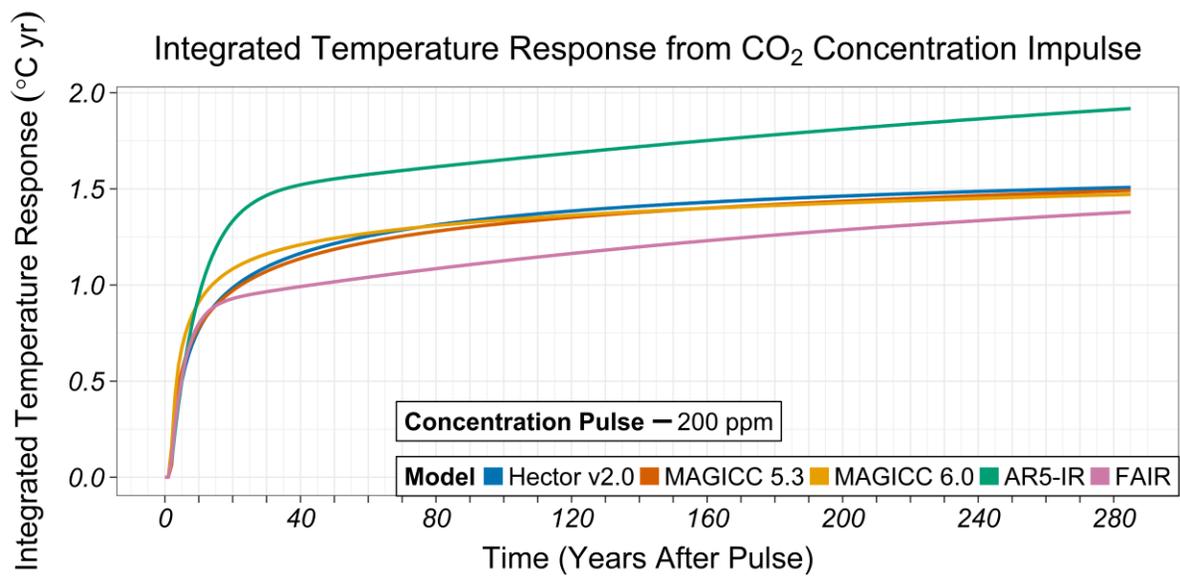


560

Figure S16 Time-integrated forcing response from a CO₂ concentration impulse for the SCMs to the end of the model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR - pink).

Figure S17 shows the time-integrated global mean temperature response from a CO₂ concentration impulse to the end of the model period. We see that the comprehensive SCMs respond similarly, while AR5-IR has a stronger response and FAIR, a slightly weaker response. The associated values time integrated temperature responses are in Table S4.

565



570 **Figure S17** Time-integrated temperature response from a CO₂ concentration impulse for the SCMs to the end of the model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, HECTOR v2.0 – blue, AR5-IR – green, FAIR - pink).

575

578 **Table S4** Integrated Temperature Responses from a CO₂ Concentration Impulse in the SCMs

579

Time After Pulse	Integrated Temperature Response (°Cyr)						Percent Difference from Comprehensive SCMs Average (%)				
	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	FAIR	AR5-IR	Average of Comprehensive SCMs	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	FAIR	AR5-IR
10	0.85	0.98	0.85	0.87	0.24	0.90	-4.79	9.59	-4.79	-3.57	-73.5
20	1.00	1.11	1.02	0.94	1.10	1.04	-4.25	6.29	-2.04	-9.80	5.33
50	1.20	1.25	1.22	1.02	1.39	1.22	-2.07	2.26	-0.19	-16.6	13.7
100	1.32	1.34	1.35	1.13	1.65	1.34	-1.25	0.25	1.00	-15.5	23.4
150	1.39	1.39	1.42	1.13	1.74	1.40	-0.71	-0.71	1.43	-19.3	24.3
285	1.46	1.47	1.51	1.38	1.92	1.48	-1.31	-0.63	1.94	-6.71	29.8

580

581

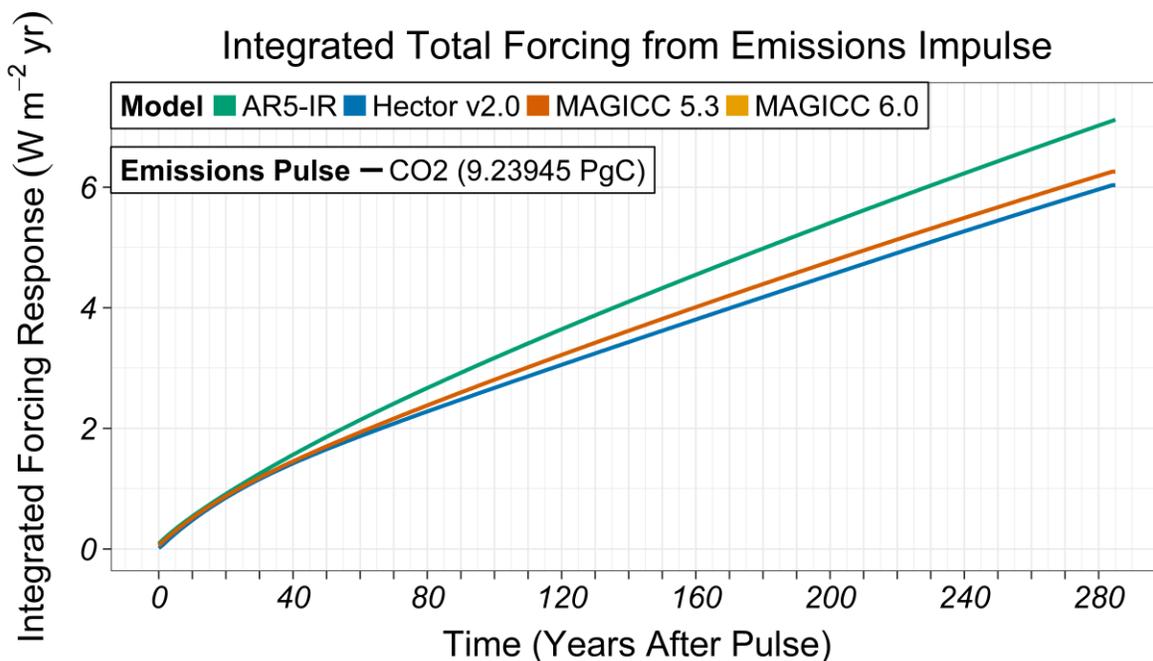
582 **S9.2 Time Integrated Responses from a CO₂ Emissions Impulse**

583

584 Figure S18 and Figure S19 show the integrated forcing (Table S5) and temperature response

585 (Table S6) for the CO₂ emissions impulse experiment to the end of the model period,

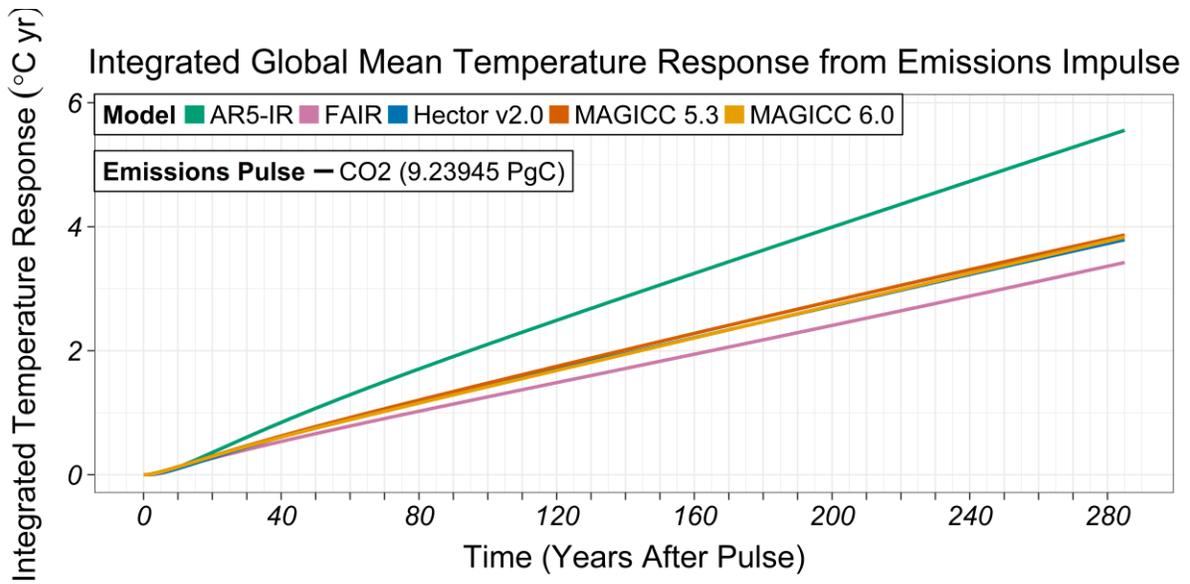
586 respectively. The numerical data is shown in Table S5 and Table S6.



587

588 **Figure S18** Time-integrated total forcing response from a CO₂ emissions impulse for the SCMs to the end of the

589 model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green).



590 **Figure S19** Time-integrated temperature response from a CO₂ emissions impulse for the SCMs to the end of the
 591 model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR - pink).
 592
 593

594 **Table S5** Integrated Forcing Responses from a CO₂ Emissions Impulse in the SCMs

595

Time After Pulse	Integrated Forcing Response (Wm ⁻² yr)					Percent Difference from Comprehensive SCMs Average (%)			
	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR	Average of Comprehensive SCMs	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR
10	0.51	0.43	0.48	0.54	0.47	8.67	-9.51	0.85	14.38
20	0.88	0.75	0.85	0.91	0.82	6.39	-9.38	2.99	10.63
50	1.70	1.48	1.65	1.86	1.61	5.63	-8.28	2.65	15.38
100	2.81	2.50	2.67	3.17	2.66	5.52	-5.96	0.44	19.13
150	3.82	3.47	3.62	4.32	3.63	4.97	-4.52	-0.45	18.87
285	6.26	5.97	6.03	7.12	6.09	2.79	-1.89	-0.90	16.98

596

597

598 **Table S6** Integrated Temperature Responses from a CO₂ Emissions Impulse in the SCMs

599

Time After Pulse	Integrated Temperature Response (°Cyr)						Percent Difference from Comprehensive SCMs Average (%)				
	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	FAIR	AR5-IR	Average of Comprehensive SCMs	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	FAIR	AR5-IR
10	0.16	0.16	0.13	0.14	0.18	0.15	6.81	5.49	-12.31	-5.71	20.66
20	0.33	0.33	0.31	0.29	0.42	0.32	2.99	1.44	-4.43	-9.38	29.90
50	0.81	0.78	0.79	0.69	1.00	0.79	1.86	-1.69	-0.17	-13.07	26.15
100	1.50	1.45	1.46	1.27	1.93	1.47	2.16	-1.59	-0.57	-13.51	31.44
150	2.17	2.10	2.10	1.85	2.86	2.12	2.20	-1.10	-1.10	-12.87	34.69
285	3.87	3.85	3.80	3.44	5.87	3.84	0.83	0.17	-1.00	-10.38	52.93

600 **S9.3 Time Integrated Responses from a CH₄ Emissions Impulse**

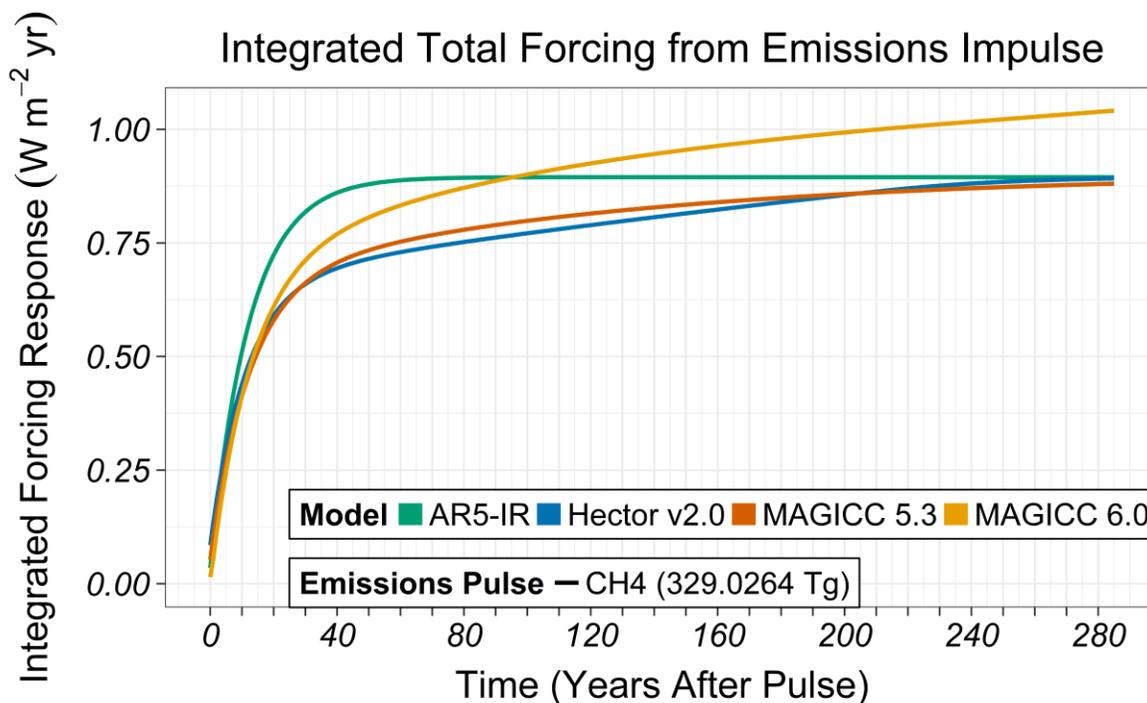
601

602 Figure S17 and Figure S18 show the integrated forcing (Table S6) and temperature response

603 (Table S7) for the CH₄ emissions impulse experiment to the end of the model period. The

604 numerical data in Table S6 and Table S7.

605

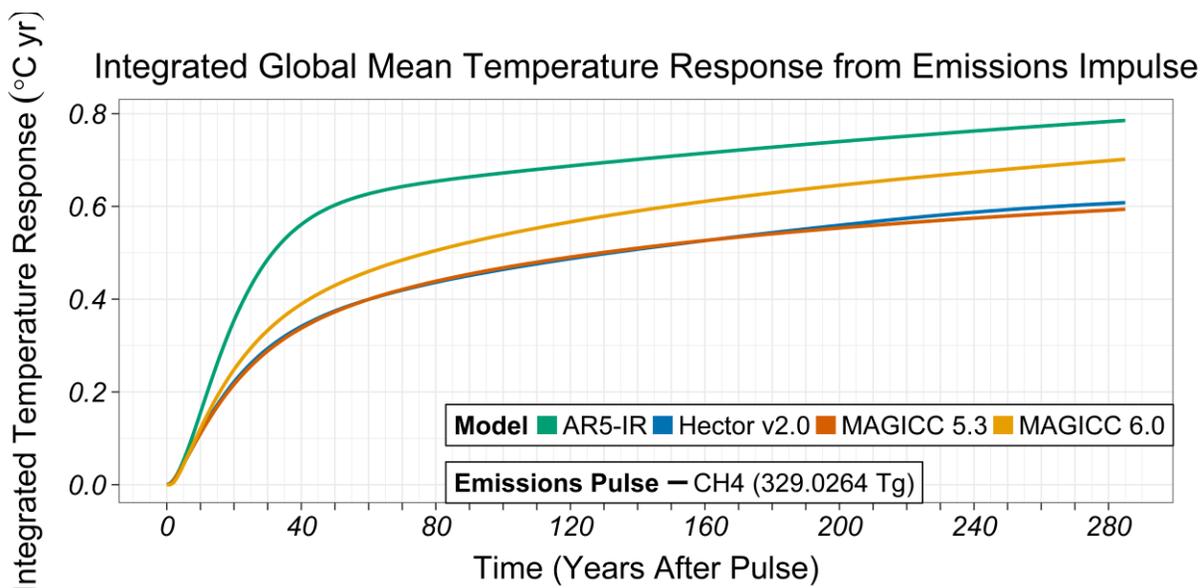


606

607 **Figure S20** Time-integrated total forcing response from a CH₄ emissions impulse for the SCMs to the end of the
608 model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green).

609

610



611

612 **Figure S21** Time-integrated temperature response from a CO₂ emissions impulse for the SCMs to the end of the
613 model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR - pink).

614

615 **Table S7** Integrated Forcing Responses from a CH₄ Emissions Impulse in the SCMs

Time After Pulse	Integrated Forcing Response (Wm ⁻² yr)					Percent Difference from Comprehensive SCMs Average (%)			
	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR	Average of Comprehensive SCMs	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR
10	0.41	0.41	0.44	0.51	0.42	-2.14	-2.14	4.28	21.1
20	0.58	0.61	0.59	0.72	0.59	-2.31	2.76	-0.45	21.9
50	0.73	0.81	0.72	0.88	0.75	-2.44	7.28	-4.84	16.9
100	0.80	0.90	0.77	0.89	0.82	-3.04	9.36	-6.32	8.63
150	0.83	0.95	0.82	0.89	0.87	-3.88	9.95	-6.07	3.03
285	0.88	1.04	0.89	0.89	0.94	-6.01	10.9	-4.94	-4.62

616

617

618 **Table S8** Integrated Temperature Responses from a CH₄ Emissions Impulse in the SCMs

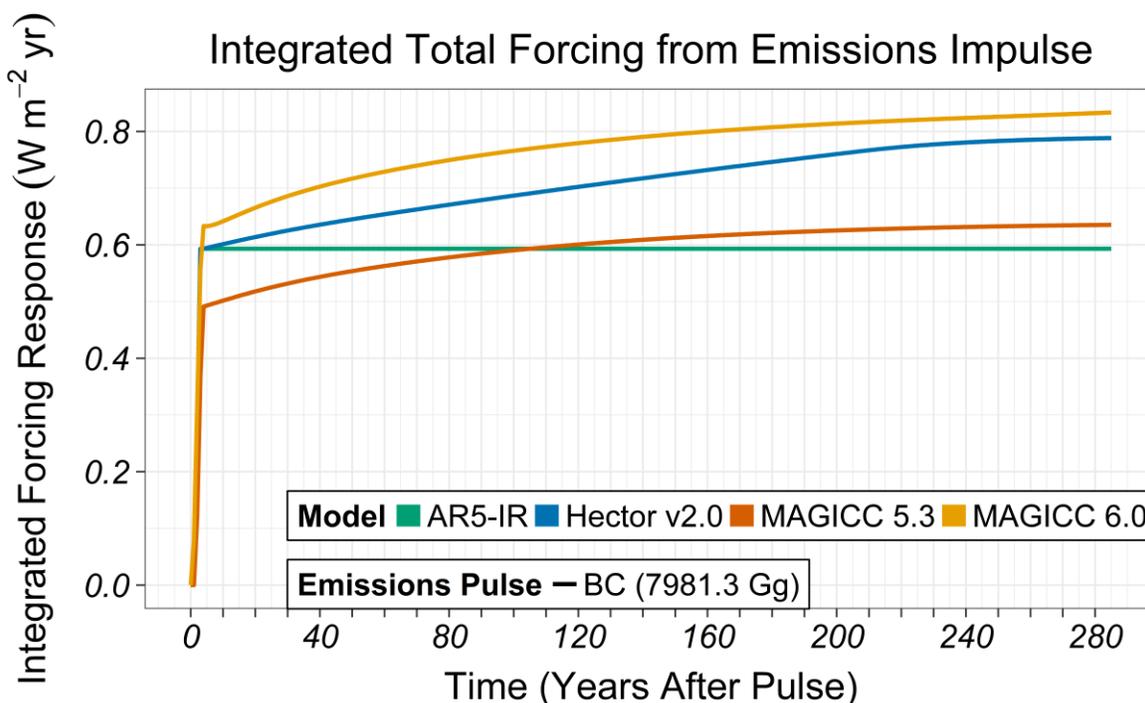
Time After Pulse	Integrated Temperature Response (°Cyr)					Percent Difference from Comprehensive SCMs Average (%)			
	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR	Average of Comprehensive SCMs	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR
10	0.13	0.15	0.14	0.16	0.14	-4.26	7.10	-2.83	17.2
20	0.23	0.27	0.24	0.36	0.25	-5.56	8.68	-3.12	47.4
50	0.38	0.44	0.38	0.45	0.40	-5.03	9.55	-4.52	12.3
100	0.47	0.54	0.47	0.58	0.49	-4.54	9.88	-5.35	17.4
150	0.52	0.60	0.52	0.70	0.55	-4.99	10.2	-5.17	28.1
285	0.60	0.70	0.61	0.85	0.64	-6.20	10.5	-4.31	33.5

619 **S9.4 Time Integrated Responses from a BC Emissions Impulse**

620

621 Figure S19 and Figure S20 show the integrated forcing and temperature response for the BC
622 emissions impulse experiment to the end of the model period, respectively. FAIR is not in this
623 figure because we used FAIR v1.0, which only represented the response from CO₂ emissions. An
624 updated version, FAIR v1.3, was recently released and includes non-CO₂ forcing. Table S8
625 shows the integrated temperature response data.

626

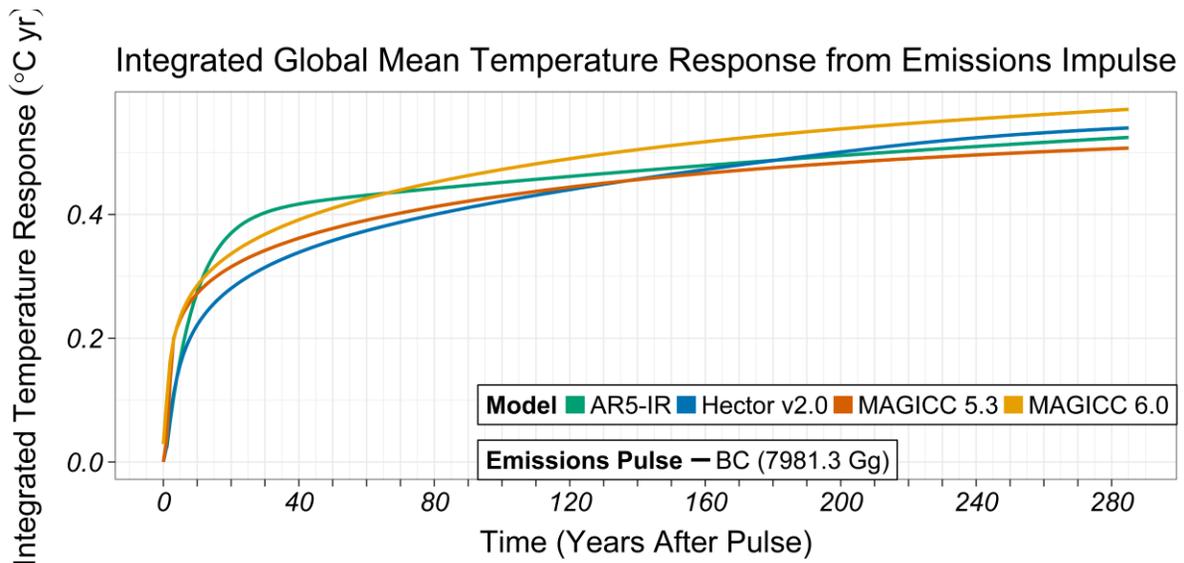


627

628 **Figure S22** Time-integrated total forcing response from a BC emissions impulse for the SCMs to the end of the
629 model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green).

630

631



632

633

634 **Figure S23** Time-integrated temperature response from a BC emissions impulse for the SCMs to the end of the
635 model period (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR - pink).

636

637 We see that Hector v2.0, which does not differentiate BC forcing over land and ocean and has a
638 9% weaker response 20 years after the pulse. MAGICC 6.0 diverges from the MAGICC 5.3
639 temperature response 20 years after the pulse. AR5-IR represents the temperature response from
640 a BC perturbation as a simple exponential decay analogous to the greenhouse gas IRF, leading to
641 a much stronger integrated temperature response (20%) 20 years after the pulse.

642

643 **Table S9** Integrated Temperature Responses from a BC Emissions Impulse in the SCMs

Time After Pulse	Integrated Temperature Response (°Cyr)					Percent Difference from Comprehensive SCMs Average (%)			
	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR	Average of Comprehensive SCMs	MAGICC 5.3 BC-OC	MAGICC 6.0	Hector v2.0	AR5-IR
10	0.28	0.30	0.24	0.30	0.27	3.91	9.22	-13.1	11.0
20	0.32	0.34	0.29	0.38	0.32	1.13	8.12	-9.25	19.3
50	0.38	0.41	0.36	0.43	0.38	-1.22	7.43	-6.21	10.7
100	0.43	0.47	0.42	0.45	0.44	-2.68	7.12	-4.44	2.22
150	0.46	0.51	0.47	0.48	0.48	-3.80	6.76	-2.96	-0.92
285	0.51	0.57	0.54	0.53	0.54	-5.90	5.73	0.17	-2.56

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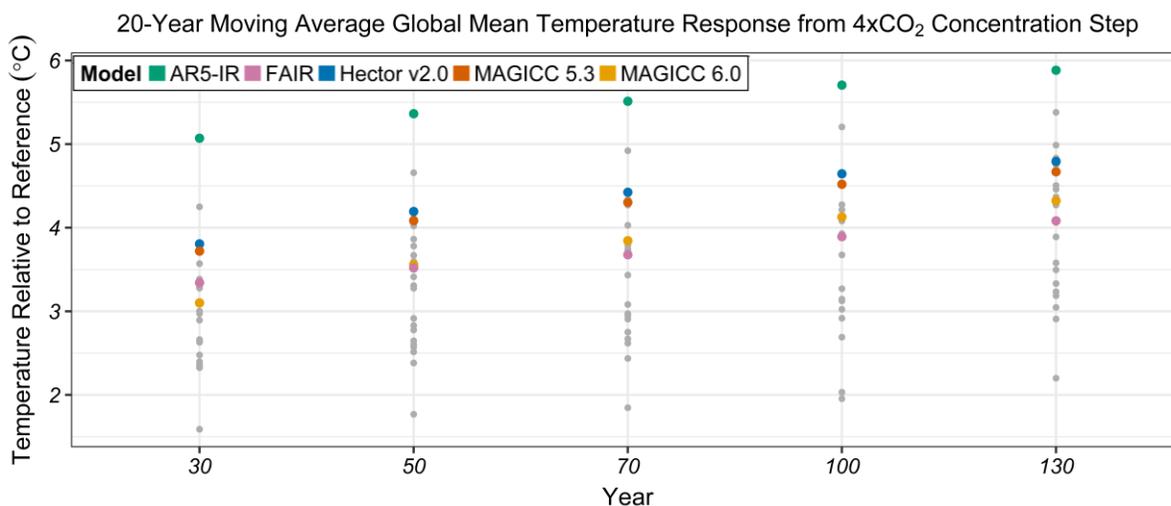
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649

650 **S10 Temporal Response of SCMs Compared to 4xCO₂ Concentration Step Experiment**
 651 **from CMIP5**

652
 653 Here we compare the 20-year moving average at time t=30, t= 50, t=70, t=100, and t=130 in the
 654 CMIP5 models and SCMs to show the temporal response of temperature. Hector v2.0 and
 655 MAGICC 5.3 have a faster response than the other SCMs and the majority of the complex
 656 models to an abrupt 4xCO₂ concentration step.



657
 658 **Figure S24** 20-Year moving average centered at year shown of the global mean temperature response from 4xCO₂
 659 concentration step in CMIP5 models (grey) and SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector
 660 v2.0 – blue, FAIR – pink, AR5-IR – green).
 661

662 Table S10 shows the ECS values and the realized warming fraction (RWF) for the CMIP5 data
 663 and SCMs used to produce Figure 4. The RWF reveals that the SCMs used in this study
 664 generally warm faster than the more complex models in CMIP5.
 665

666

667 **Table S10** *CMIP5 and SCM model information with ECS and RWF*

668

Centre(s)	Model name	ESC (°C)	RWF (%) $\sqrt{2}x \frac{\text{Average of the last 40 years}}{ECS}$
Beijing Climate Center (BCC) China	BCC-CSM1.1	2.8	58
Canadian Centre for Climate Modelling and Analysis (CCCma) Canada	CanESM2	3.7	54
National Center for Atmospheric Research USA	CCSM4	2.9	51
Centre National de Recherches Météorologiques, Centre Européen de Recherche et de Formation Avancée en Calcul Scientifique (CNRM-CERFACS) France	CNRM-CM5	3.3	51
Commonwealth Scientific and Industrial Research Organization/Queensland Climate Change Centre of Excellence Australia	CSIRO-Mk3-6-0	4.1	47
Institut Pierre Simon Laplace (IPSL) France	IPSL-CM5A-LR	4.1	49
	IPSL-CM5A- MR	NA	--
	IPSL-CM5B-LR	2.6	54
Institute of Atmospheric Physics, Chinese Academy of Sciences (LASG-CESS) China	FGOALS-g2	NA	--
	MIROC-ESM	4.7	48

Atmosphere and Ocean Research Institute (The University of Tokyo), National Institute for Environmental Studies, and Japan Agency for Marine-Earth Science and Technology (MIROC) Japan	MIROC5	2.7	49
Max Planck Institute for Meteorology (MPI-M) Germany	MPI-ESM-MR	NA	--
	MPI-ESM-P	3.5	51
Meteorological Research Institute Japan	MRI-CGCM3	2.6	55
Norwegian Meteorological Institute Norway	NorESM1-M	2.8	48
NASA/GISS (Goddard Institute for Space Studies; NASA-GISS) USA	GISS-E2-H	2.3	49
	GISS-E2-R	2.1	44
Geophysical Fluid Dynamics Laboratory (NCAR; NSF-DOE-NCAR) USA	GFDL-CM3	4.0	52
	GFDL-ESM2G	2.4	57
	GFDL-ESM2M	2.4	65
Raper et al., 1996; Wigley and Raper 2002; Smith and Bond 2014	MAGICC 5.3 BC-OC	3.0*	64
Meinshausen et al., 2011	MAGICC 6.0	3.0*	53
Hartin et al., 2015 Hartin et al., 2016	Hector v2.0	3.0*	63
Millar et al., 2017	FAIR	2.7**	61
Myhre et al., 2013	AR5-IR	3.9**	62

669 *Unless otherwise noted.

670 ** The ECS value for FAIR and AR5-IR is not adjustable (see S2)

671 Note: NA denotes models that have not reported an ESC value from Table 9.5 in IPCC AR5
672 (Flato et al., 2013).

673 **S11 Simple Sensitivity Tests in SCMs**

674

675 Here we discuss the SCM responses under a range of climate sensitivity and ocean diffusivity
676 values.

677

678 **S11.1 Changing Equilibrium Climate Sensitivity Values in SCMs with Comparison to** 679 **CMIP5**

680

681 We changed the ECS values in the SCMs to illustrate the effects of parameter selection on the
682 model responses. We reproduce Figure 4 from the main paper using different ECS values in
683 Hector v2.0, MAGCC 5.3, and MAGIC 6.0. We run each of these SCMs with a climate
684 sensitivity values of 2.1°C, the same as GISS-E2-R, and 4.7°C, the same as MIROC-ESM. These
685 two model values were selected because they represent the largest range of climate sensitivity
686 values in the model data used here.

687

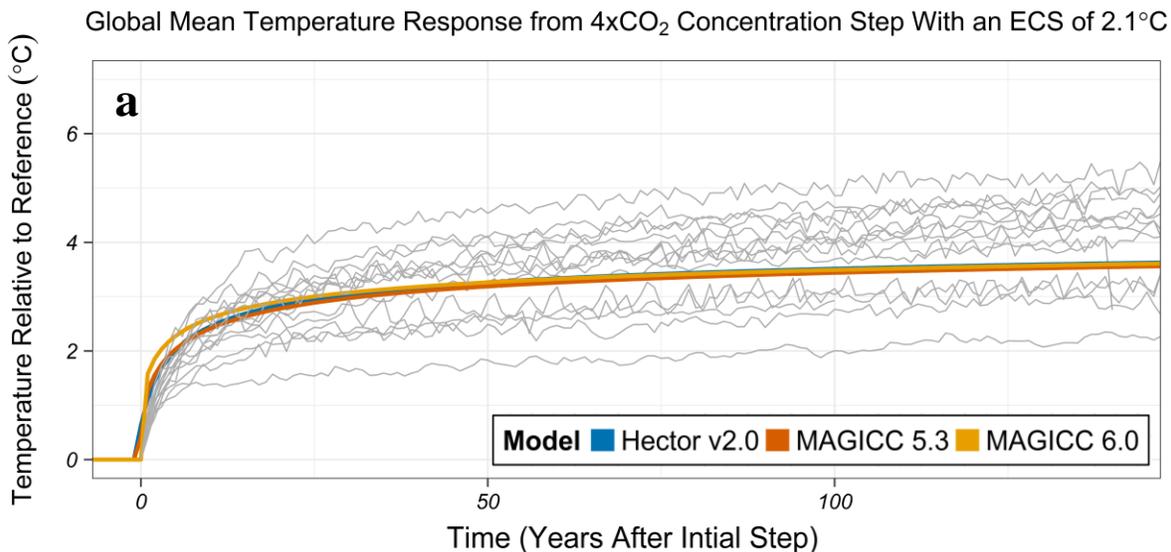
688 Figure S25 shows the global mean temperature response from 4xCO₂ concentration step in
689 CMIP5 models and SCMs. The SCMs were run with two different ECS values. Figure S25a
690 shows the SCM response with an ECS value of 2.1°C and Figure S25b shows the SCM
691 responses with an ECS value of 4.7°C. We found that spanning the range of complex model ECS
692 values still resulted in stronger SCM responses, which supports the conclusion in our main paper
693 that the SCMs have a faster warming rate under strong forcing regimes compared to more
694 complex models.

695

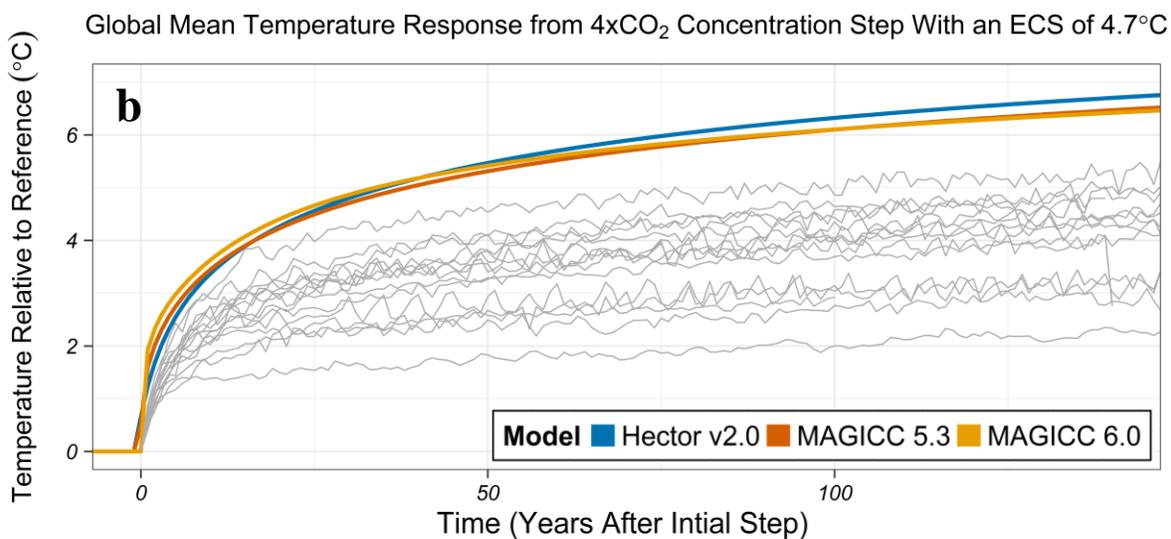
696

697

698



699



700 **Figure S25** Global mean temperature response from 4xCO₂ concentration step in CMIP5 models and SCMs, as in
701 Figure 5, with the SCMs run with two different ECS values. Figure 22a shows the SCM response with an ECS
702 value of 2.1°C, and Figure 22b shows the SCM responses with an ECS value of 4.7°C (MAGICCC 6.0 – yellow,
703 MAGICCC 5.3 BC-OC – red, Hector v2.0 – blue)

703

704

705

706

707 **S11.2 Additional Sensitivity Experiment in SCMs Using MAGICC6.0 Parameters**

708
709 The aim of this paper is not to validate any individual SCM, nor the range of parameters used in
710 the SCMs, which are also explored in the literature cited in our manuscript. Rather, we are
711 evaluating the fundamental behavior of the simple models. However, understanding the
712 uncertainty associated with our results is important.

713
714 In S11.1 we conducted a simple sensitivity test for the 4xCO₂ concentration step
715 experiment by changing the climate sensitivity values in the three comprehensive SCMs
716 used in this paper. Below, we have added some additional tests by exploring a range of
717 climate sensitivity values and ocean diffusivity values in MAGICC 6.0 under a unit pulse of
718 CO₂ emissions and a unit pulse of CO₂ concentration.

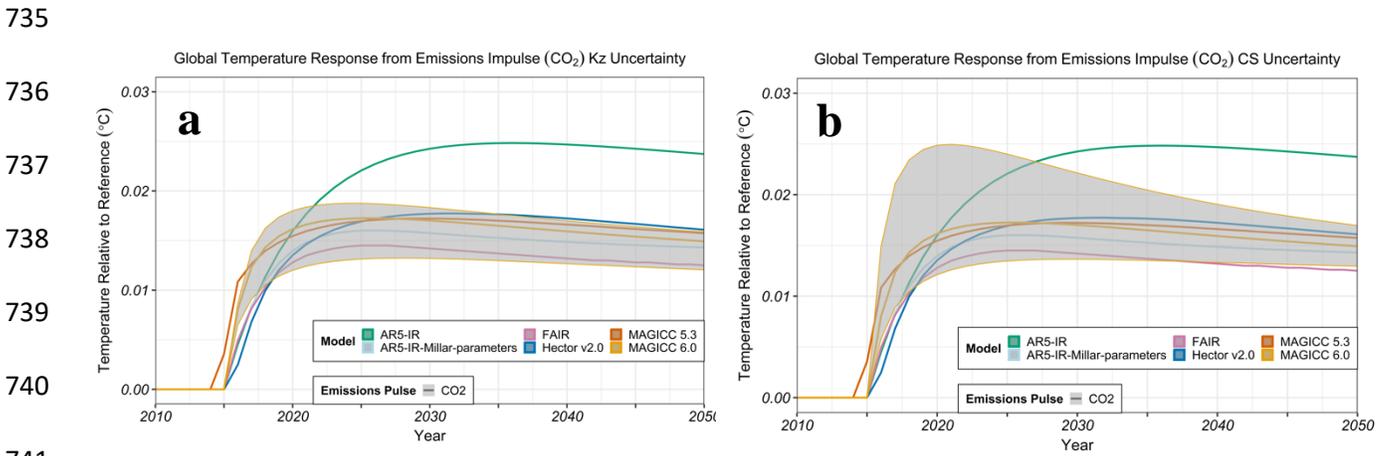
719
720 We selected climate sensitivity and ocean diffusivity values from the parameter ranges
721 presented in Table 1B in Meinshausen et al. (2011). The values are the native MAGICC 6.0
722 parameters required to emulate complex models used in CMIP3 using three calibrated
723 parameters (climate sensitivity, ocean diffusivity, and land/ocean warming). We provided
724 the climate sensitivity and ocean diffusivity value ranges we explored in Table 11 below.

725
726 **Table S11** MAGICC 6.0 parameter values from Meinshausen et al., 2011 Table 1B for
727 sensitivity tests

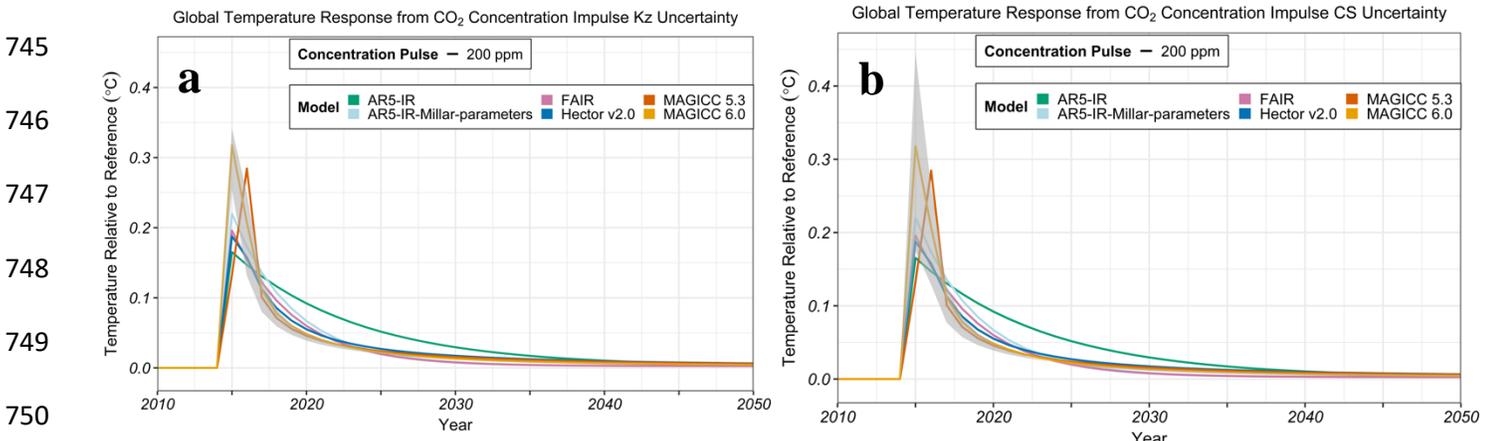
Scenario	Climate sensitivity (K)	Ocean diffusivity (cm ² s ⁻¹)
Base Case	3.0	1.1
High Ocean diffusivity	3.0	3.74
Low Ocean diffusivity	3.0	0.50
High Climate sensitivity	6.03	1.1
Low Climate sensitivity	1.94	1.1

728

729 Figure S26 shows the global mean temperature response exploring the range of ocean
 730 diffusivity (K_z) (a) and global mean temperature response exploring the range of climate
 731 sensitivity (CS) (b) under a CO_2 emissions perturbation. Figure S27 shows the same results for
 732 under a CO_2 concentration pulse. Both figures illustrate that climate sensitivity has the greatest
 733 impact on the responses and in our manuscript, we accounted for this and used similar climate
 734 sensitivity values in SCMs where possible, unless otherwise noted in the supplemental figures.



741 **Figure S26** Global mean temperature response exploring the range of ocean diffusivity (K_z) (a) and Global mean
 742 temperature response exploring the range of climate sensitivity (CS) (b) from a CO_2 emissions perturbation in SCMs. The
 743 grey shaded region in each figure shows the range in MAGICC 6.0 responses found using the Table S11 parameters. We
 744 note that the range of responses exploring CS (b) are normalized to account for the different climate conditions under
 745 difference CS values. (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR –
 746 pink, AR5-IR-Millar-parameters –light blue)



751 **Figure S27** Temperature response exploring the range of climate sensitivity (CS) (b) from a CO_2 concentration pulse in SCMs
 752 (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue, AR5-IR – green, FAIR –pink, AR5-IR-Millar-parameters
 753 –light blue). The grey shaded region in each figure shows the range in MAGICC 6.0 responses found using the Table R2
 754 parameters. We note that the range of responses exploring CS (b) are normalized to account for the different climate conditions
 755 difference CS values.

754 We acknowledge, however, that vertical ocean diffusivity has a large impact on ocean heat
755 uptake and we do note that this parameter selection also impacts the responses in the SCMs,
756 particular under a CO₂ emissions pulse (Meinshausen et al., 2011). However, the SCMs we
757 compare in our paper either do not have the same definitions of vertical ocean diffusivity, as
758 is the case for the comprehensive SCMs, or ocean diffusivity is not directly represented in
759 the models, as is the case for idealized SCMs. For our purposes, therefore, we kept the
760 ocean diffusivity values at their default values within the comprehensive SCMs.

761
762 For completeness, we also acknowledge that Meinshausen et al. (2011) spanned ranges of
763 land/ocean warming contrast (RLO) in the three-parameter calibration described in Table 1B
764 of their manuscript. And again, the SCMs either use the same values of RLO, as is the case
765 for both versions of MAGICC, or this parameter is not represented in the idealized models.
766 In fact, from our work using impulse response test to characterize SCMs, we concluded that
767 SCMs without differential warming do not correctly capture the response pattern to BC
768 perturbations.

769 **S12 Comparison to Previous Impulse Responses Work by Joos et al. (2013)**

770
771 We conducted the same perturbation experiment done by Joos et al. (2013) with our three
772 comprehensive SCMs and two idealized SCMs, however, we do not conduct this against a
773 constant CO₂ concentration background. Instead, we use the RCP 4.5 scenario and add a 100GtC
774 CO₂ pulse in 2015. The versions used in each study differ slightly. Joos et al. used MAGICC
775 model version 6.3 run in 171 different parameter settings that emulate 19 AOGCMs and 9
776 coupled climate-carbon cycle models. MAGICC 6.0 used in this study was set at the default
777 setting using the AOGCM multi-model mean.

778
779 Table S12 shows the time-integrated airborne fraction at chosen time horizons from the 100 GtC
780 pulse of CO₂ emissions. The Table S12 results are graphically represented in Figure S28. These
781 results are largely discussed in the main paper.

782

783 **Table S12** Time-integrated Airborne Fraction from a 100 GtC CO₂ Emissions Impulse in SCMs
 784 Compared to Results from Table 4 in Joos et al. (2013)

Time Horizon	20 yr	50 yr	100 yr
NCAR CSM1.4	13.8	27.8	46.6
HadGEM2-ES	14.7	30.9	53.3
MPI-ESM	14.5	29.2	48.8
Bern3D-LPJ (reference)	15.4	34.3	61.9
Bern3D-LPJ ensemble	15.1 (14.0-16.0)	32.7 (28.9-36.0)	57.6 (48.9-65.6)
Bern2.5D-LPJ	13.9	29.7	51.1
CLIMBER2-LPJ	13.0	26.8	49.2
DCESS	14.6	31.8	56.3
GENIE ensemble	13.6 (10.9-17.6)	28.9 (21.7-41.4)	50.5 (38.3-77.9)
LOVECLIM	13.5	27.9	45.3
MESMO	15.1	33.6	61.1
UVic2.9	13.7	29.5	53.0
ACC2	13.7	27.9	46.5
Bern-SAR	14.0	29.0	48.9
TOTEM2	16.9	38.3	66.6
MAGICC 6.0 ensemble	14.0 (12.0-16.1)	29.6 (23.6-35.7)	51.8 (40.0-64.2)
Multi-model mean	14.3 ± 1.8	30.2 ± 5.7	52.4 ± 11.3
Hector v2.0	16.2	34.0	58.3
MAGICC 5.3	16.0	33.4	58.3
MAGICC 6.0	15.3	32.2	57.9
AR5-IR	15.0	31.0	53.1
FAIR	14.6	32.6	61.6

Joos et al. Comparison of Time-Integrated Airborne Fraction Response from an Emissions Impulse

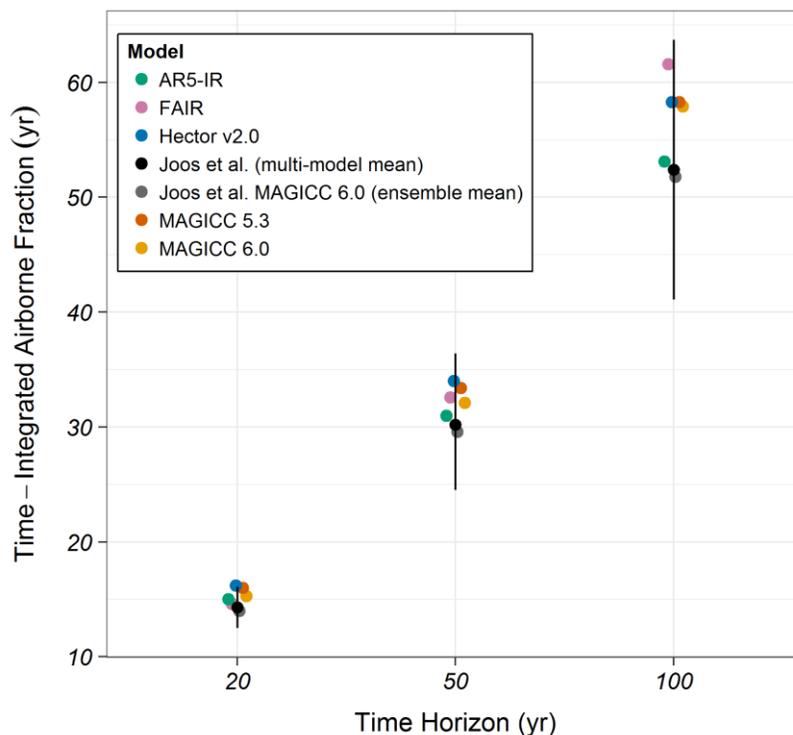


Figure S28 Time-integrated airborne fraction from a 100GtC CO₂ emissions impulse in SCMs compared to Joos et al. This is not a direct comparison because we did not perform this experiment with a constant CO₂ concentration background, as done by Joos et al. The colored points represent the time-integrated airborne fraction in the SCMs used in this study, following Joos et al., and the Joos et al. MAGICC 6.0 ensemble mean. The black point is the Joos et al. multi-model mean and the vertical black line represents the range of the Joos et al. model results. (Joos et al. MAGICC 6.0 ensemble mean –grey, MAGICC 6.0 –yellow, MAGICC 5.3 BC-OC –red, Hector v2.0 –blue, AR5-IR –green, FAIR –pink).

787 We also indirectly compare the temperature response of the comprehensive SCMs and more
788 complex models in Joos et al. MAGICC 6.0 was used both here and by Joos et al., and we find
789 similar responses with ≤ 1 °C yr difference from Joos et al. at each reported period. Though the
790 other two comprehensive SCMs were not used by Joos et al., their similar responses to our
791 MAGICC 6.0 allow us to make a larger conclusion, as done in the main paper. Using this logic,
792 we are able to validate our SCM responses from a finite pulse. We find that the comprehensive
793 SCM responses are generally less varied, close to the Joos et al. ensemble mean 20 years after
794 the pulse, and below most Joos et al. model responses 50 and 100 years after the pulse (see
795 Figure S29).

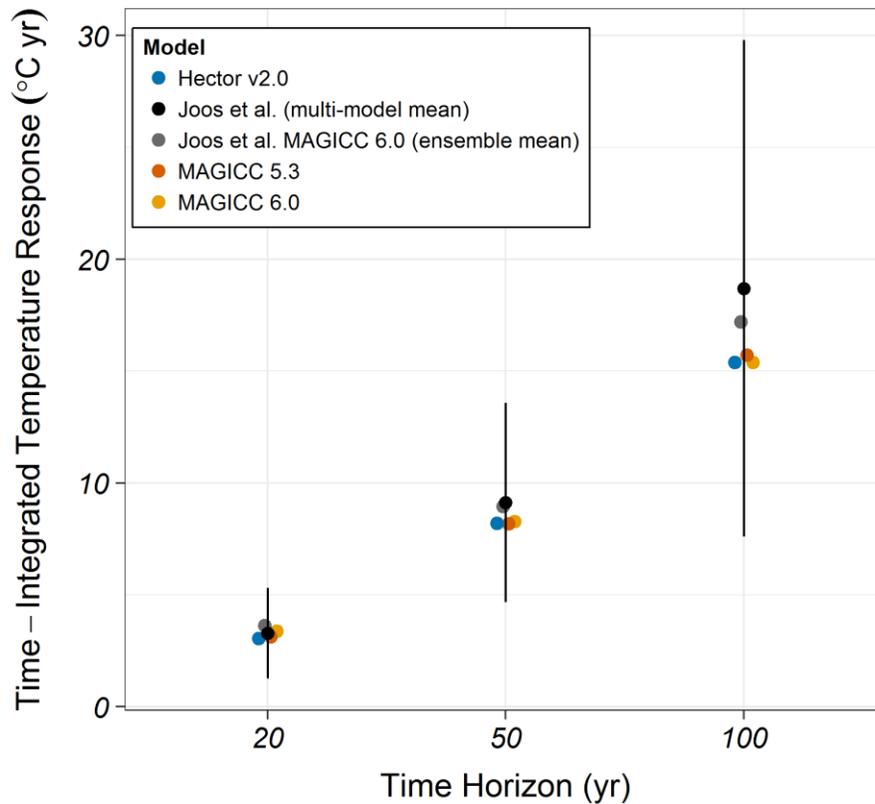
796

797 **Table S13** Time-integrated temperature response from a 100 GtC CO₂ Emissions Impulse in
798 SCMs Compared to Results from Table 7 in Joos et al. (2013).

Time Horizon	20 yr	50 yr	100 yr
NCAR CSM1.4	2.53	7.36	10.6
HadGEM2-ES	4.24	12.4	30.3
MPI-ESM	3.83	8.84	19.1
Bern3D-LPJ (reference)	4.11	12.1	24.5
Bern3D-LPJ ensemble	3.20 (2.1-4.6)	8.61 (5.1-13.5)	17.3 (9.5-29.3)
Bern2.5D-LPJ	3.15	8.40	17.1
CLIMBER2-LPJ	3.05	7.96	16.5
DCESS	3.38	9.96	20.6
GENIE ensemble	3.77	10.54	21.6
LOVECLIM	0.22	3.46	7.83
MESMO	4.41	12.5	26.0
UVic2.9	3.40	9.17	18.5
ACC2	3.99	10.55	20.0
Bern-SAR	n/a	n/a	n/a
TOTEM2	n/a	n/a	n/a
MAGICC 6.0 ensemble	3.64 (2.7-4.7)	8.96 (6.6-12.7)	17.2 (12-26)
Multi-model mean	3.29 ± 2.03	9.13 ± 4.45	18.7 ± 11.1
Hector v2.0	3.05	8.20	15.54
MAGICC 5.3	3.13	8.19	15.73
MAGICC 6.0	3.39	8.28	15.54

799

Joos et al. Comparison of Time-Integrated Temperature Response from an Emissions Impulse



800

801 **Figure S29** Time-integrated temperature response from a 100GtC CO₂ emissions impulse in SCMs compared to
 802 Joos et al. This is not a direct comparison because we did not perform this experiment with a constant CO₂
 803 concentration background, as done by Joos et al. The colored points represent the time-integrated temperature
 804 response in the SCMs used in this study, following Joos et al., and the Joos et al. MAGICCC 6.0 ensemble mean. The
 805 black point is the Joos et al. multi-model mean and the vertical black line represents the range of the Joos et al.
 806 model results. (Joos et al. MAGICCC 6.0 ensemble mean –grey, MAGICCC 6.0 – yellow, MAGICCC 5.3 BC-OC – red,
 807 Hector v2.0 – blue).

808

809 We compare the comprehensive SCM responses from the 100GtC CO₂ pulse to our earlier
 810 experiment using a ~10GtC CO₂ pulse. We find that the relative behavior of the comprehensive
 811 SCMs in the 100 GtC CO₂ impulse is similar to the response pattern from the smaller pulse
 812 experiment (see Figure 3a and Figure S29). The MAGICC 6.0 temperature response pattern is
 813 consistent with our prior experiments, where we see an initially stronger response (10 years
 814 following the perturbation) compared to the other comprehensive SCMs. Due to the initial
 815 oscillatory behavior in complex model responses (see Figure 2a in Joos et al. (2013)), it is
 816 difficult to compare SCM responses to complex models on these short time scale.
 817

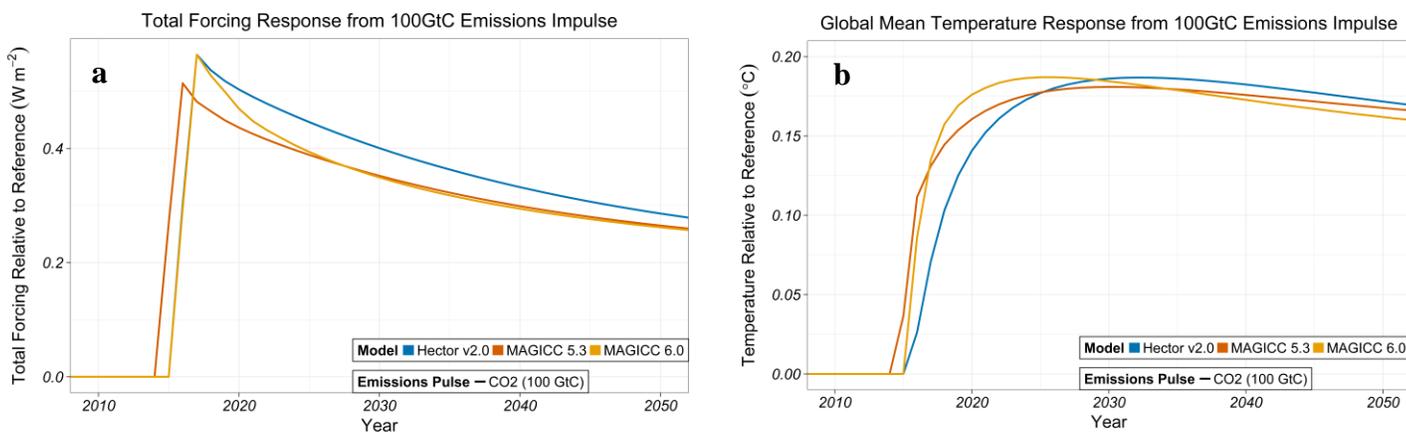


Figure S30 Total forcing response (a) and global mean temperature response (b) from a 100GtC CO₂ emissions impulse in the SCMs (MAGICC 6.0 – yellow, MAGICC 5.3 BC-OC – red, Hector v2.0 – blue).

818
 819
 820

821 **S13 Investigating Temperature Response from BC Step Experiment**

822

823 We investigate SCM responses to a black carbon (BC) emissions step by quadrupling (4x) the
824 values in 2015. We choose two of the SCMs, Hector v2.0 and MAGICC 5.3, as examples and
825 compare the temperature response to Figure 1 in Sand et al. (2016). Sand et al. finds that after
826 applying a 25x BC emissions step to NorESM1-M, a complex climate model, the temperature
827 response levels off after less than 10 years. We find that temperature in both of these SCMs
828 continue to increase over a century time-scale after the BC perturbation. The SCMs, therefore,
829 fail to capture the temporal response to BC as seen in Sand et al. (2016), also seen in Yang et al.
830 (2019).

831

832

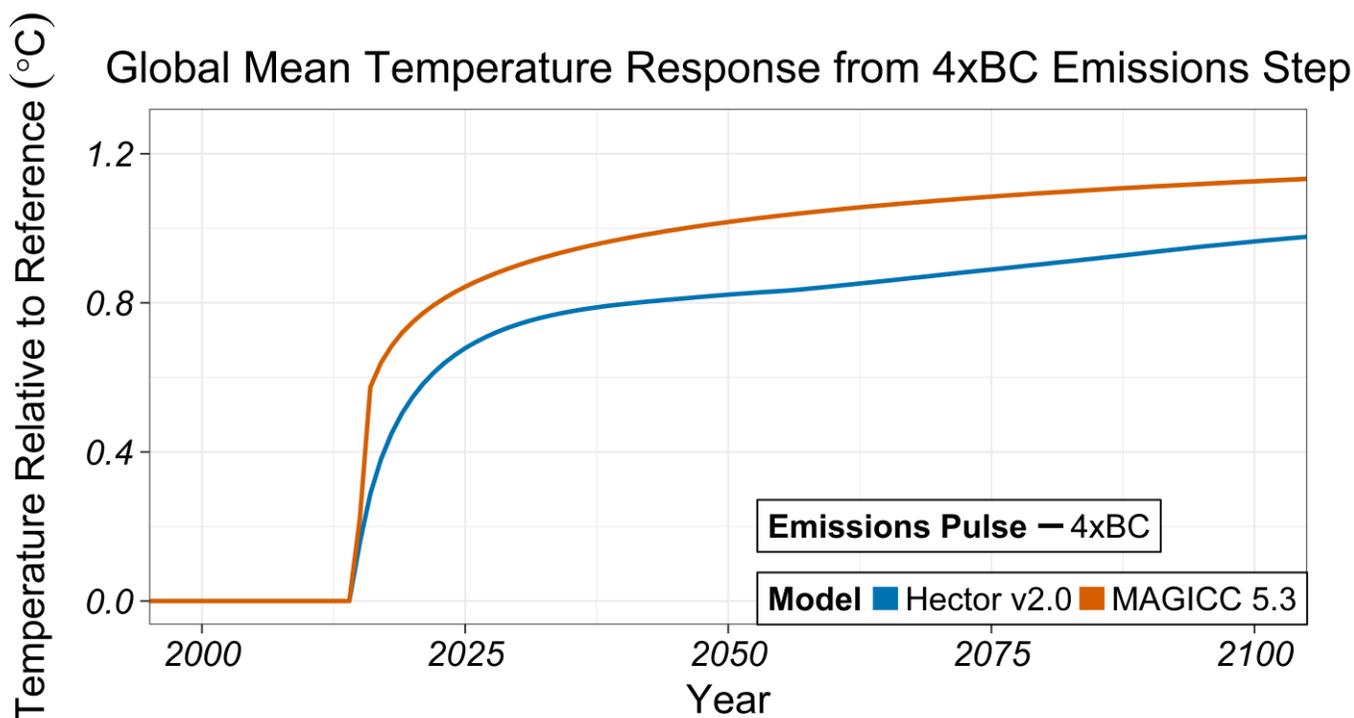


Figure S31 Global mean temperature response from a 4xBC emissions step in the SCMs (MAGICC 5.3 BC-OC – red, Hector v2.0 – blue).

833 **S14 Supplementary Data**

834

835 Other supplementary materials for this manuscript can be found at
836 <https://github.com/akschw04/Fundamental-Impulse-Tests-in-SCMs-Datasets> and include the
837 following:

838

839 **Dataset S1 (separate file)**

840 Simple climate model responses from 4xBC emissions step.

841

842 **Dataset S2 (separate file)**

843 Simple climate model responses from 4xCO₂ concentration step with 2.3 ocean diffusion and an
844 ECS = 3 °C.

845

846 **Dataset S3 (separate file)**

847 Simple climate model responses from a 100PgC CO₂ emissions impulse experiment.

848

849 **Dataset S4 (separate file)**

850 Simple climate model responses from a CH₄ emissions impulse experiment.

851

852 **Dataset S5 (separate file)**

853 Simple climate model responses from a BC emissions impulse experiment.

854

855 **Dataset S6 (separate file)**

856 Simple climate model responses from CO₂ concentration impulse experiment.

857

858 **Dataset S7 (separate file)**

859 Simple climate model responses from CO₂ emissions impulse experiment.

860

861 **Dataset S8 (separate file)**

862 AR5-IR code to produce responses to BC emissions impulse.

863
864 **Dataset S9 (separate file)**
865 AR5-IR code to produce responses to CH₄ emissions impulse.
866
867 **Dataset S10 (separate file)**
868 AR5-IR code to produce responses to CO₂ emissions impulse.
869
870 **Dataset S11 (separate file)**
871 AR5-IR code to produce responses to 100PgC CO₂ emissions impulse for comparison to Joos *et*
872 *al.* (2013)
873
874 **Dataset S12 (separate file)**
875 AR5-IR code to produce responses to CO₂ concentration step.
876
877 **Dataset S13 (separate file)**
878 FAIR CO₂ concentration impulse experiment input file.
879
880 **Dataset S14 (separate file)**
881 FAIR 4xCO₂ concentration step experiment input file.
882
883 **Dataset S15 (separate file)**
884 FAIR CO₂ emissions impulse experiment input file.
885
886 **Dataset S16 (separate file)**
887 FAIR 100Pg CO₂ emissions impulse experiment input file.
888
889 **Dataset S17 (separate file)**
890 FAIR CO₂ emissions impulse experiment reference input file.
891

892 **Dataset S18 (separate file)**

893 Hector v2.0 CO₂ concentration impulse experiment input file.

894

895 **Dataset S19 (separate file)**

896 Hector v2.0 CO₂ concentration impulse experiment reference input file.

897

898 **Dataset S20 (separate file)**

899 Hector v2.0 4xCO₂ concentration step experiment reference input file.

900

901 **Dataset S21 (separate file)**

902 Hector v2.0 4xCO₂ concentration step experiment input file.

903

904 **Dataset S22 (separate file)**

905 Hector v2.0 BC emissions impulse experiment input file.

906

907 **Dataset S23 (separate file)**

908 Hector v2.0 BC emissions step experiment input file.

909

910 **Dataset S24 (separate file)**

911 Hector v2.0 CH₄ emissions impulse experiment input file.

912

913 **Dataset S25 (separate file)**

914 Hector v2.0 CO₂ emissions impulse experiment input file.

915

916 **Dataset S26 (separate file)**

917 Hector v2.0 100Pg CO₂ emissions impulse experiment input file.

918

919 **Dataset S27 (separate file)**

920 Hector v2.0 emissions impulse experiment reference input file.
921
922 **Dataset S28 (separate file)**
923 Hector v2.0 emissions step experiment reference input file.
924
925 **Dataset S29 (separate file)**
926 MAGICC5.3 CO₂ concentration impulse experiment reference input file.
927
928 **Dataset S30 (separate file)**
929 MAGICC5.3 CO₂ concentration impulse experiment input file.
930
931 **Dataset S31 (separate file)**
932 MAGICC5.3 4xCO₂ concentration step experiment input file.
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934 **Dataset S32 (separate file)**
935 MAGICC5.3 4xCO₂ concentration step experiment reference input file.
936
937 **Dataset S33 (separate file)**
938 MAGICC5.3 BC emissions impulse experiment input file.
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940 **Dataset S34 (separate file)**
941 MAGICC5.3 BC emissions step experiment input file.
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943 **Dataset S35 (separate file)**
944 MAGICC5.3 CH₄ emissions impulse experiment input file.
945
946 **Dataset S36 (separate file)**
947 MAGICC5.3 1% CO₂ emissions impulse experiment in 2010 input file.

948

949 **Dataset S37 (separate file)**

950 MAGICC5.3 1.01% CO₂ emissions impulse experiment in 2010 input file.

951

952 **Dataset S38 (separate file)**

953 MAGICC5.3 5% CO₂ emissions impulse experiment in 2010 input file.

954

955 **Dataset S39 (separate file)**

956 MAGICC5.3 10% CO₂ emissions impulse experiment in 2010 input file.

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958 **Dataset S40 (separate file)**

959 MAGICC5.3 50% CO₂ emissions impulse experiment in 2010 input file.

960

961 **Dataset S41 (separate file)**

962 MAGICC5.3 100% CO₂ emissions impulse experiment in 2010 input file.

963

964 **Dataset S42 (separate file)**

965 MAGICC5.3 100% CO₂ emissions impulse experiment in 2015 input file.

966

967 **Dataset S43 (separate file)**

968 MAGICC5.3 100% CO₂ emissions impulse experiment in 2020 input file.

969

970 **Dataset S44 (separate file)**

971 MAGICC5.3 100% CO₂ emissions impulse experiment in 2030 input file.

972

973 **Dataset S45 (separate file)**

974 MAGICC5.3 100% CO₂ emissions impulse experiment in 2040 input file.

975

976 **Dataset S46 (separate file)**
977 MAGICC5.3 100% CO₂ emissions impulse experiment in 2050 input file.
978
979 **Dataset S47 (separate file)**
980 MAGICC5.3 100% CO₂ emissions impulse experiment in 2060 input file.
981
982 **Dataset S48 (separate file)**
983 MAGICC5.3 100% CO₂ emissions impulse experiment in 2070 input file.
984
985 **Dataset S49 (separate file)**
986 MAGICC5.3 100PgC CO₂ emissions impulse experiment in 2015 input file.
987
988 **Dataset S50 (separate file)**
989 MAGICC5.3 CO₂ emissions impulse experiment reference input file.
990
991 **Dataset S51 (separate file)**
992 MAGICC5.3 CO₂ emissions step experiment reference input file.
993
994 **Dataset S52 (separate file)**
995 MAGICC56.0 4xCO₂ concentration impulse experiment input file.
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997 **Dataset S53 (separate file)**
998 MAGICC56.0 4xCO₂ concentration impulse experiment reference input file.
999
1000 **Dataset S54 (separate file)**
1001 MAGICC56.0 4xCO₂ concentration step experiment input file.
1002
1003 **Dataset S55 (separate file)**

1004 MAGICC56.0 4xCO₂ concentration step experiment reference input file.
1005
1006 **Dataset S56 (separate file)**
1007 MAGICC6.0 BC emissions impulse experiment input file.
1008
1009 **Dataset S57 (separate file)**
1010 MAGICC6.0 CH₄ emissions impulse experiment input file.
1011
1012 **Dataset S58 (separate file)**
1013 MAGICC6.0 100% CO₂ emissions impulse experiment input file.
1014
1015 **Dataset S59 (separate file)**
1016 MAGICC6.0 100PgC CO₂ emissions impulse experiment input file.
1017
1018 **Dataset S60 (separate file)**
1019 MAGICC6.0 emissions impulse experiment reference input file.
1020
1021 **Dataset S61 (separate file)**
1022 MAGICC 6.0 MAGCFG_USER parameters.
1023
1024 **Dataset S62 (separate file)**
1025 FAIRv1.0 model with general parameters.
1026
1027 **Dataset S63 (separate file)**
1028 AR5-IR general parameters.
1029
1030 **Dataset S64 (separate file)**
1031 Hector general parameters.

1032

1033 **Dataset S65 (separate file)**

1034 MAGICC5.3 maggas_c parameters.

1035

1036 **Dataset S66 (separate file)**

1037 MAGICC5.3 magice_c parameters.

1038

1039 **Dataset S67 (separate file)**

1040 MAGICC5.3 magmod_c parameters.

1041

1042 **Dataset S68 (separate file)**

1043 MAGICC5.3 magrun_c parameters.

1044

1045 **Dataset S69 (separate file)**

1046 MAGICC5.3 maguser_c parameters.

1047

1048 **Dataset S70 (separate file)**

1049 MAGICC5.3 magxtra_c parameters.

1050

1051 **S15 References**

1052

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